

## Solutions

PG 1re

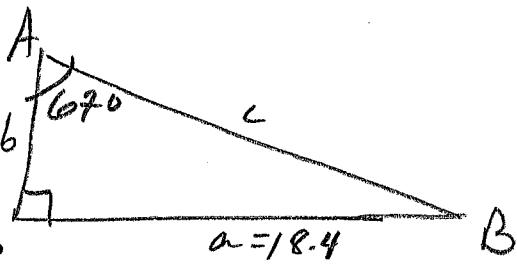
(II)

⑥ Given:

$$\angle C = 90^\circ$$

$$\angle A = 67^\circ$$

$$a = 18.4 \text{ cm}$$



Find

$\angle B = 23^\circ$
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$$b = 7.8 \text{ cm}$$

$$c = 20.0 \text{ cm}$$

$$\begin{aligned} \angle B &= 90 - \angle A \\ &= 90 - 67 \\ &= 23^\circ \end{aligned}$$

$$\frac{b}{\sin(67^\circ)} = \frac{18.4}{\sin(23^\circ)}$$

$$\Rightarrow b \cdot \tan(67^\circ) = 18.4$$

$$\Rightarrow b = \frac{18.4}{\tan(67^\circ)}$$

$$= 7.810334$$

$$= 7.8$$

$$\frac{c}{\sin(67^\circ)} = \frac{18.4}{\sin(23^\circ)}$$

$$\Rightarrow c \cdot \sin(67^\circ) = 18.4$$

$$\Rightarrow c = \frac{18.4}{\sin(67^\circ)}$$

$$= 19.98903\dots$$

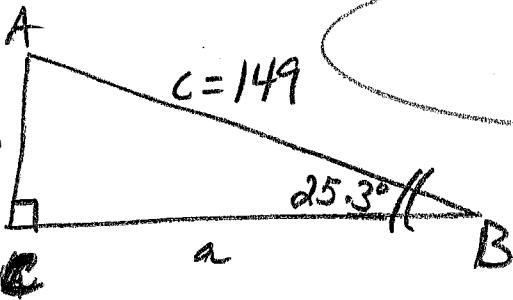
$$= 20.0$$

⑦. Given

$$\angle C = 90^\circ$$

$$\angle B = 25.3^\circ$$

$$c = 149 \text{ ft}$$



Find:

$\angle A = 64.7^\circ$
-------------------------

$$a = 134.7 \text{ ft}$$

$$b = 63.7 \text{ ft}$$

$$\begin{aligned} \angle A &= 90 - \angle B \\ &= 90 - 25.3 \\ &= 64.7^\circ \end{aligned}$$

$$\underline{\underline{a}}: \cos(25.3^\circ) = \frac{a}{149}$$

$$\Rightarrow a = 149 \cdot \cos(25.3^\circ)$$

$$= 134.70829\dots$$

$$= 134.7$$

$$\underline{\underline{b}}: \sin(25.3^\circ) = \frac{b}{149}$$

$$\Rightarrow b = 149 \cdot \sin(25.3^\circ)$$

$$= 63.67632\dots$$

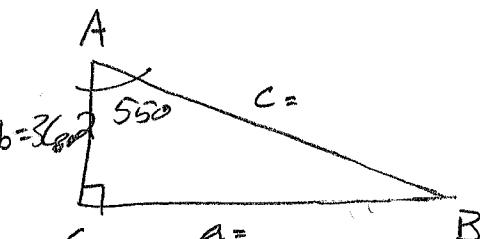
$$= 63.7$$

⑧ Given:

$$\angle C = 90^\circ$$

$$\angle A = 55^\circ$$

$$b = 36.2 \text{ m}$$



Find:

$\angle B = 35^\circ$
$a = 51.7 \text{ m}$
$c = 63.1 \text{ m}$

$$\begin{aligned} \angle B &= \\ \angle B &= 90^\circ - 55^\circ \\ &= 35^\circ \end{aligned}$$

$$\begin{aligned} \frac{a}{\tan(55^\circ)} &= \frac{a}{36.2} \\ \Rightarrow a &= 36.2 \tan(55^\circ) \end{aligned}$$

$$\begin{aligned} &= 51.69895 \dots \\ &= 51.7 \end{aligned}$$

$$\begin{aligned} \frac{c}{\cos(55^\circ)} &= \frac{36.2}{1} \\ \Rightarrow c \cdot \cos(55^\circ) &= 36.2 \end{aligned}$$

