

6.7: Solving Quadratic Equations by Factoring (cont'd)

Note Title

11/5/2018

6.7.3

Ex: Solve.

$$x^2 - 19x = -60$$

+60 +60

$$x^2 - 19x + 60 = 0$$

$$(x - 4)(x - 15) = 0$$

$$x - 4 = 0 \text{ or } x - 15 = 0$$

+4 +4

$$x = 4$$

+15 +15

$$x = 15$$

Sol'n Set: $\{4, 15\}$

Recall:

- * Equations get solved
- * Expressions get simplified or factored

$$\begin{array}{r} x^2 \\ \wedge \\ x \cdot x \\ 1 \cdot 60 \\ 2 \cdot 30 \\ 3 \cdot 20 \\ 4 \cdot 15 \\ 5 \cdot 12 \\ 6 \cdot 10 \end{array}$$

4x

15x

$$x^2 - 19x + 60$$

sample signs sum of 19x

Check:

$$\begin{aligned} (x - 4)(x - 15) \\ x^2 - 15x - 4x + 60 \\ x^2 - 19x + 60 \end{aligned}$$

Recall: Steps for solving a quadratic equation.

1) Write in standard form $ax^2 + bx + c = 0$.

2) Factor the non zero side.

3) Set each factor equal to zero. (Apply the Zero Product Property).

4) Solve the resulting equations.

6.7.4

Ex. Solve.

$$6x^2 - 5 = 7x$$

-7x -7x

$$6x^2 - 7x - 5 = 0$$

$$(2x + 1)(3x - 5) = 0$$

$2x + 1 = 0$ -1 -1 $2x = -1$ $\frac{2x}{2} = \frac{-1}{2}$ $x = -\frac{1}{2}$	$3x - 5 = 0$ +5 +5 $3x = 5$ $\frac{3x}{3} = \frac{5}{3}$ $x = \frac{5}{3}$
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Check: $(2x + 1)(3x - 5)$

$$= 6x^2 - 10x + 3x - 5$$

$$= 6x^2 - 7x - 5 \checkmark$$

Sol'n Set: $\left\{-\frac{1}{2}, \frac{5}{3}\right\}$

Ex. Solve.

$$(w + 5)(w - 3) = 20$$

$$w^2 - 3w + 5w - 15 = 20$$

$$w^2 + 2w - 15 = 20$$

-20 -20

$$w^2 + 2w - 35 = 0$$

$$(w - 5)(w + 7) = 0$$

$w - 5 = 0$ $w = 5$	$w + 7 = 0$ $w = -7$
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Sol'n Set: $\{5, -7\}$

Ex: Solve.

$$x^2 = 9$$

$$x^2 - 9 = 0$$

$$(x+3)(x-3) = 0$$

$$\begin{array}{l|l} x+3=0 & x-3=0 \\ -3 & +3 \\ x=-3 & x=3 \end{array}$$

Recall:
 $a^2 - b^2 = (a+b)(a-b)$

Sol'n Set: $\boxed{\{3, -3\}}$

Also written: $\boxed{\{\pm 3\}}$

read "plus or minus 3"

Ex: $9x - 6x^2 = -x^3$

$$+x^3$$

$$+x^3$$

$$x^3 + 9x - 6x^2 = 0$$

$$x^3 - 6x^2 + 9x = 0$$

$$x(x^2 - 6x + 9) = 0$$

$$x(x-3)(x-3) = 0$$

$$\begin{array}{l|l|l} x=0 & x-3=0 & x-3=0 \\ & x=3 & x=3 \end{array}$$

Sol'n Set: $\boxed{\{0, 3\}}$

$$\begin{array}{cc} x^2 & 9 \\ \wedge & \wedge \\ x \cdot x & 3 \cdot 3 \end{array}$$

Check: $(x-3)(x-3)$
 $= x^2 - 3x - 3x + 9$
 $= x^2 - 6x + 9 \checkmark$

6.7.6

Ex.: Solve. $128 - 18x^2 = 0$
 $-18x^2 + 128 = 0$
 $-2(9x^2 - 64) = 0$

$$-2(3x+8)(3x-8) = 0$$

$-2=0$ cannot be true. False for every x ! This factor does not contribute any solutions.	$3x+8=0$ $-8 \quad -8$ $3x = -8$ $\frac{3x}{3} = \frac{-8}{3}$ $x = -\frac{8}{3}$	$3x-8=0$ $+8 \quad +8$ $3x = 8$ $\frac{3x}{3} = \frac{8}{3}$ $x = \frac{8}{3}$
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Solution Set:

$$\left\{-\frac{8}{3}, \frac{8}{3}\right\}$$

or $\left\{\pm \frac{8}{3}\right\}$

Ex.: $5x(2x-5)(x+4)=0$

Solve.

$5x=0$ $\frac{5x}{5} = \frac{0}{5}$ $x=0$	$2x-5=0$ $2x=5$ $\frac{2x}{2} = \frac{5}{2}$ $x = \frac{5}{2}$	$x+4=0$ $x=-4$
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Solⁿ Set:

$$\left\{0, \frac{5}{2}, -4\right\}$$

7.7: Ratios and Proportions

7.7.1

Example: A cookie recipe requires 6 cups of flour for 4 dozen cookies. How many cups of flour are needed to make 10 dozen cookies?

$$\frac{6 \text{ cups}}{4 \text{ dozen}} = \frac{?}{10 \text{ dozen}}$$

$$\frac{6 \text{ cups}}{4 \text{ doz}} = \frac{x}{10 \text{ doz}}$$

$$\left(\frac{10 \text{ doz}}{1}\right) \frac{6 \text{ cups}}{4 \text{ doz}} = \frac{x}{10 \text{ doz}} \left(\frac{10 \text{ doz}}{1}\right)$$

$$\frac{60 \text{ cups}}{4} = x$$

$$15 \text{ cups} = x$$

So 15 cups of flour are needed

Tip:

Cross-multiplication

$$\text{If } \frac{a}{b} = \frac{c}{d}, \text{ then } ad = bc.$$

$$\frac{a}{b} = \frac{c}{d}$$

7.7.2

Ex: Solve. $\frac{15}{2} = \frac{7}{4x}$

Cross-multiply: $15(4x) = 7(2)$

$$60x = 14$$

$$\frac{60x}{60} = \frac{14 \div 2}{60 \div 2}$$

$$x = \frac{7}{30}$$

$$\boxed{\left\{ \frac{7}{30} \right\}}$$

Sol'n
Set

Ex: $\frac{y+2}{8} = \frac{2y}{5}$

$$5(y+2) = 2y(8)$$

$$\begin{array}{rcl} 5y + 10 & = & 16y \\ -5y & & -5y \end{array}$$

$$10 = 11y$$

$$\frac{10}{11} = \frac{11y}{11}$$

$$\frac{10}{11} = y$$

$\Rightarrow$

Sol'n Set: $\boxed{\left\{ \frac{10}{11} \right\}}$