

From

RR 17

Note Title

2/5/2015

Review:

$$2x - y = 8$$

 $x=0$

$$\begin{aligned} 2(0) - y &= 8 \\ 0 - y &= 8 \\ -y &= 8 \\ \frac{-y}{1} &= \frac{8}{-1} \end{aligned}$$

$$y = -8 \quad (0, -8)$$

x	y
0	-8
-1	-10
2	-4
	-6
	2

 $x=-1$

$$2(-1) - y = 8$$

$$\begin{aligned} -2 - y &= 8 \\ +2 &+2 \\ -y &= 10 \\ \frac{-y}{-1} &= \frac{10}{-1} \\ y &= -10 \end{aligned}$$

$$(-1, -10)$$

 $x=2$

$$2x - y = 8$$

$$\begin{aligned} 2(2) - y &= 8 \\ 4 - y &= 8 \\ -4 &-4 \\ -y &= 4 \\ \frac{-y}{-1} &= \frac{4}{-1} \\ y &= -4 \end{aligned}$$

$$(2, -4)$$

 $y=-6$

$$2x - y = 8$$

$$2x - (-6) = 8$$

$$2x + 6 = 8$$

$$-6 -6$$

$$\begin{aligned} 2x &= 2 \\ \frac{2x}{2} &= \frac{2}{2} \end{aligned}$$

$$x = 1$$

$$(1, -6)$$

 $y=2$

$$2x - 2 = 8$$

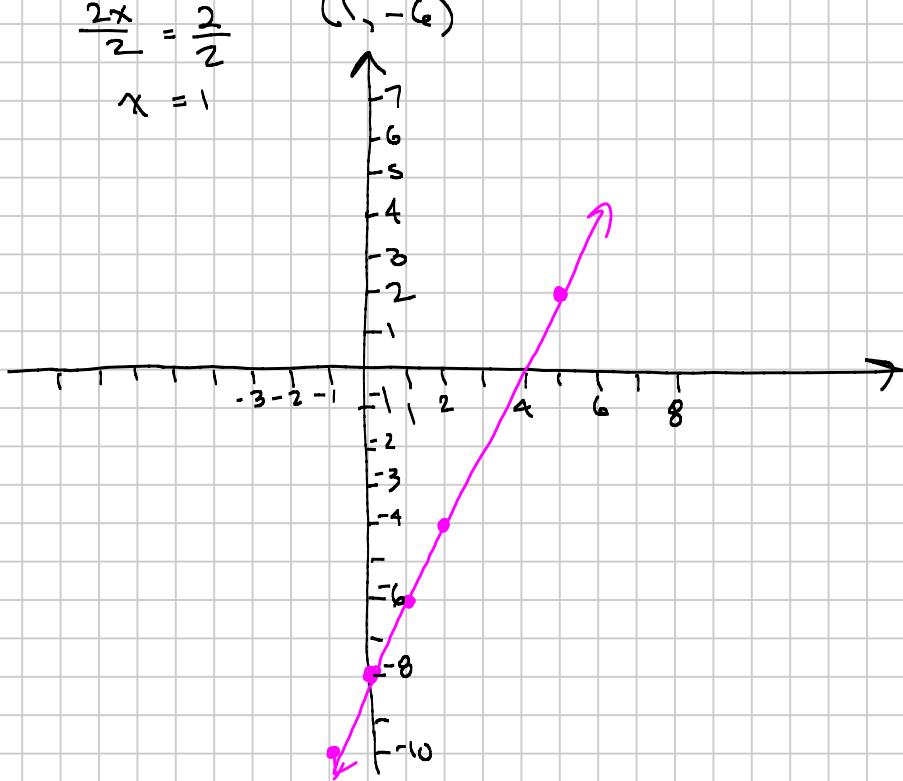
$$+2 +2$$

$$2x = 10$$

$$\frac{2x}{2} = \frac{10}{2}$$

$$x = 5$$

$$(5, 2)$$



3.2: Linear equations in two variables (cont'd)

3.2.4

Example: Find at least 5 ordered pair solutions.
Graph the line.

