

### Logarithmic Functions:

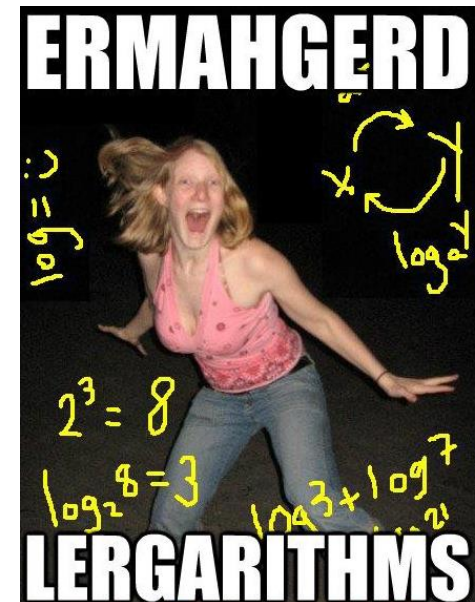
A function of the form  $f(x) = \log_b x$  with  $b > 0$  and  $b \neq 1$  is called a logarithmic function with base  $b$ . It is the inverse of the exponential function  $b^x$ , so we can get the graph of a logarithmic function by reflecting the graph of the corresponding exponential function about the line  $y = x$ .

Just like the exponential functions, the bases separate into two categories:

