

I. FIND THE DERIVATIVE OF EACH FUNCTION. YOU NEED NOT SIMPLIFY YOUR RESULT (IN FACT I'D RATHER PREFER IT IF YOU DIDN'T).

1.  $f(x) = 4x^5 + 5x^4$

2.  $f(x) = \sqrt{x} + \frac{1}{\sqrt[3]{x}}$

3.  $f(x) = \tan(x) - \cos(x^3)$

4.  $f(x) = \frac{x^{-3} - x}{\sin(x)}$

5.  $f(x) = x^4 \tan(x)$

6.  $f(x) = (x^{-3} - x^{-2})^{-1}$

7.  $f(x) = \frac{\sin(x)}{x^2}$

8.  $f(x) = -x \csc(x) - \cos(x)$

9.  $f(x) = \sqrt{1 + \cot(x)}$

10.  $f(x) = \left( \frac{x-2}{x-4} \right)^3$

II. FIND THE SECOND DERIVATIVE OF EACH FUNCTION.

14.  $f(x) = x^2 + \cos^2(x)$

15.  $f(x) = (x^2 + 2)^5$

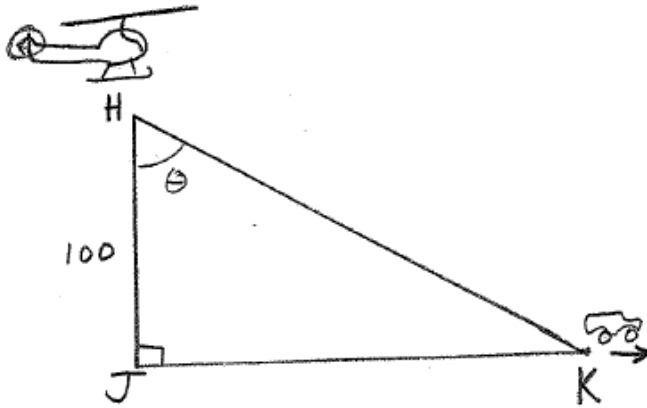
III. USE IMPLICIT DIFFERENTIATION TO FIND  $\frac{dy}{dx}$ .

16.  $x^2 + 3xy + y^3 = 10$

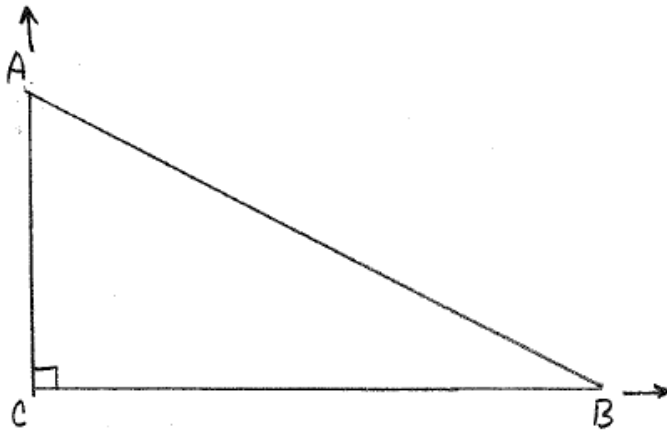
17.  $\cos(x + 2y) = x + 2y$

III. USE THE METHODS DISCUSSED IN CLASS TO SOLVE EACH PROBLEM.

18. A HELICOPTER IS HOVERING 100ft ABOVE A JEEP, WHICH IS NOT MOVING. A KIA SEDONA IS MOVING AWAY FROM THE JEEP AT THE RATE OF 3000 ft/min. HOW FAST IS THE ANGLE  $\theta$  (SEE PICTURE) CHANGING (IN DEGREES PER MINUTE) WHEN THE KIA SEDONA IS 142.85ft AWAY FROM THE JEEP?



19. FROM STARTING POINT C (SEE PICTURE) TWO STEAMROLLERS LEAVE AT THE SAME TIME. "STEAMROLLER A" IS GOING DUE NORTH AT THE RATE OF 45ft/min AND "STEAMROLLER B" IS GOING DUE EAST AT THE RATE OF 60ft/min. HOW FAST IS THE DIAGONAL DISTANCE BETWEEN THEM INCREASING 2 MINUTES AFTER THEY START?  
HINT: DETERMINE HOW FAR EACH HAS TRAVELED DURING THE TWO MINUTES.



20. A CONE IS EXPANDING IN SUCH A WAY THAT THE HEIGHT IS ALWAYS  $\sqrt{3}$  TIMES THE RADIUS. ASSUME THE CONE'S LATERAL AREA IS INCREASING AT THE RATE OF  $120\text{cm}^2/\text{min}$  WHEN THE RADIUS IS 10cm. WHAT IS THE RATE OF CHANGE OF THE CONE'S VOLUME AT THAT SAME POINT IN TIME?

THE FORMULAE FOR VOLUME AND LATERAL AREA ARE:

$$V = \frac{1}{3} \pi r^2 h$$

$$L = \pi r \sqrt{r^2 + h^2}$$