Name\_

Date

Solve the equation.

1) 
$$(y - 4) - (y + 5) = 5y$$

2) 
$$13(8c - 7) = 8c - 9$$

3) 
$$3(2z - 4) = 5(z + 5)$$

4) 
$$2x + 3(-2x - 5) = -16 - 3x$$

5) 
$$\frac{2x}{5} - \frac{x}{3} = 2$$

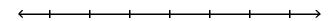
6) 
$$\frac{17}{14}x + \frac{2}{7} = \frac{8}{7}x$$

7) 
$$\frac{4(7-x)}{3} = x$$

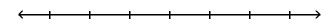
8) 
$$\frac{3(y-2)}{5} = 1 - 3y$$

Solve the inequality. Graph the solution set and write it in interval notation.

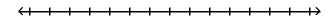
9)  $-24x + 8 \le -4(5x - 11)$ 



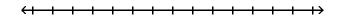
10)  $25x + 5 \le 5(4x + 5)$ 



11)  $-32 \le -5x + 3 \le -12$ 



12)  $4 \le 2(x - 5) \le 8$ 



Solve.

13) The owners of a candy store want to sell, for \$6 per pound, a mixture of chocolate-covered raisins, which usually sells for \$3 per pound, and chocolate-covered macadamia nuts, which usually sells for \$8 per pound. They have a 40-pound barrel of the raisins. How many pounds of the nuts should they mix with the barrel of raisins so that they hit their target value of \$6 per pound for the mixture?

- 14) A chemist needs 100 milliliters of a 67% solution but has only 55% and 85% solutions available. Find how many milliliters of each that should be mixed to get the desired solution.
- 15) How can \$56,000 be invested, part at 4% annual simple interest and the remainder at 10% annual simple interest, so that the interest earned by the two accounts is equal at the end of the year?
- 16) Melissa invested a sum of money at 3% annual simple interest. She invested three times that sum at 5% annual simple interest. If her total yearly interest from both investments was \$3600, how much was invested at 3%?
- 17) Linda and Dave leave simultaneously from the same starting point biking in opposite directions. Linda bikes at 5 miles per hour and Dave bikes at 9 miles per hour. How long will it be until they are 23 miles apart from each other?
- 18) Jeff starts driving at 55 miles per hour from the same point that Lauren starts driving at 50 miles per hour. They drive in opposite directions, and Lauren has a half-hour head start. How long will they be able to talk on their cell phones that have a 400-mile range?
- 19) Eight less than three times a number is less than ten. Find all such numbers.
- 20) Three-fourths a number decreased by one is between negative five and sixteen. Find all such numbers.

Determine whether the equation is a linear equation in two variables.

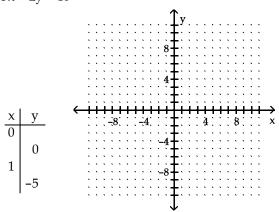
- 21) x = 3
- 22)  $3x^2 = 7y 6$

Complete the ordered pair so that it is a solution of the given linear equation.

23) 
$$8x + y = -52$$
;  $(-7, ), (0, ), (1, )$ 

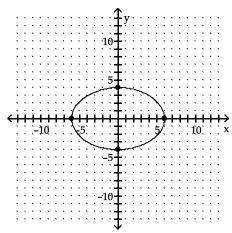
Complete the table of ordered pairs for the given linear equation; then plot the solution.

24) 
$$5x + 2y = 10$$

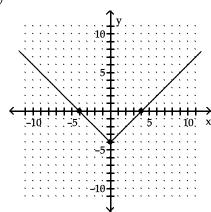


Identify the intercepts.

25)

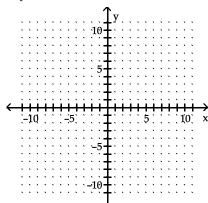


26)

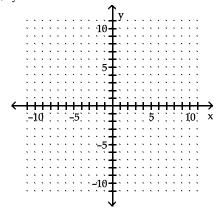


Graph the linear equation by finding x- and y- intercepts.

27) 
$$15y - 5x = -10$$

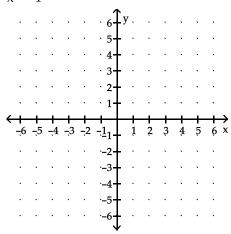


28) y = 5x

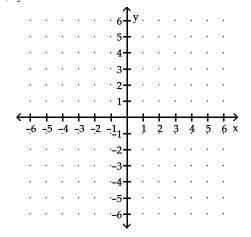


Graph the linear equation.

29) x = -4

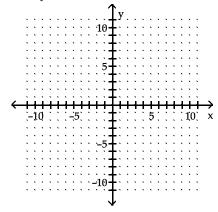


30) y - 2 = 0

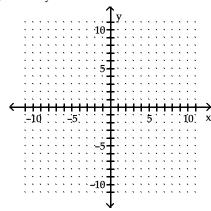


Use the slope-intercept form to graph the equation.

31) 
$$6x + y = 0$$



32) 
$$2x + 5y = 10$$



Evaluate the expression with the given replacement values.