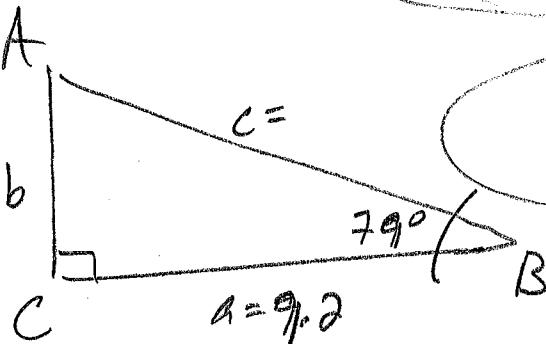
$$\begin{aligned} \Rightarrow c &= \frac{36.2}{\cos(55^\circ)} \\ &= 63.11277 \dots \\ &= 63.1 \end{aligned}$$

Given:

$$\angle C = 90^\circ$$

$$\angle B = 79^\circ$$

$$a = 9.2 \text{ in}$$



Find:

$$\angle A = 11^\circ$$

$$b = 47.3 \text{ in}$$

$$c = 48.2 \text{ in}$$

$$\begin{aligned} \angle A &= \\ \angle A &= 90^\circ - 79^\circ \\ &= 11^\circ \end{aligned}$$

$$\begin{aligned} \frac{b}{\tan(79^\circ)} &= \frac{b}{9.2} \\ \Rightarrow b &= (9.2) \cdot \tan(79^\circ) \end{aligned}$$

$$\begin{aligned} &= 47.32989 \dots \\ &= 47.3 \end{aligned}$$

$$\begin{aligned} \frac{c}{\cos(79^\circ)} &= \frac{9.2}{1} \\ \Rightarrow c \cos(79^\circ) &= 9.2 \end{aligned}$$

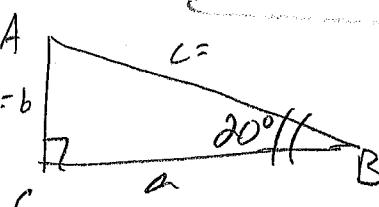
$$\begin{aligned} \Rightarrow c &= \frac{9.2}{\cos(79^\circ)} \\ &= 48.21575 \dots \\ &= 48.2 \end{aligned}$$

Given:

$$\angle C = 90^\circ$$

$$\angle B = 20^\circ$$

$$b = 88.8 \text{ cm}$$



Find:

$$\angle A = 70^\circ$$

$$a = 244.0 \text{ cm}$$

$$c = 259.6 \text{ cm}$$

$$\begin{aligned} \angle A &= \\ \angle A &= 90^\circ - \angle B \\ &= 90^\circ - 20^\circ \\ &= 70^\circ \end{aligned}$$

$$\begin{aligned} \frac{a}{\tan(20^\circ)} &= \frac{88.8}{a} \\ \Rightarrow a \cdot \tan(20^\circ) &= 88.8 \end{aligned}$$

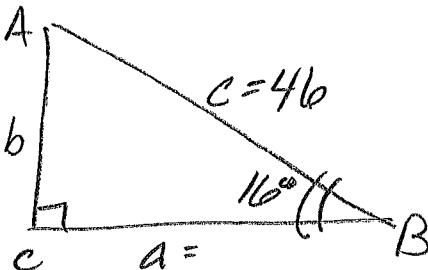
$$\begin{aligned} \Rightarrow a &= \frac{88.8}{\tan(20^\circ)} \\ &= 243.97599 \Rightarrow 244.0 \end{aligned}$$

$$\begin{aligned} \frac{b}{\sin(20^\circ)} &= \frac{88.8}{c} \\ \Rightarrow c \sin(20^\circ) &= 88.8 \end{aligned}$$

$$\begin{aligned} \Rightarrow c &= \frac{88.8}{\sin(20^\circ)} \\ &= 259.63383 \dots \\ &= 259.6 \end{aligned}$$

