

Trigonometry Unit #1

Form #1

* If your item #1 references 45, you have Form #1.

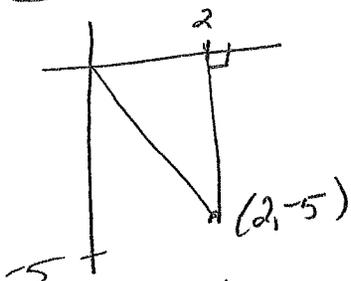
- I**
- ① B
 - ④ A
 - ⑦ D
 - ⑨ D
 - ② C
 - ⑤ Free
 - ⑧ D
 - ⑩ A
 - ③ FLBB
 - ⑥ D

II ⑪. α and β are alternate exterior angles, so they are equal:

$$\alpha = \beta \Rightarrow \begin{array}{r} 4x + 30 = 6x - 20 \\ -4x + 20 \quad -4x + 20 \\ \hline 50 = 2x \\ 25 = x \end{array}$$

$$\begin{array}{l} \overset{50}{\alpha} = 4(25) + 30 = \boxed{130^\circ} \\ \beta = 6(25) - 20 = \boxed{130^\circ} \end{array}$$

III ⑫. $P = (2, -5)$



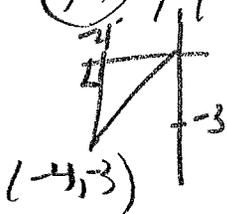
$$\begin{array}{l} \Rightarrow x = 2 \checkmark \\ y = -5 \checkmark \\ r = \sqrt{(2)^2 + (-5)^2} \\ = \sqrt{4 + 25} \\ = \sqrt{29} \checkmark \end{array}$$

$$\overset{50}{\sin}(\theta) = -\frac{5}{\sqrt{29}} \quad \csc(\theta) = -\frac{\sqrt{29}}{5}$$

$$\cos(\theta) = \frac{2}{\sqrt{29}} \quad \sec(\theta) = \frac{\sqrt{29}}{2}$$

$$\tan(\theta) = -\frac{5}{2} \quad \cot(\theta) = -\frac{2}{5}$$

⑭ $P(-4, -3)$



$$\begin{array}{l} x = -4 \checkmark \\ y = -3 \checkmark \\ r = \sqrt{(-4)^2 + (-3)^2} \\ = \sqrt{16 + 9} \\ = \sqrt{25} = 5 \checkmark \end{array}$$

$$\overset{50}{\sin}(\theta) = -\frac{3}{5} \quad \csc(\theta) = -\frac{5}{3}$$

$$\cos(\theta) = -\frac{4}{5} \quad \sec(\theta) = -\frac{5}{4}$$

$$\tan(\theta) = \frac{-3}{-4} = \frac{3}{4} \quad \cot(\theta) = \frac{4}{3}$$

III

15) Verify $\sin(\theta) = \frac{1}{\csc(\theta)}$

⊕ start with the more complicated side:

$$\begin{aligned} \frac{1}{\csc(\theta)} &= \frac{1}{\frac{r}{y}} \\ &= 1 \cdot \frac{y}{r} \\ &= \frac{y}{r} \\ &= \sin(\theta) \checkmark \end{aligned}$$

16) Verify: $\cot(\theta) = \frac{\csc(\theta)}{\sec(\theta)}$

$$\begin{aligned} \frac{\csc(\theta)}{\sec(\theta)} &= \frac{\frac{r}{y}}{\frac{r}{x}} \\ &= \frac{r}{y} \cdot \frac{x}{r} \\ &= \frac{x}{y} \\ &= \cot(\theta) \checkmark \end{aligned}$$