33) 
$$-3x^3y$$
;  $x = 2$  and  $y = -5$ 

34) 
$$\frac{8}{3x^2}$$
;  $x = -3$ 

Use the product rule to simplify. Write the results using exponents.

35) 
$$g^9 \cdot g^5 \cdot g^8$$

36) 
$$(7x)(4x^5)(x^3)$$

Use the quotient rule to simplify the expression.

$$37) \ \frac{40m^{16}n^9}{5m^{15}n^7}$$

Simplify the following.

38) 
$$-8y^0$$

Simplify the expression. Write the result using positive exponents only.

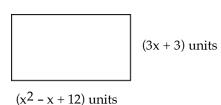
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39) 
$$\frac{(4x^2)^3}{x^{15}}$$

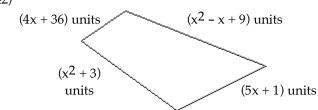
40) 
$$(-5x^3y^{-4})(3x^{-1}y)$$

Find the perimeter.

41)



42)



Perform the indicated operations.

43) 
$$(6x^5 + 2x^4 - 7x^3 + 6) - (4x^5 - 4x^4 - 5x^3 - 5)$$

44) 
$$(-7x^4 + 9x^6 - 8 + 9x^5) - (-5 + 5x^5 + 2x^6 + 9x^4)$$

Find the following product.

45) 
$$(3z + 11)^2$$

46) 
$$(x + 1)(x^2 - x + 1)$$

Perform the division.

47) 
$$\frac{x^2 + 7x + 3}{x + 5}$$

48) 
$$\frac{8x^3 - 28x^2 + 14x + 19}{2x - 5}$$

Factor out the GCF from the polynomial.

50) 
$$21x^3y + 15xy^6$$

Factor by grouping.

51) 
$$xy + 11x - 5y - 55$$

52) 
$$4xy - 16x + 7y - 28$$

Factor the polynomial completely. If the polynomial cannot be factored, write prime.

53) 
$$x^3 - x^2 - 30x$$

54) 
$$5x^6 + 60x^5 + 175x^4$$

55) 
$$x^2 - 16xy + 64y^2$$

56) 
$$64x^2 + 80xy + 25y^2$$

57) 
$$r^{20} - a^2$$

58) 
$$x^4 - 625$$

59) 
$$t^3 + 1000$$

60) 
$$750x^3 - 162x^6$$

Solve the equation.

61) 
$$(5y + 29)(2y + 11) = 0$$

62) 
$$b(b + 18) = 0$$

63) 
$$49x^2 - 3 = 14x$$

64) 
$$(x + 8)(x + 1) = 44$$

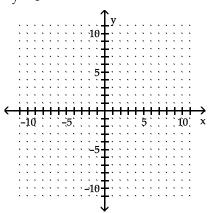
Without graphing, determine whether the system has one solution, no solution, or an infinite number of solutions.

 $\int 2x + y = 2$ 

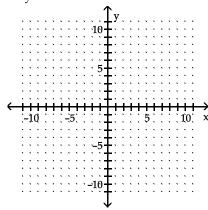
66) 
$$\begin{cases} x + 6y = 24 \\ y = -\frac{1}{6}x + 4 \end{cases}$$

Solve the system of equations by graphing the equations on the same set of axes.

67) 
$$\begin{cases} x + y = 1 \\ x - y = 5 \end{cases}$$



$$\begin{cases} x + 2y = 5 \\ 3x - 2y = -9 \end{cases}$$



Solve the system of equations by the substitution method.

69) 
$$\begin{cases} 3x + y = 15 \\ 12x + 4y = 60 \end{cases}$$

70) 
$$\begin{cases} -5x - 20y = 10 \\ 6x + 24y = 0 \end{cases}$$

Solve the system of equations by the addition method.

71) 
$$\begin{cases} 3x - 5y = 7 \\ 6x - 10y = 28 \end{cases}$$

72) 
$$\begin{cases} -6x - 6y = -4 \\ 12x + 12y = 8 \end{cases}$$

Simplify the rational expression.

73) 
$$\frac{2x-8}{12-3x}$$

74) 
$$\frac{4-x}{6x-24}$$

Perform the indicated operation. Simplify if possible. 75) 
$$\frac{2x}{x^2 - 7x + 12} - \frac{8}{x^2 - 7x + 12}$$

76) 
$$\frac{10x+3}{x^2+10x+16} - \frac{9x-5}{x^2+10x+16}$$

Divide. Simplify if possible.

77) 
$$\frac{x-1}{-7-x} \div \frac{x^2-4x-5}{x^2+8x+7}$$

78) 
$$(x+2) \div \frac{x^2 - 10x + 16}{8 - x}$$

Find all numbers for which the rational function is defined.