Pg 3hree

- (11) Given:  
 $\angle B = 16^\circ$   
 $\angle C = 90^\circ$   
 $C = 46\text{m}$



Find:

$$\begin{aligned}\angle A &= 74^\circ \\ a &= 44.2 \text{ m} \\ b &= 12.7 \text{ m}\end{aligned}$$

$$\begin{aligned}\angle A &= 90 - \angle B \\ &= 90 - 16 \\ &= 74^\circ\end{aligned}$$

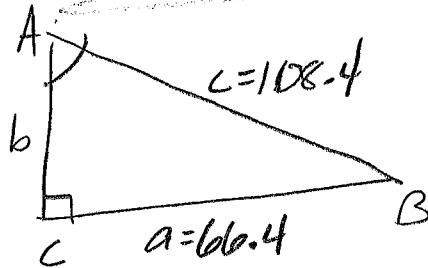
$$\frac{a}{c} = \cos(16^\circ) = \frac{a}{46}$$

$$\begin{aligned}\Rightarrow a &= 46 \cdot \cos(16^\circ) \\ &= 44.21803\dots \\ &= 44.2\end{aligned}$$

$$\begin{aligned}\frac{b}{c} &= \sin(16^\circ) = \frac{b}{46} \\ \Rightarrow b &= 46 \cdot \sin(16^\circ) \\ &= 12.67931\dots \\ &= 12.7\end{aligned}$$

- (12) Given:

$$\begin{aligned}\angle C &= 90^\circ \\ a &= 66.4 \text{ cm} \\ c &= 108.4 \text{ cm}\end{aligned}$$



Find:

$$\begin{aligned}\angle A &= 37.8^\circ \\ \angle B &= 52.2^\circ \\ b &= 85.6 \text{ cm}\end{aligned}$$

$$\begin{aligned}\frac{a}{c} &= \sin(A) = \frac{66.4}{108.4} \\ \Rightarrow 108.4 \cdot \sin(A) &= 66.4 \\ \Rightarrow \sin(A) &= \frac{66.4}{108.4} \\ \Rightarrow A &= \sin^{-1}\left(\frac{66.4}{108.4}\right)\end{aligned}$$

$$\Rightarrow A = 37.77383\dots = 37.8^\circ$$

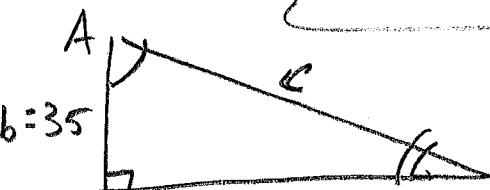
$$\begin{aligned}\angle B &= 90 - \angle A \\ &= 90 - 37.8 \\ &= 52.2^\circ\end{aligned}$$

$$b = \tan(37.8^\circ) = \frac{66.4}{b}$$

$$\begin{aligned}\Rightarrow b \cdot \tan(37.8^\circ) &= 66.4 \\ \Rightarrow b &= \frac{66.4}{\tan(37.8^\circ)} \\ &= 85.60236\dots \\ &= 85.6\end{aligned}$$

- (13) Given:

$$\begin{aligned}\angle C &= 90^\circ \\ a &= 42 \text{ m} \\ b &= 35 \text{ m}\end{aligned}$$



Find:

$$\begin{aligned}\angle A &= 50.2^\circ \\ \angle B &= 39.8^\circ \\ c &= 54.7 \text{ m}\end{aligned}$$

$$\begin{aligned}\frac{a}{c} &= \cos(50.2^\circ) = \frac{42}{35} \\ \Rightarrow 35 \cdot \cos(50.2^\circ) &= 42 \\ \Rightarrow \cos(50.2^\circ) &= \frac{42}{35} \\ \Rightarrow A &= \cos^{-1}\left(\frac{42}{35}\right) \\ &= 50.19442\dots = 50.2\end{aligned}$$

$$\begin{aligned}\frac{b}{c} &= \sin(50.2^\circ) = \frac{35}{c} \\ \Rightarrow 35 \cdot \sin(50.2^\circ) &= b \\ \Rightarrow \sin(50.2^\circ) &= \frac{b}{35} \\ \Rightarrow B &= \sin^{-1}\left(\frac{b}{35}\right) \\ &= 39.8\end{aligned}$$

