

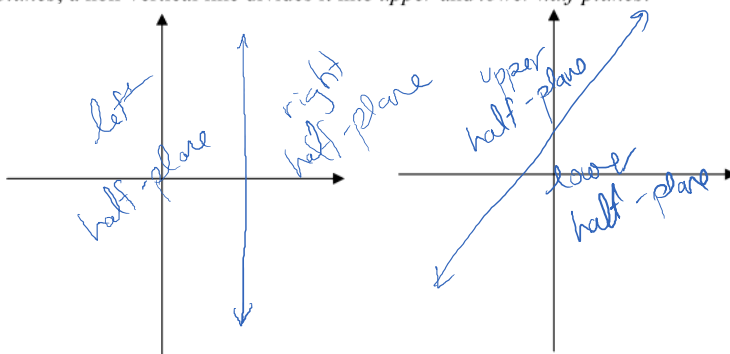
1324-BZBS1
4e-Notes...

5.1.1

5.1: Linear Inequalities in Two Variables

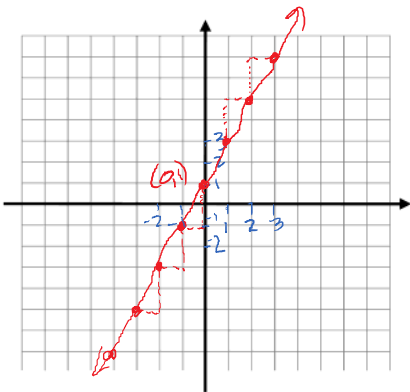
Half-planes:

A line divides the plane into two *half-planes*. A vertical line divides it into *left* and *right half-planes*; a non-vertical line divides it into *upper* and *lower half-planes*.



Graphing linear inequalities:

Example 1: There are four linear inequalities related to the line $y = 2x + 1$.

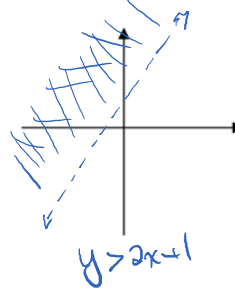
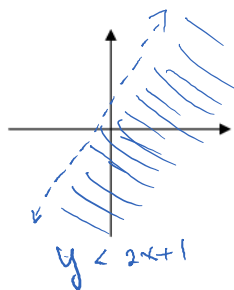
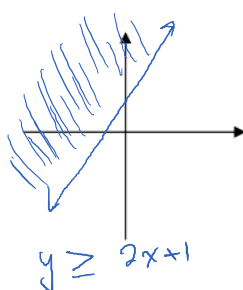
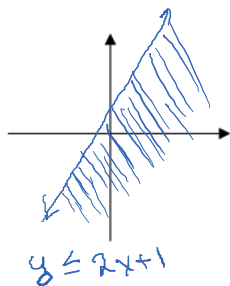


1st graph the line: $y = 2x + 1$

Recall: $y = mx + b$

$m = \text{slope}$
 b or $(0, b)$ is the
y-intercept

Here, slope = $m = \frac{\text{rise}}{\text{run}} = \frac{2}{1}$ \uparrow
y-intercept is 1 or $(0, 1)$



Steps for Graphing a Linear Inequality:

Step 1: First graph the line $Ax + By = C$. Use a solid line if equality is included (\leq or \geq) and a dashed line if equality is not included ($<$ or $>$).

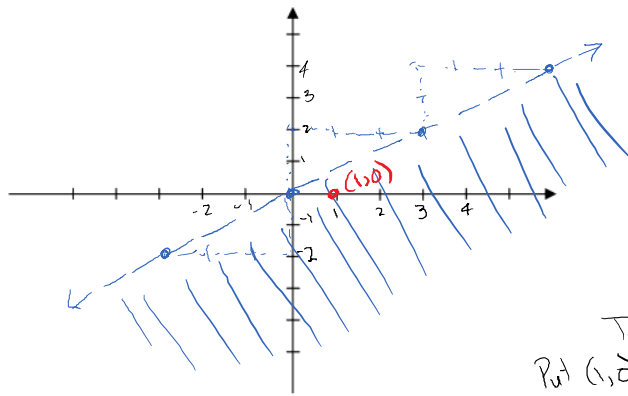
Step 2: Choose a test point not on the line and substitute the coordinates into the inequality. Determine whether this gives a true or a false statement.

Note: The origin $(0,0)$ is usually a good choice, as long as it is not on the line.

Step 3:

- If your test point makes the inequality *true*, shade the half-plane containing the test point.
- If your test point makes the inequality *false*, shade the half-plane not containing the test point.

Example 2: Graph the inequality $2x > 3y$.



1st graph the line: $2x = 3y$
write as $y = mx + b$:

$$3y = 2x$$

$$\frac{3y}{3} = \frac{2x}{3}$$

$$y = \frac{2}{3}x + 0$$

y-int: 0 or $(0,0)$

slope: $m = \frac{2}{3}$

Test point not on line: $(1,0)$

Put $(1,0)$ into $2x > 3y$
 $x=1, y=0 \Rightarrow 2(1) > 3(0)$

$2 > 0$ True.

$(1,0)$ needs to be shaded.
shade the half-plane
that contains $(1,0)$