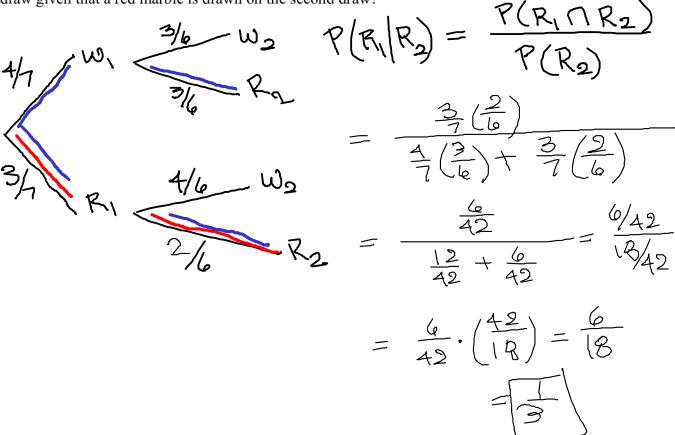
8.4: Bayes' Formula

Previously, when we discussed conditional probabilities, we considered the probability of a "later" event (in a probability tree), given that an "earlier" event occurred.

Now, we will consider the probability of an event "earlier" in the tree, given that a "later" event occurs.

Example 1: A box contains 4 white marbles and 3 red marbles. Two marbles are drawn in succession without replacement. What is the probability of drawing a red marble on the first draw given that a red marble is drawn on the second draw?



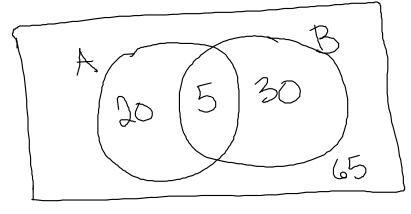
We've just used something a theorem known as *Bayes' Theorem*. You don't need to memorize it, as it is just the conditional probability formula $P(A \mid B) = \frac{P(A \cap B)}{P(B)}$.

Bayes' Formula:

$$P(A \mid B) = \frac{\text{product of probabilities on path to B through A}}{\text{sum of all branch products leading to B}}$$

Example 2: The picture tubes for the Pulsar 19-inch television sets are manufactured in three locations and then shipped to the main plant for final assembly. Plants A, B, and C supply 50%, 30%, and 20%, respectively, of the picture tubes. The quality-control department of the company has determined that 1% of the picture tubes produced by plant A are defective, whereas 2% of the tubes produced by plants B and C are defective. If a Pulsar 19-inch color television is selected at random and the picture tube is found to be defective, what is the probability that the picture tube was manufactured in plant C?

Ex 3' Consider this benn diagram. Assume it represents an equally likely sample space.



Find P()