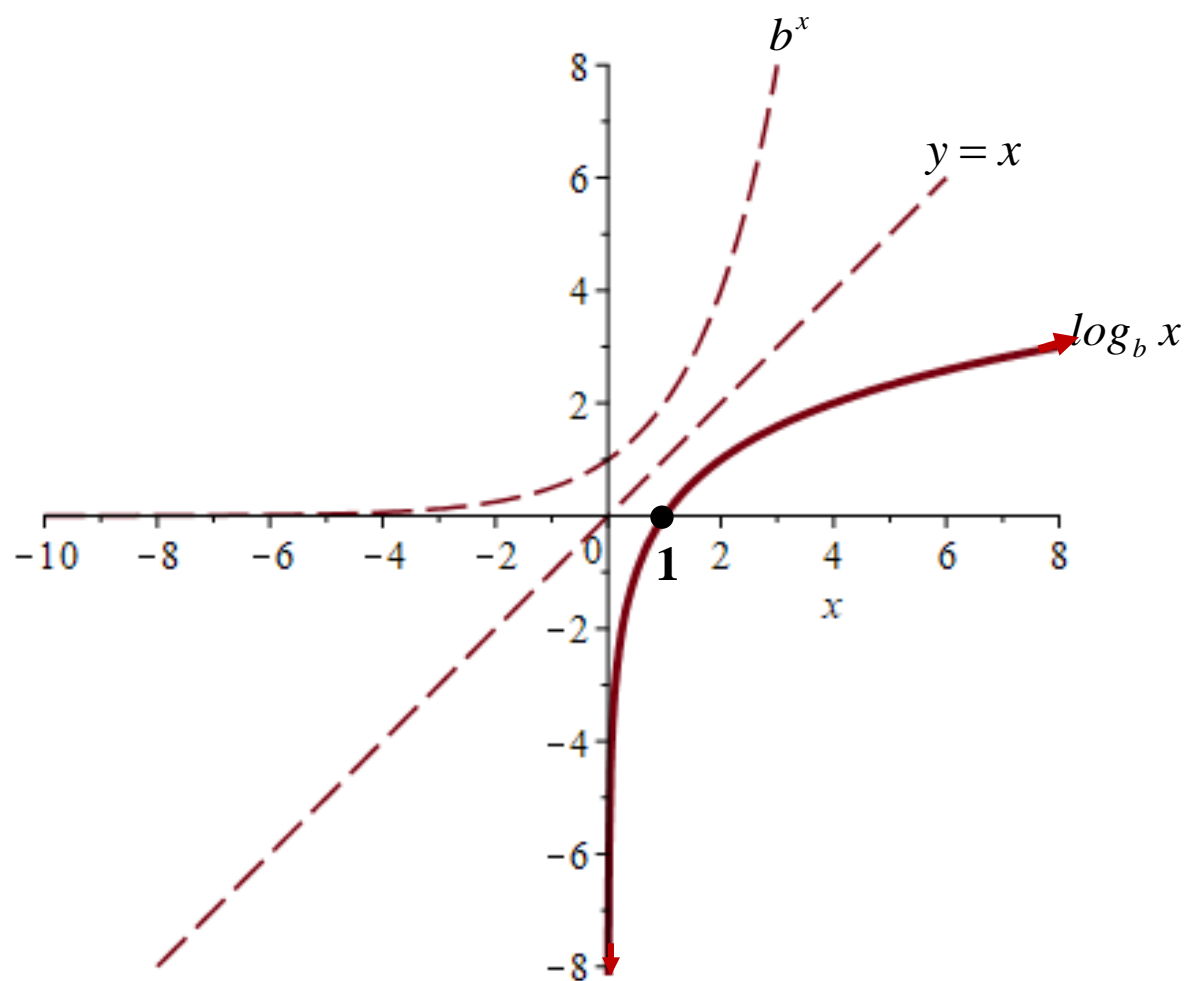
$$b > 1$$

And

$$0 < b < 1$$



For  $b > 1$ ,



Domain:  $(0, \infty)$

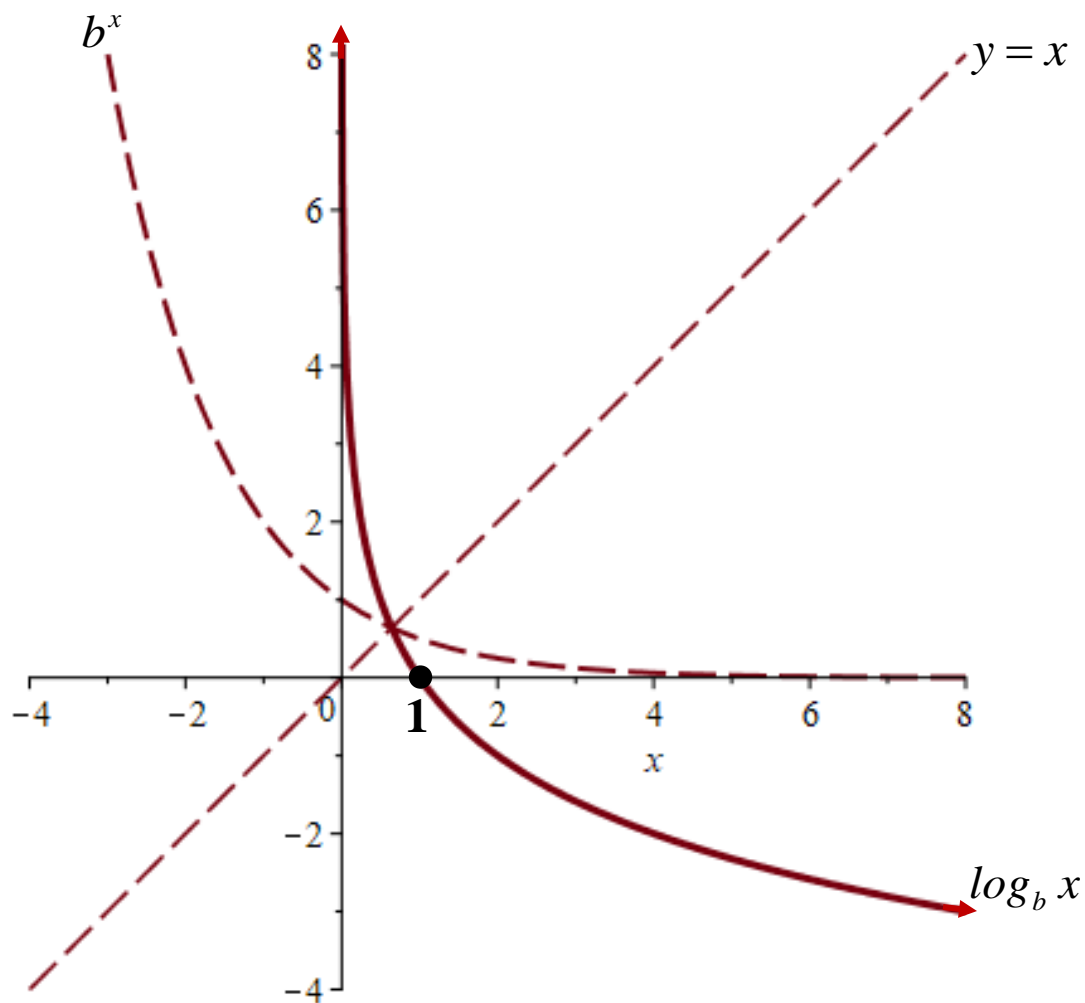