$$x - 2y = -6$$

Points:

$$(-4, 0)$$

$$(-2, 2)$$

$$(0, 3)$$

$$(0, 1)$$

$$(2, 4)$$

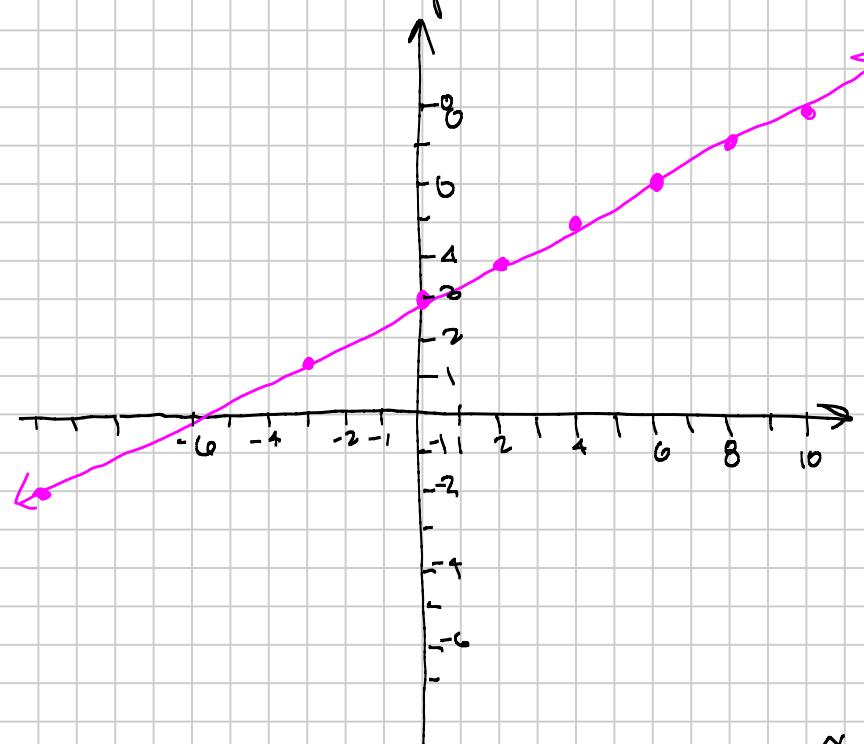
$$(-3, 1\frac{1}{2})$$

$$(10, 8)$$

$$(-10, -2)$$

$$(0, 3)$$

$$(4, 5)$$



$$\underline{x = 8}$$

$$x - 2y = -6$$

$$8 - 2y = -6$$

$$-8$$

$$-2y = -14$$

$$\frac{-2y}{-2} = \frac{-14}{-2}$$

$$y = 7 \quad (8, 7)$$

$$\underline{x = -3} \quad -3 - 2y = -6$$

$$+3 \qquad +3$$

$$-2y = -3$$

$$\frac{-2y}{-2} = \frac{-3}{-2}$$

$$y = \frac{3}{2} = 1\frac{1}{2}$$

Ex. Solve the equation for y first.
Then find solutions and graph.

