

Solving Trigonometric Equations

Find all solutions of the equation in the given interval.

#	Problem	Interval	Answers
1.	$1 + \cos x = 0$	$[0, 2\pi)$	$\{\pi\}$
2.	$\sqrt{3} - 2\sin x = 0$	$[0, 2\pi)$	$\left\{\frac{\pi}{3}, \frac{2\pi}{3}\right\}$
3.	$2\sin x \cos x - \sin x = 0$	$[0, 2\pi)$	$\left\{0, \pi, \frac{\pi}{3}, \frac{5\pi}{3}\right\}$
4.	$\cos x = 0$	$[0, 2\pi)$	$\left\{\frac{\pi}{2}, \frac{3\pi}{2}\right\}$
5.	$-\sin x = 0$	$[0, 2\pi)$	$\{0, \pi\}$
6.	$\frac{1}{2} - \sin x = 0$	$[0, 2\pi)$	$\left\{\frac{\pi}{6}, \frac{5\pi}{6}\right\}$
7.	$2\sin x \cos x + \cos x = 0$	$[0, 2\pi)$	$\left\{\frac{\pi}{2}, \frac{3\pi}{2}, \frac{7\pi}{6}, \frac{11\pi}{6}\right\}$
8.	$-\sin x - 1 = 0$	$[0, 4\pi)$	$\left\{\frac{3\pi}{2}, \frac{7\pi}{2}\right\}$
9.	$2 - \sec^2 x = 0$	$\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$	$\left\{-\frac{\pi}{4}, \frac{\pi}{4}\right\}$
10.	$2 - \csc^2 x = 0$	$(0, \pi)$	$\left\{\frac{\pi}{4}, \frac{3\pi}{4}\right\}$
11.	$1 - 2\cos x = 1$	$[-\pi, \pi]$	$\left\{\frac{\pi}{2}, -\frac{\pi}{2}\right\}$
12.	$2\sec^2 x = \frac{8}{\pi}$	$\left[-\frac{\pi}{4}, \frac{\pi}{4}\right]$	$\{\pm 0.4817\}$
13.	$\cos x = \frac{3\sqrt{3}}{2\pi}$	$\left[-\frac{\pi}{3}, \frac{\pi}{3}\right]$	$\{\pm 0.5971\}$
14.	$\sin x = \frac{2}{\pi}$	$[0, \pi]$	$\{0.6901, 2.4515\}$
15.	$\cos x = \frac{2}{\pi}$	$\left[0, \frac{\pi}{2}\right]$	$\{0.8807\}$
16.	$2\sec \theta \tan \theta + \sec^2 \theta = 0$	$[0, 2\pi)$	$\left\{\frac{7\pi}{6}, \frac{11\pi}{6}\right\}$
17.	$\sec x \tan x = 0$	$\left[-\frac{\pi}{4}, \frac{\pi}{4}\right]$	$\{0\}$
18.	$2\cos x + 2\cos 2x = 0$	$[0, \pi]$	$\left\{\frac{\pi}{3}, \pi\right\}$

19.	$2 \cos x - 2 \sin 2x = 0$	$[0, 2\pi)$	$\left\{ \frac{\pi}{2}, \frac{3\pi}{2}, \frac{\pi}{6}, \frac{5\pi}{6} \right\}$
20.	$-2 \sin x - 4 \sin 2x = 0$	$[0, 2\pi)$	$\{0, \pi, 1.8235, 4.4597\}$
21.	$-\sin x + \sin 2x = 0$	$[0, 2\pi)$	$\left\{ 0, \pi, \frac{\pi}{3}, \frac{5\pi}{3} \right\}$
22.	$-\cos x + 2 \cos 2x = 0$	$[0, 2\pi)$	$\{0.5678, 2.2057, 4.0775, 5.7154\}$
23.	$2 \csc^2 x \cot x = 0$	$(0, \pi)$	$\left\{ \frac{\pi}{2} \right\}$
24.	$2 \sin x = \tan x$	$\left[-\frac{\pi}{3}, \frac{\pi}{3} \right]$	$\left\{ \pm \frac{\pi}{3}, 0 \right\}$
25.	$\sin 2x = \cos x$	$\left[\frac{\pi}{6}, \frac{5\pi}{6} \right]$	$\left\{ \frac{\pi}{6}, \frac{\pi}{2}, \frac{5\pi}{6} \right\}$
26.	$2 \sin x + \sin 2x = 0$	$[0, \pi]$	$\{0, \pi\}$
27.	$-\pi \sin \pi x = 0$	$\left[0, \frac{1}{6} \right)$	$\{0\}$
28.	$2 \cos 2x = 0$	$\left[\frac{\pi}{6}, \frac{\pi}{3} \right]$	$\left\{ \frac{\pi}{4} \right\}$
29.	$4 - \pi \sec^2 \pi x = 0$	$\left[-\frac{1}{4}, \frac{1}{4} \right]$	$\{\pm 0.1533\}$
30.	$\frac{1}{2} - \frac{\pi}{6} \cos \frac{\pi}{6} x = 0$	$[-1, 0]$	$\{-0.5756\}$
31.	$\frac{6}{\pi} - 8 \sin x \cos x = 0$	$\left[0, \frac{\pi}{6} \right]$	$\{0.2489\}$
32.	$\cos^2 x - \sin^2 x = 0$	$[0, 2\pi)$	$\left\{ \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4} \right\}$
33.	$\frac{1}{2} \cos \frac{x}{2} = 0$	$[0, 4\pi)$	$\{\pi, 3\pi\}$
34.	$-\frac{1}{4} \sin \frac{x}{2} = 0$	$[0, 4\pi)$	$\{0, 2\pi\}$
35.	$-3 \csc \frac{3x}{2} \cot \frac{3x}{2} = 0$	$(0, 2\pi)$	$\left\{ \frac{\pi}{3}, \pi, \frac{5\pi}{3} \right\}$
36.	$\cos x - \sin x = 0$	$[0, 2\pi)$	$\left\{ \frac{\pi}{4}, \frac{5\pi}{4} \right\}$
37.	$-\sin x - \cos x = 0$	$[0, 2\pi)$	$\left\{ \frac{3\pi}{4}, \frac{7\pi}{4} \right\}$