Range:  $(-\infty, \infty)$

Vertical Asymptote:  $x = 0$  from the right

Increasing:  $(0, \infty)$



**For  $0 < b < 1$ ,**



**Domain:**  $(0, \infty)$

**Range:**  $(-\infty, \infty)$

**Vertical Asymptote:**  $x = 0$  from the right

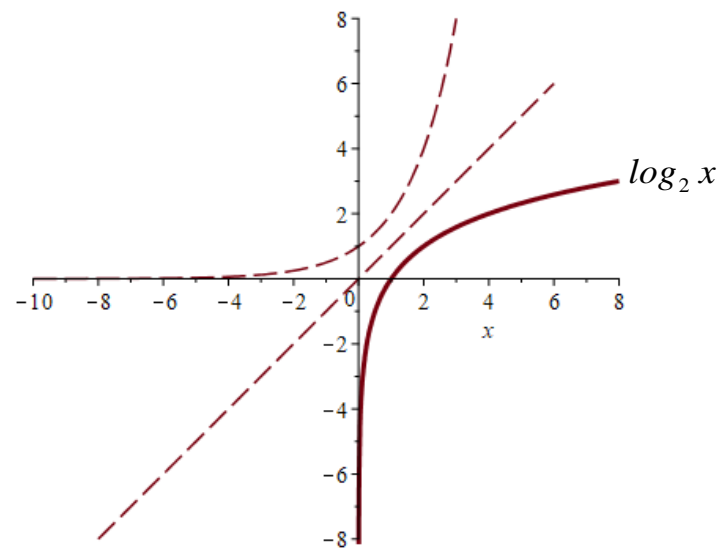
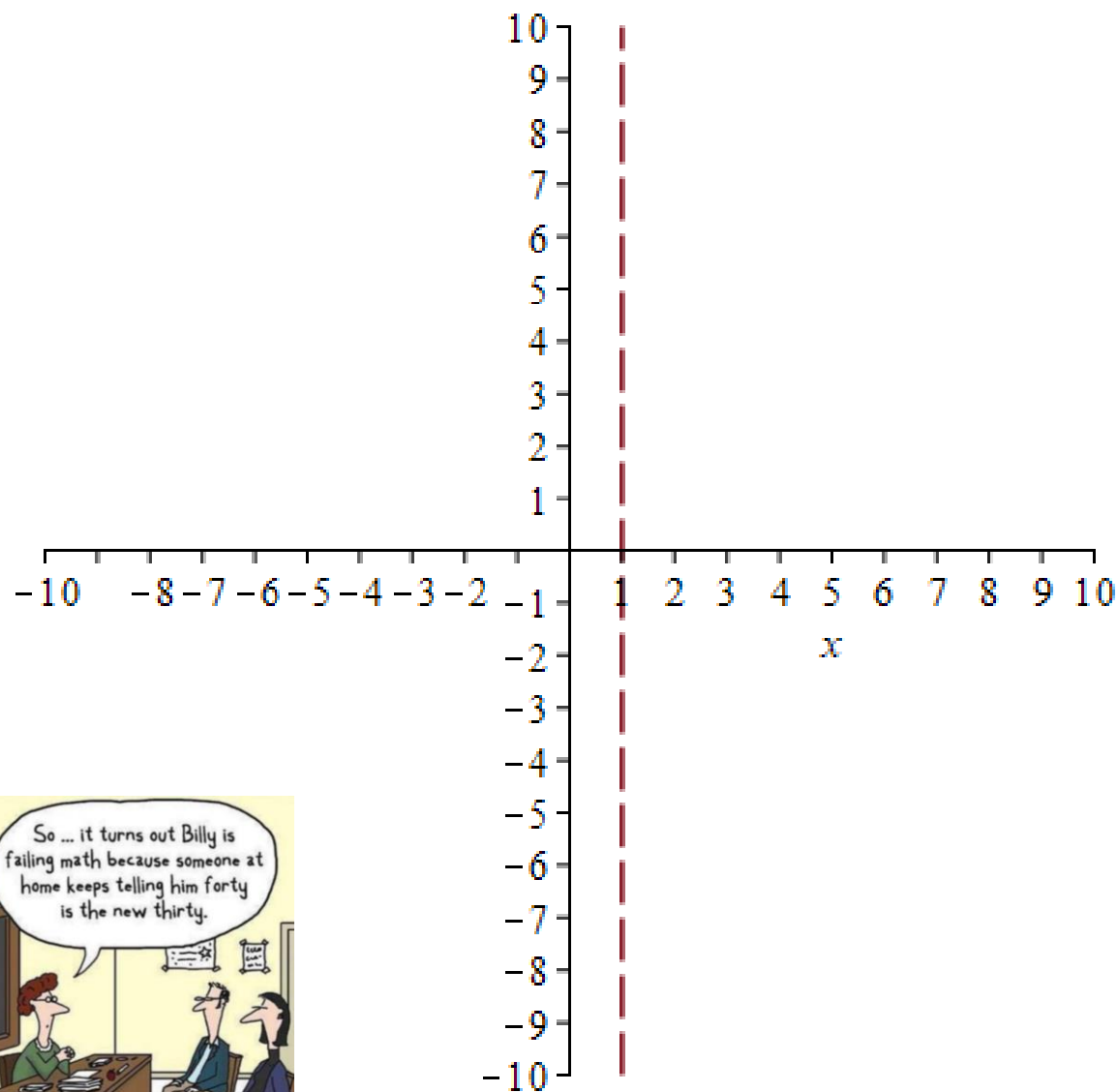
**Decreasing:**  $(0, \infty)$