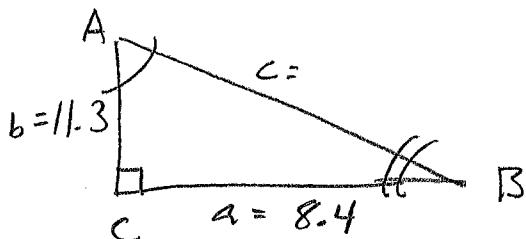
$$\begin{aligned}\frac{c}{c} &= \frac{35}{\cos(50.2^\circ)} \\ \Rightarrow c \cdot \cos(50.2^\circ) &= 35 \\ \Rightarrow c &= \frac{35}{\cos(50.2^\circ)} \\ &= 54.67812\dots \\ &= 54.7\end{aligned}$$

(14) Given:

$$\angle C = 90^\circ$$

$$a = 8.4 \text{ cm}$$

$$b = 11.3 \text{ cm}$$



Find:

$$\angle A = 36.6^\circ$$

$$\angle B = 53.4^\circ$$

$$c = 14.1 \text{ cm}$$

$\angle A$ :

$$\tan(A) = \frac{8.4}{11.3}$$

$$\Rightarrow A = \tan^{-1}\left(\frac{8.4}{11.3}\right)$$

$$= 36.62574\ldots$$

$$= 36.6^\circ$$

$\angle B$ :

$$\angle B = 90 - \angle A$$

$$= 90 - 36.6$$

$$= 53.4^\circ$$

$$\Rightarrow c \cdot \cos(36.6^\circ) = 11.3$$

$$\Rightarrow c = \frac{11.3}{\cos(36.6^\circ)}$$

$$= 14.07542\ldots$$

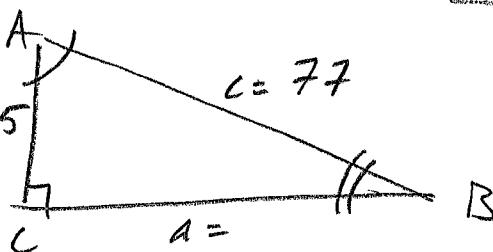
$$= 14.1$$

(15) Given:

$$\angle C = 90^\circ \quad b = 65$$

$$b = 65 \text{ m}$$

$$c = 77 \text{ m}$$



Find:

$$\angle A = 32.4^\circ$$

$$\angle B = 57.6^\circ$$

$$a = 41.3 \text{ m}$$

$\angle A$ :

$$\cos(A) = \frac{65}{77}$$

$$\Rightarrow A = \cos^{-1}\left(\frac{65}{77}\right)$$

$$= 32.41839\ldots$$

$$= 32.4^\circ$$

$$\angle B = 90 - \angle A$$

$$= 90 - 32.4$$

$$= 57.6^\circ$$

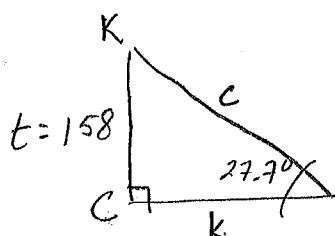
$$\frac{a}{c} = \tan(32.4^\circ) = \frac{a}{65}$$

$$\Rightarrow a = 65 \cdot \tan(32.4^\circ)$$

$$= 41.25025\ldots$$

$$= 41.3$$

(16)



Given:

$$\angle C = 90^\circ$$

$$\angle T = 27.2^\circ$$

$$t = 158 \text{ m}$$

Find:

- $k = 300.9 \text{ m}$
- $c = 339.9 \text{ m}$

(a) Find  $k$ :

$$\frac{\tan(27.2^\circ)}{1} = \frac{158}{k}$$

$$\Rightarrow k \cdot \tan(27.2^\circ) = 158$$

$$\Rightarrow k = 158 / \tan(27.2^\circ)$$

$$= 300.94565\ldots$$

$$= 300.9 \text{ m}$$

(b) Find  $c$ :

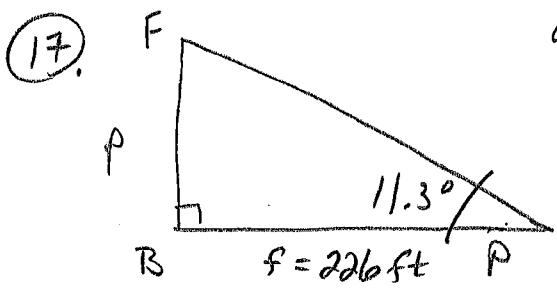
$$\frac{\sin(27.2^\circ)}{1} = \frac{158}{c}$$

$$\Rightarrow c \cdot \sin(27.2^\circ) = 158$$

$$\Rightarrow c = 158 / \sin(27.2^\circ)$$

$$= 339.90040\ldots$$

$$= 339.9 \text{ m}$$



Given:  $\angle B = 90^\circ$   
 $f = 226 \text{ ft}$   
 $\angle P = 11.3^\circ$

Find:  $P$

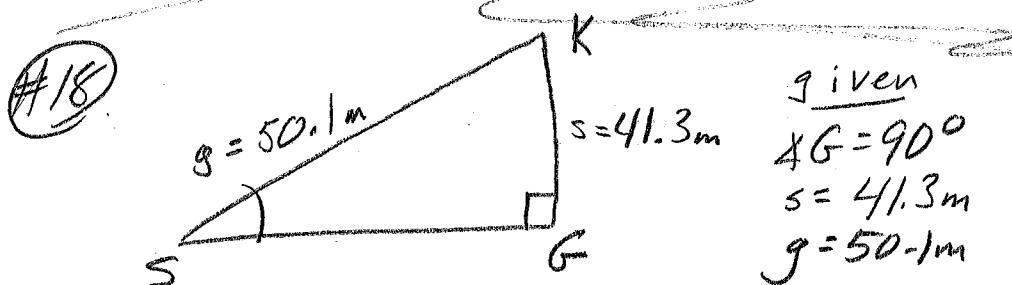
$$P = 45.2 \text{ ft}$$

P: pg 5 five  
 $\tan(11.3^\circ) = \frac{P}{226}$

$$\Rightarrow P = 226 \cdot \tan(11.3^\circ)$$

$$= 45.15925 \dots$$

$$= 45.2 \text{ ft}$$

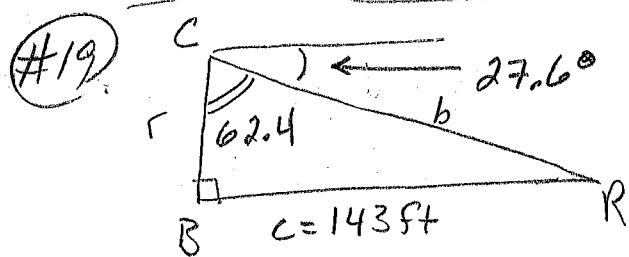


Given  
 $\angle G = 90^\circ$   
 $s = 41.3 \text{ m}$   
 $g = 50.1 \text{ m}$

Find:  
 $\angle S = 55.5^\circ$

$\angle S = \sin(\angle S) = \frac{41.3}{50.1} \Rightarrow \angle S = 55.52277 \dots$   
 $= 55.5^\circ$

