I cobbled this together from a couple different semester which is why the numbering of the problems is off. Solutions coming soon.

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- I. DETERMINE THE CONVERGENCE OR DIVERGENCE OF EACH SERIES. ALSO:
 (A) STATE THE NAME OF THE TEST YOU USE
 (B) IF A SERIES IS EITHER GEOMETRIC OR TELESCOPING, AND IT CONVERGES, FIND THE SUM OF THE SERIES.
- 1. $\sum_{n=1}^{\infty} 8(-.25)^{n-1}$ 2. $\sum_{n=1}^{\infty} \frac{n-2}{n^5+n^3-1}$ 3. $\sum_{n=1}^{\infty} \left(\frac{2}{2n-3} - \frac{2}{2n-1}\right)$ 4. $\sum_{n=1}^{\infty} \frac{(-1)^n (n-3)}{(n+1)!}$ $\frac{\infty}{n-1} (-1)^{n+1} (2\pi)^n$ $\frac{\infty}{n-2} (-1)^n (n-3)$ $\frac{\infty}{n-1} (-1)^{n+1} [3 \cdot 5 \cdot 7 \cdot ... \cdot (2n)]$

5.
$$\sum_{n=0}^{\infty} \frac{(-1)^{n+1} (2\pi)^n}{(2n)!}$$
6.
$$\sum_{n=1}^{\infty} \frac{(-1)^{n+1} [3 \cdot 5 \cdot 7 \cdot ... \cdot (2n+1)]}{(2n)!}$$

I. DETERMINE THE CONVERGENCE OR DIVERGENCE OF EACH SERIES. ALSO: (A) STATE THE NAME OF THE TEST YOU USE (B) IF A CONVERGENT SERIES IS EITHER GEOMETRIC OR TELESCOPING, FIND THE SUM OF THE SERIES.

1.
$$\sum_{n=1}^{\infty} \left(\frac{n^2}{n^2 - 3} - \frac{(n+1)^2}{n^2 + 2n - 2} \right)$$

2.
$$\sum_{n=1}^{\infty} \frac{n^2 - 2}{n^4 + 4}$$

3.
$$\sum_{n=0}^{\infty} 5(\pi - 3)^n$$

4.
$$\sum_{n=1}^{\infty} \frac{(-1)^n e^{2n}}{(n+1)!}$$

5.
$$\sum_{n=1}^{\infty} \frac{(-1)^{n+1} [2 \cdot 5 \cdot 8 \cdot ... \cdot (3n-1)]}{n!}$$

II. FIND THE INTERVAL OF CONVERGENCE FOR EACH SERIES.

6.
$$\sum_{n=0}^{\infty} \frac{(-1)^n (x-2)^n}{(2n)!}$$
7.
$$\sum_{n=1}^{\infty} \frac{(-1)^{n+1} (x+1)^n}{n+5}$$

III. GIVEN THAT $\cos(x) = \sum_{n=0}^{\infty} \frac{(-1)^{n+1} (2x)^n}{(2n)!}$

8. USE THE FIRST THREE TERMS OF THE POWER SERIES EXPANSION OF THE INTEGRAL TO FIND AN APPROXIMATION FOR $\int_{0}^{1} \cos(x^{\frac{1}{2}}) dx$.