Me Trying To Figure Out Why My Friend  
Asked Me For Logarithm Table on English Exam



## Transformations of Logarithmic Functions:

1.  $f(x) = \log_2(x-1)$

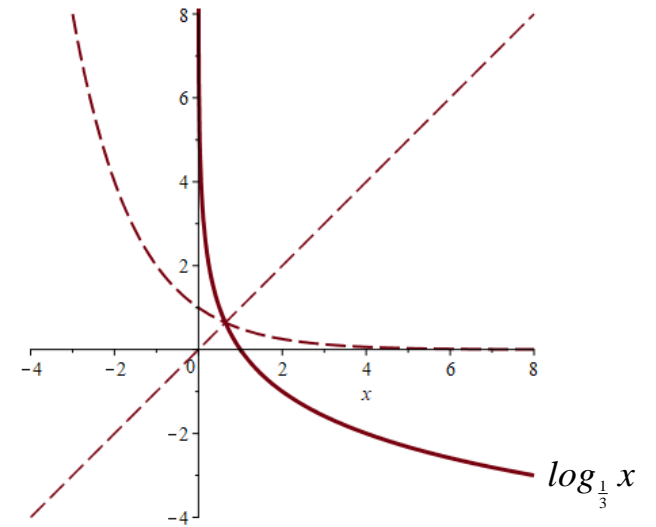
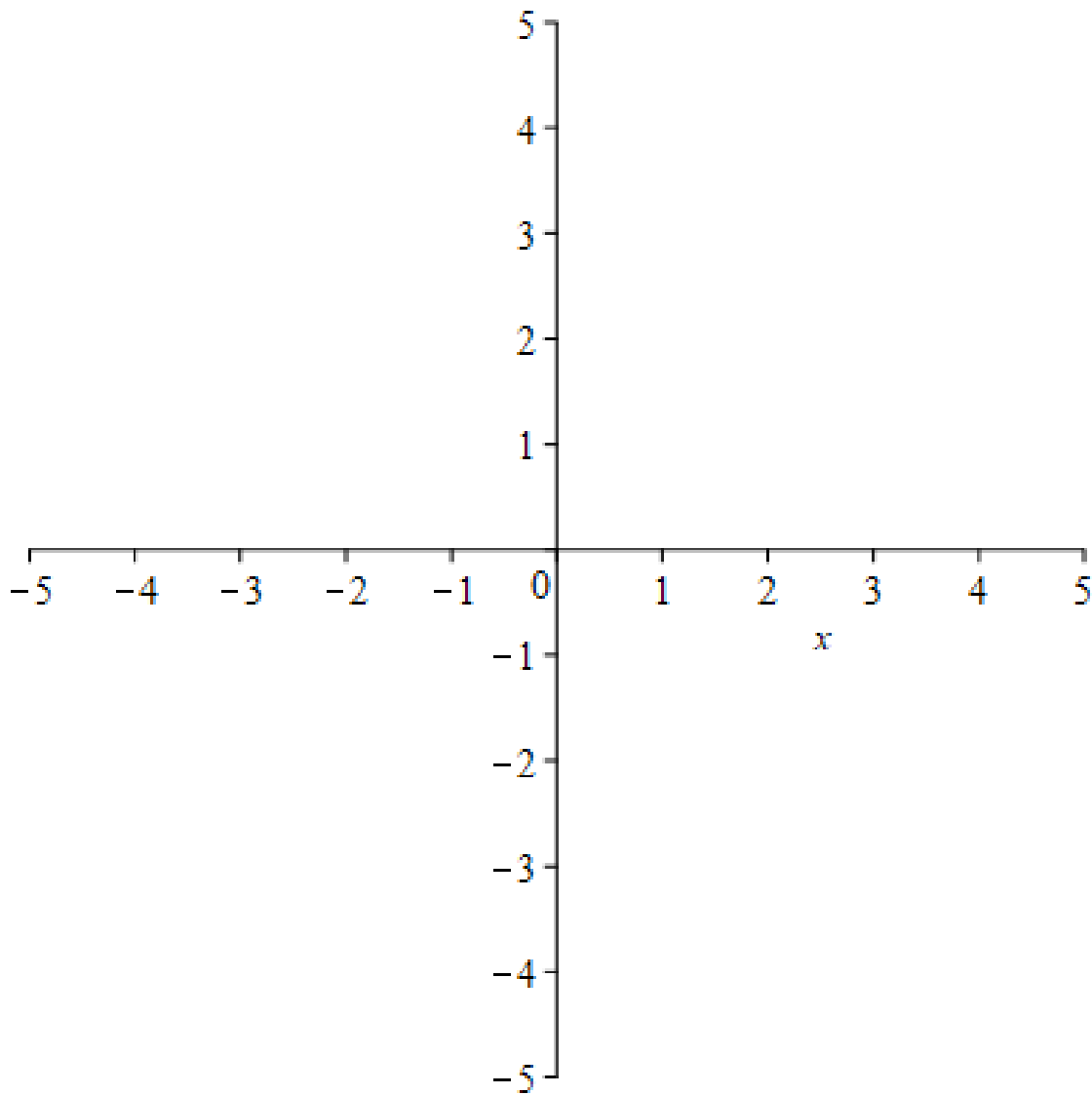