$$\Rightarrow \angle S = \sin^{-1}\left(\frac{41.3}{50.1}\right)$$

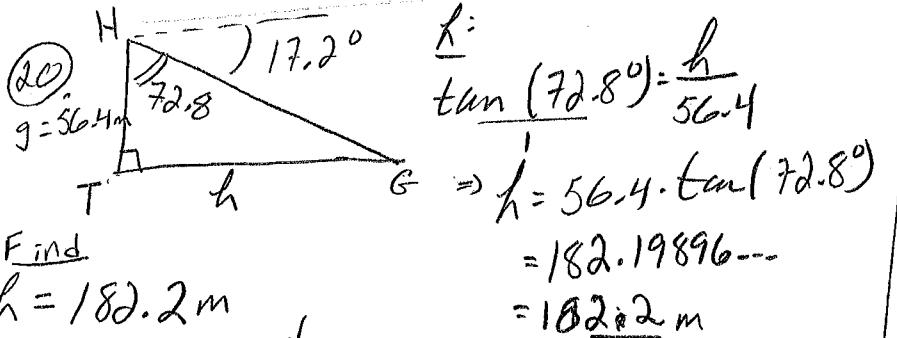


Find: (a)  $\angle R = 27.6^\circ$   
(b)  $r = 74.8 \text{ ft}$

Given:  
 $\angle B = 90^\circ$   
 $c = 143 \text{ ft}$   
Coyote's angle of depression =  $27.6^\circ$   
so  $\angle BCR = 90 - 27.6 = 62.4^\circ$

(a):  
 $\angle R = 90 - \angle BCR$   
 $= 90 - 62.4^\circ$   
 $= 27.6^\circ$

(b).  $\tan(62.4^\circ) = \frac{143}{r}$   
 $\Rightarrow r \cdot \tan(62.4^\circ) = 143$   
 $\Rightarrow r = 143 / \tan(62.4)$   
 $= 74.75859 \dots$   
 $= 74.8 \text{ ft}$



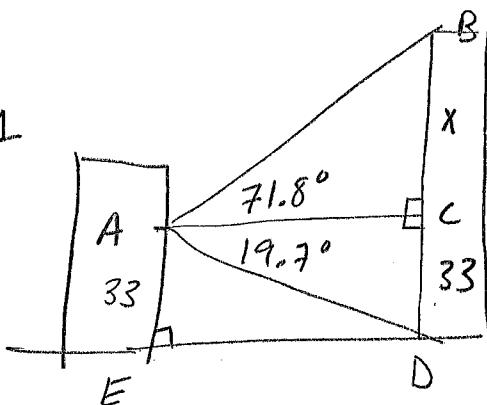
$\frac{h}{\tan(17.2^\circ)} = \frac{h}{56.4}$   
 $\Rightarrow h = 56.4 \cdot \tan(17.2^\circ)$   
 $= 182.19896 \dots$   
 $= 182.2 \text{ m}$

Find:  
 $h = 182.2 \text{ m}$

Given:  $g = 56.4$   
Angle of depression =  $17.2^\circ$   
 $\Rightarrow \angle THG = 90 - 17.2^\circ = 72.8^\circ$

(21)

#1



NOTE:

We may use  $CD = 33$

in  $\triangle ADC$  to find

length AC

Then switch to  $\triangle ABC$   
and use the AC value  
to find  $x = BC$

Finally Notice:

$$\underline{\underline{BD = BC + CD}}$$

$\underline{\underline{BD}}$  in  $\triangle ADC$

$$\tan(19.7^\circ) = \frac{33}{AC}$$

$$\Rightarrow AC \cdot \tan(19.7^\circ) = 33$$

$$\Rightarrow AC = \frac{33}{\tan(19.7^\circ)}$$

$$= 92.16542 \dots$$

$$= 92.2$$

#2 Given:

$$AE = 33$$

$$\text{so } CD = 33$$

$$\angle DAC = 19.7^\circ$$

$$\angle CAB = 71.8^\circ$$

Find  $BD = m$

Pg 6ix

Now, SWITCHING TO  $\triangle ABC$ :

$$\tan(71.8^\circ) = \frac{x}{92.2}$$

$$\Rightarrow x = 92.2 \cdot \tan(71.8^\circ)$$

$$= 280.42789 \dots$$

$$= 280.4$$

So Finally:

Height of BLDG #2 = BD

$$BD = BC + CD$$

$$= 280.4 + 33$$

$$= \boxed{313.4 \text{ m}}$$