1342-Notes\_Navidi\_5-2\_addition-complement-rules

Wednesday, October 2, 2019 9:25 AM



5.2.2

**Example 2:** Assume that an equally likely sample space is described by the Venn diagram below.



**Complements:** 

| Probability of a complement: |
|------------------------------|
| $P(E^{C}) = 1 - P(E)$        |
| $P(E) = 1 - P(E^C)$          |

**Example 1:** Suppose that the probability of someone voting for a certain candidate is 0.46. What is the probability of not voting for the candidate?

$$P(A) = 0.46$$
  
 $P(A^{c}) = 1 - 0.46 = 0.54$ 

Table 1. Distribution of Household Money Income by Selected Income Class, 2012 # of Households (in thousands) Income Class % of Households All Households 122,459 100.0 Less than \$5,000 4,204 3.4 \$5,000 to \$9,999 4,729 3.9 \$10,000 to \$14,999 6,982 5.7 \$15,000 to \$19,999 7,157 5.8 \$20,000 to \$24,999 7,131 5.5 \$25,000 to \$29,999 6,740 5.4 \$30,000 to \$34,999 6.354 5.2 \$35,000 to \$39,999 5,832 4.8 \$40,000 to \$44,999 5,547 4.5 \$45,000 to \$49,999 5,254 4,4 \$50,000 to \$59,999 9,358 7.6 \$60,000 to \$69,999 8,305 6.8 \$70,000 to \$79,999 7,170 5.9 \$80,000 to \$89,999 5,969 4.9 \$90,000 to \$99,999 4,901 4.0 \$100,000 to \$124,999 9,490 7.7 \$125,000 to \$149,999 5,759 4.7 \$150,000 to \$199,999 6,116 5.0 \$200,000 to \$249,999 2.1 2,549 \$250,000 and above 2,911 2.4

## Example 2: Consider the data below, from the Congressional Research Service. https://fas.org/sgp/crs/misc/RS20811.pdf

Source: U.S. Census Bureau, 2012 Annual Social and Economic Supplement to the Current Population Survey.

\$51.017 \$71.274

Median Income

Mean Income

a) What is the probability that a randomly selected household has an income of \$100,000 or more?

b) What is the probability that a randomly selected household has an income below \$40,000?

c) What is the probability that a randomly selected household has an income below \$40,000?

5.2.4

d) What is the probability that a randomly selected household has an income below \$250,000?

e) What is the probability that a randomly selected household has an income of \$20,000 or more?

f) Approximate the median household income.

| <b>A</b> | * |   | 2  | ÷ |    | 3                   | *        |           | 4 <b>*</b> | *        | 5. | *  | 6. <b>*</b> | *          | 7. <b>*</b> | *          | 8. <b>.</b> | *        | 9.4                | *   | <sup>₽</sup> | **   | J           |     | K NA |
|----------|---|---|----|---|----|---------------------|----------|-----------|------------|----------|----|----|-------------|------------|-------------|------------|-------------|----------|--------------------|-----|--------------|------|-------------|-----|------|
| 2        | 8 | ŧ |    | Ŷ | 5  |                     | ÷        | •0        | Ť          | **       | ÷  | Ťġ | *           | *          | *           | *          | *           | *        | +                  | *   |              | ÷.   | M.          | -45 |      |
| A •      | • |   | \$ | ٠ |    | 3.                  | •        |           | 4.♦        | •        | 5. | •  | 6 <b>♦</b>  | •          | ₹.<br>•     | •          | 8. <b>♦</b> |          | 9.4                |     |              | •    |             |     |      |
| A        |   | • | 2  | + | \$ | 3                   | +        | \$        | <b>♦</b>   | **       | •  | ♦ţ | <b>ب</b>    | <b>*</b> g | *<br>7.     | +1         | 8.          | +        | ¢                  | •   |              | • di |             | 9   |      |
|          | • | • |    |   | -  |                     | *        |           |            | *        |    | •  |             | •          | •           | ••         |             |          | *                  | **  |              |      |             |     |      |
| A<br>•   | ٠ |   | 2  | ٨ |    | 3.                  | <b>^</b> | -         | 4♠         | ٠        | 5  | *  | 6. <b>.</b> | <u>ب</u>   | 7. <b>.</b> | **         | **          | <b>^</b> | 9. <b>4</b><br>• • | *** |              | ***  |             | •   | K    |
| _        |   | ¥ | 2  | ۴ | S. | and the             | *        | +01 -11-1 | ۴          | <b>♥</b> | ¥  | ¢ţ | *           | <b>♥</b>   | *           | ¥ <u>*</u> | •           | ¥8       | Į į                | ¥;  |              | ¥ å  | <u>i La</u> |     |      |
|          |   |   |    |   |    | and a second second |          |           |            |          |    |    |             |            |             |            |             |          |                    |     |              |      |             |     |      |

**Example 3:** Consider a standard deck of 52 cards.

a) What is the probability that a randomly selected card is a spade or a heart?

b) What is the probability that a randomly selected card is a spade or an ace?

c) What is the probability that a randomly selected card is not a black face card?