$$6x + 2y = -10$$

$$-6x \qquad -6x$$

$$2y = -10 - 6x$$

$$\frac{2y}{2} = \frac{-10}{2} - \frac{6x}{2}$$

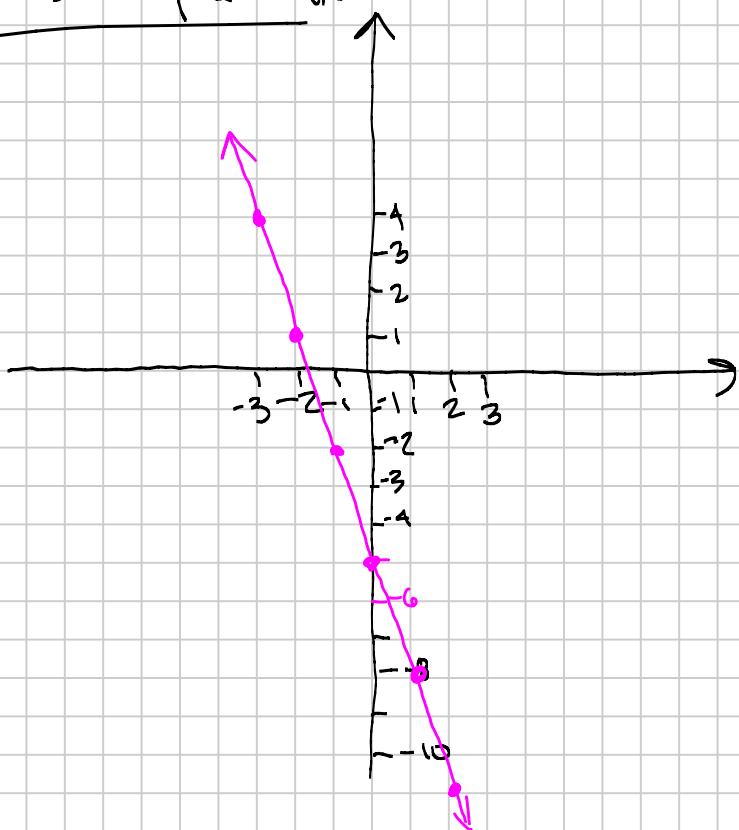
$$y = -5 - 3x$$

See next page for graph

$$\begin{array}{|c|l|l|l|} \hline x & y = -5 - 3x & & \\ \hline -3 & y = -5 - 3(-3) = -5 + 9 = 4 & (-3, 4) & \\ \hline -2 & y = -5 - 3(-2) = -5 + 6 = 1 & (-2, 1) & \\ \hline -1 & y = -5 - 3(-1) = -5 + 3 = -2 & (-1, -2) & \\ \hline 0 & y = -5 - 3(0) = -5 - 0 = -5 & (0, -5) & \\ \hline 1 & y = -5 - 3(1) = -5 - 3 = -8 & (1, -8) & \\ \hline 2 & y = -5 - 3(2) = -5 - 6 = -11 & (2, -11) & \\ \hline 3 & y = -5 - 3(3) = -5 - 9 = -14 & (3, -14) & \\ \hline \end{array}$$

Previous example cont'd:

3.2.5



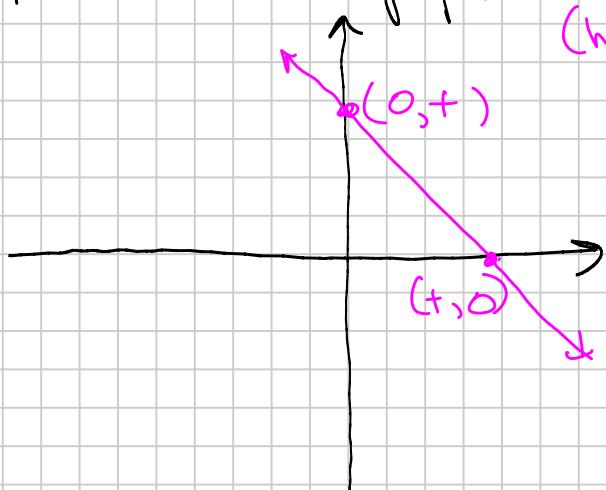
(-3, 4)
(-2, 1)
(-1, -2)
(0, -5)
(1, -8)
(2, -11)
(3, -14)

Intercepts:

x-intercept: a point where the graph intersects the x-axis.
(has the form $(a, 0)$ or just a)

y-intercept: a point where the graph intersects the y-axis.

(has the form $(0, b)$ or just b)



How to find intercepts:

* To find the x-intercept, set $y=0$ and solve for x .

* To find the y-intercept, set $x=0$ and solve for y .