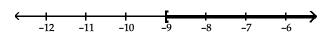
79) 
$$f(w) = \frac{w^2 - 25w}{5w}$$

80) 
$$f(x) = \frac{2x}{-3 + x}$$

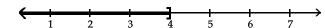
# Answer Key

### Testname: DEPARTMENTAL FINAL REVIEW 0308

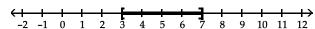
- 1)  $-\frac{9}{5}$
- 2)  $\frac{41}{48}$
- 3) 37
- 4) 1
- 5) 30
- 6) -4
- 7) 4
- 8)  $\frac{11}{18}$
- 9) [-9, ∞)



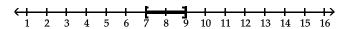
10)  $(-\infty, 4]$ 



11) [3,7]

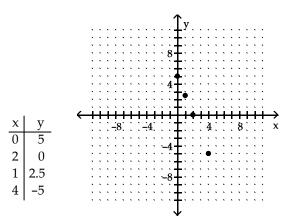


12) [7,9]

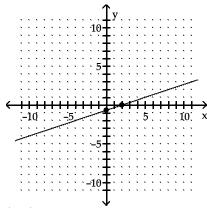


- 13) 60 lbs
- 14) 60 ml of 55%; 40 ml of 85%
- 15) \$40,000 invested at 4%; \$16,000 invested at 10%
- 16) \$20,000
- 17)  $1\frac{9}{14}$  hrs
- 18)  $3\frac{4}{7}$  hrs
- 19) x < 6
- $20) \frac{16}{3} < x < \frac{68}{3}$
- 21) yes
- 22) no
- 23) (-7, 4) (0, -52) (1, -60)

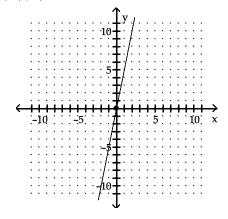
24)

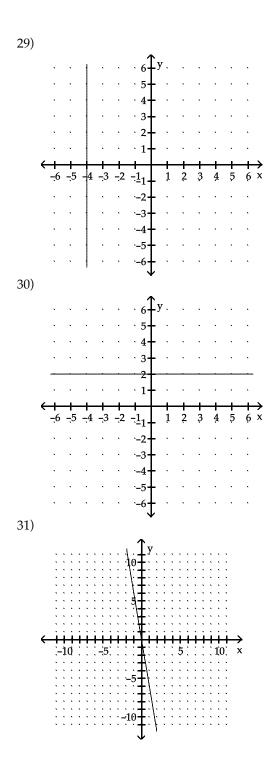


- 25) (6, 0), (-6, 0), (0, 4), (0, -4) 26) (4, 0), (-4, 0), (0, -4)
- 27)  $(0, -\frac{2}{3}), (2, 0)$



28) (0, 0)

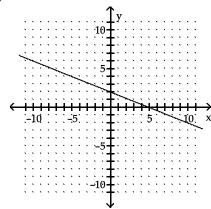




## Answer Key

#### Testname: DEPARTMENTAL FINAL REVIEW 0308





- 33) 120
- 34)  $\frac{8}{27}$
- 35) g<sup>22</sup>
- 36) 28x<sup>9</sup>
- 37) 8mn<sup>2</sup>
- 38) -8
- 39)  $\frac{64}{x^9}$

40) 
$$\frac{-15x^2}{y^3}$$

- 41)  $(2x^2 + 4x + 30)$  units
- 42)  $(2x^2 + 8x + 49)$  units
- 43)  $2x^5 + 6x^4 2x^3 + 11$
- 44)  $7x^6 + 4x^5 16x^4 3$
- 45)  $9z^2 + 66z + 121$
- 46)  $x^3 + 1$
- 47)  $x + 2 \frac{7}{x+5}$

48) 
$$4x^2 - 4x - 3 + \frac{4}{2x - 5}$$

- 49) 8(6x 1)
- 50)  $3xy(7x^2 + 5y^5)$
- 51) (y + 11)(x 5)
- 52) (4x + 7)(y 4)
- 53) x(x+5)(x-6)
- 54)  $5x^4(x+7)(x+5)$
- 55)  $(x 8y)^2$
- 56)  $(8x + 5y)^2$
- 57)  $(r^{10} + a)(r^{10} a)$
- 58)  $(x^2 + 25)(x + 5)(x 5)$
- 59)  $(t + 10)(t^2 10t + 100)$

# Answer Key

### Testname: DEPARTMENTAL FINAL REVIEW 0308

60) 
$$6x^3(5-3x)(25+15x+9x^2)$$

61) 
$$y = -\frac{29}{5}$$
,  $y = -\frac{11}{2}$ 

62) 
$$b = -18$$
,  $b = 0$ 

63) 
$$x = \frac{3}{7}, x = -\frac{1}{7}$$

64) 
$$x = -12$$
,  $x = 3$ 

73) 
$$-\frac{2}{3}$$

74) 
$$-\frac{1}{6}$$

75) 
$$\frac{2}{x-3}$$

76) 
$$\frac{1}{x+2}$$

77) 
$$-\frac{x-1}{x-5}$$

78) 
$$-\frac{x+2}{x-2}$$

79) 
$$\{w \mid w \text{ is a real number and } w \neq 0\}$$

80) 
$$\{x \mid x \text{ is a real number and } x \neq 3\}$$