3.2.6

Ex. Find the intercepts and graph the line.

$$4x - y = 20$$

Find the x-intercept: Set $y=0$:

$$4x - 0 = 20$$

$$4x = 20$$

$$\frac{4x}{4} = \frac{20}{4}$$

$$x = 5 \quad (5, 0)$$

Find y-intercept:

$$\text{Set } x=0: 4(0) - y = 20$$

$$0 - y = 20$$

$$-y = 20$$

$$\frac{-y}{-1} = \frac{20}{-1}$$

$$y = -20$$

$$(0, -20)$$

The x-intercept is $(5, 0)$. (or just 5).

The y-intercept is $(0, -20)$. (or just -20)

Find an extra point:

$$\boxed{x=2}$$

$$4x - y = 20$$

$$4(2) - y = 20$$

$$8 - y = 20$$

$$-8 \quad -8$$

$$-y = 12$$

$$y = -12$$

$$(2, -12)$$

$$\boxed{x=9}$$

$$4(9) - y = 20$$

$$36 - y = 20$$

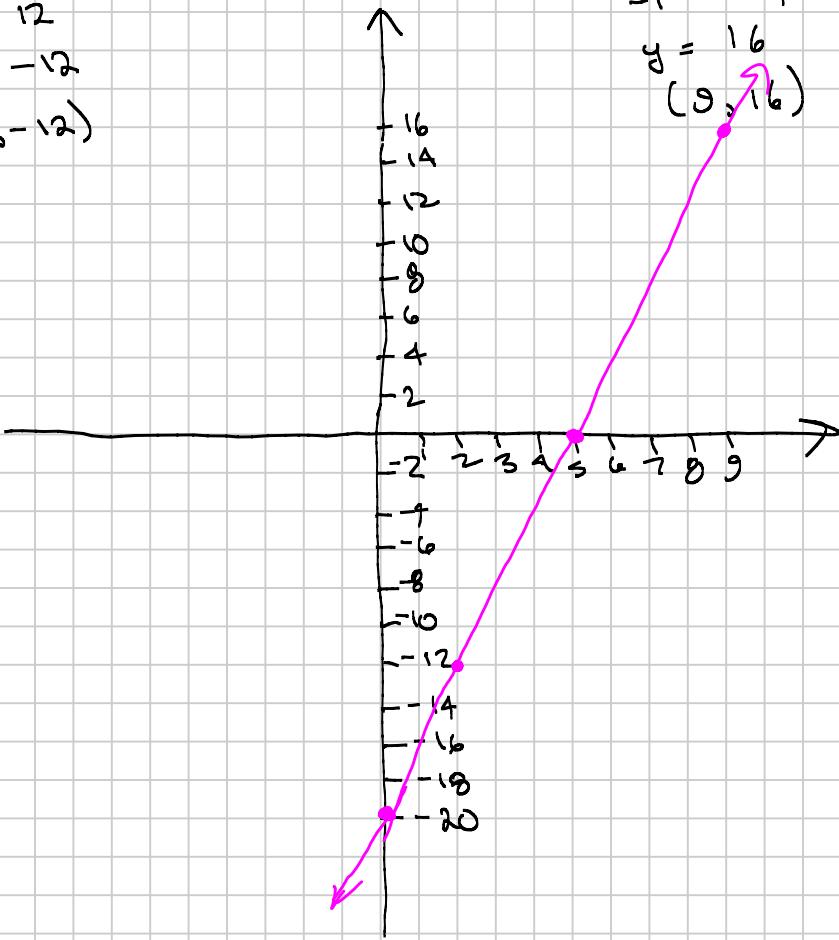
$$\cancel{-36} \quad \cancel{-36}$$

$$-y = -16$$

$$\frac{-y}{-1} = \frac{-16}{-1}$$

$$y = 16$$

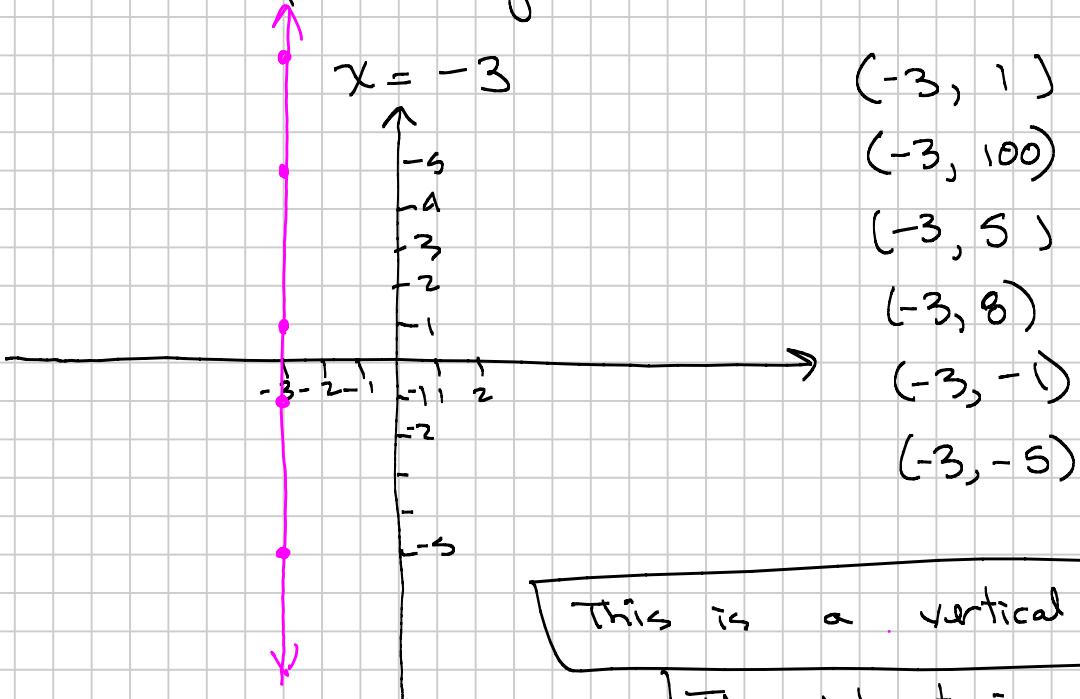
$$(9, 16)$$



Intercepts: $(0, -20)$
 $(5, 0)$

(3.2.7)

Ex. Graph the equation.



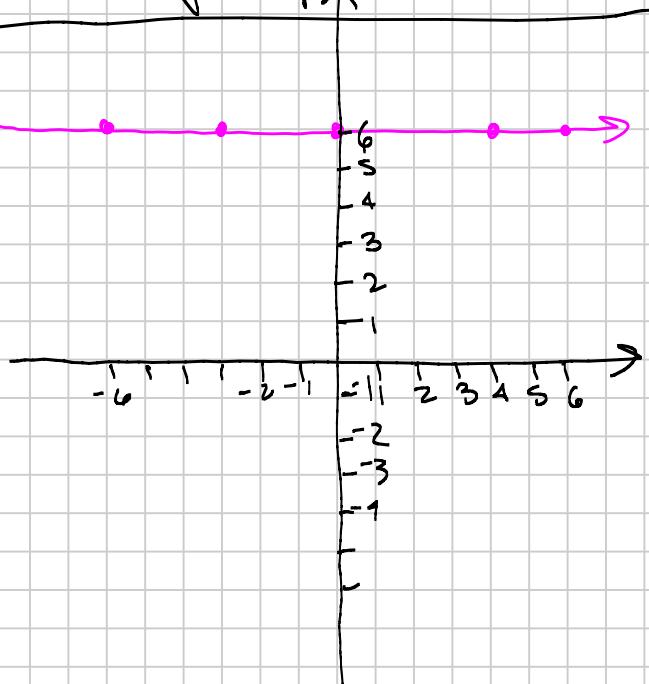
This is a vertical line.

The x-intercept is -3 or $(-3, 0)$.
There is no y-intercept.

Ex. Graph the equation.

$$y = 6$$

- $(-6, 6)$
 $(-5, 6)$
 $(-4, 6)$
 $(-3, 6)$
 $(-2, 6)$
 $(-1, 6)$
 $(0, 6)$



This is a horizontal line.

The x-intercept does not exist.
(there is no x-intercept)

The y-intercept is 6 or $(0, 6)$.