**Domain:**

**Range:**

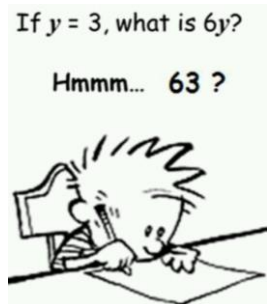


$$2. f(x) = \log_{\frac{1}{3}}(-x)$$

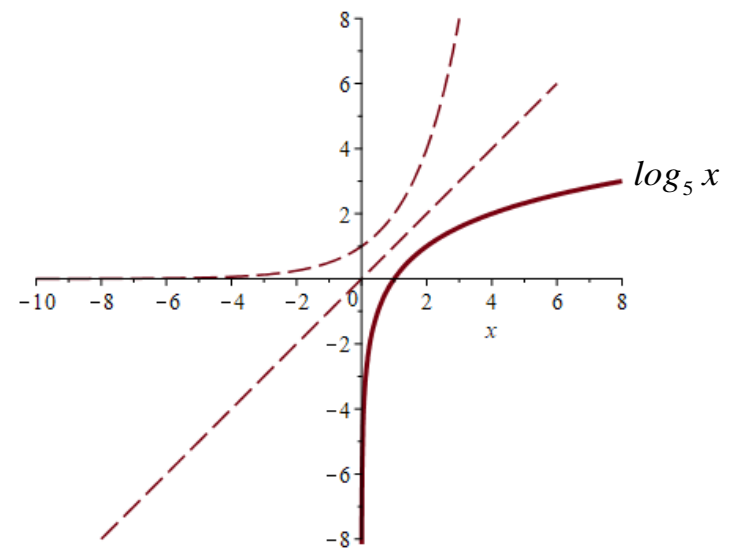
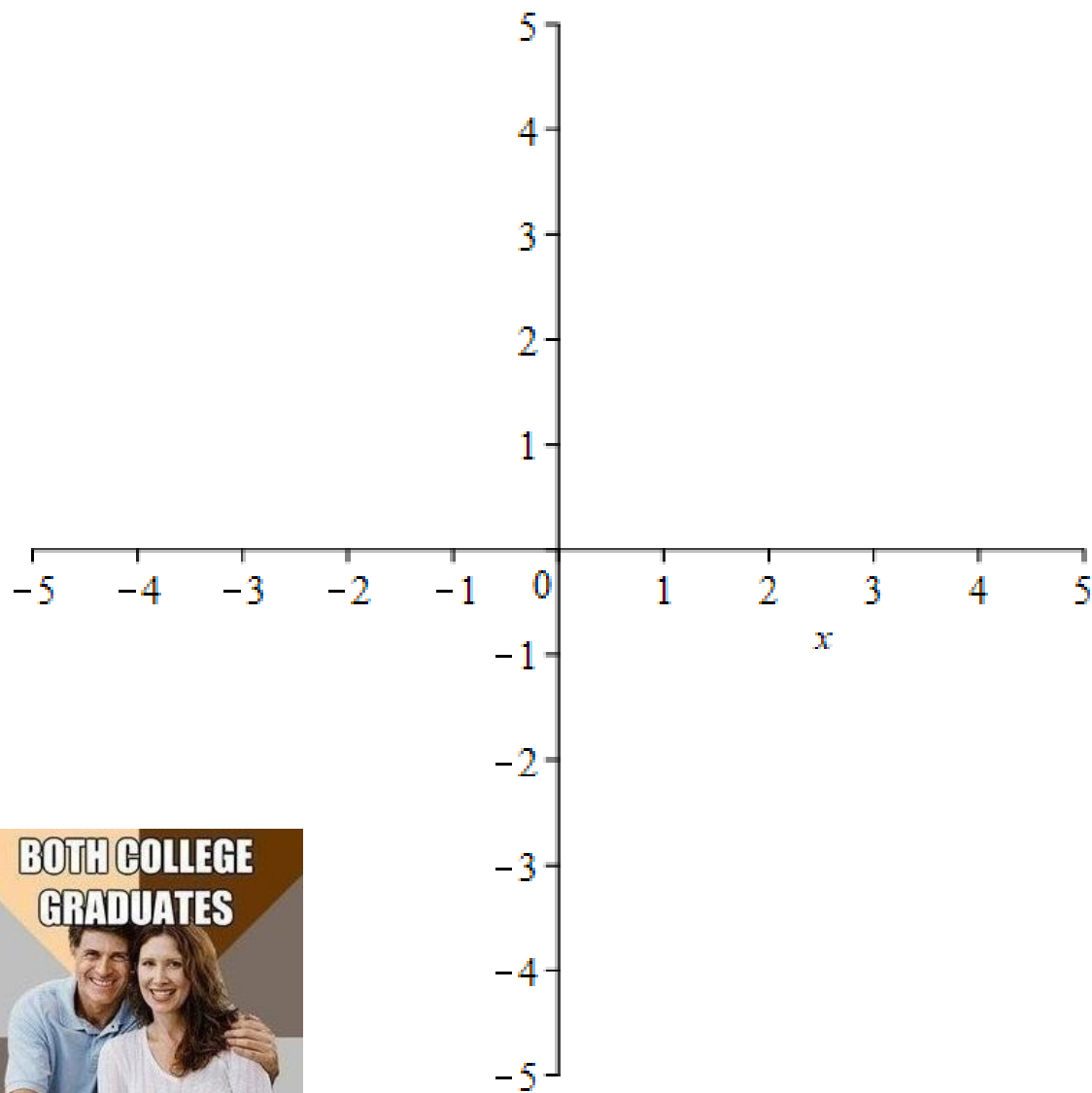


**Domain:**

**Range:**



3.  $f(x) = \log_5 x + 1$

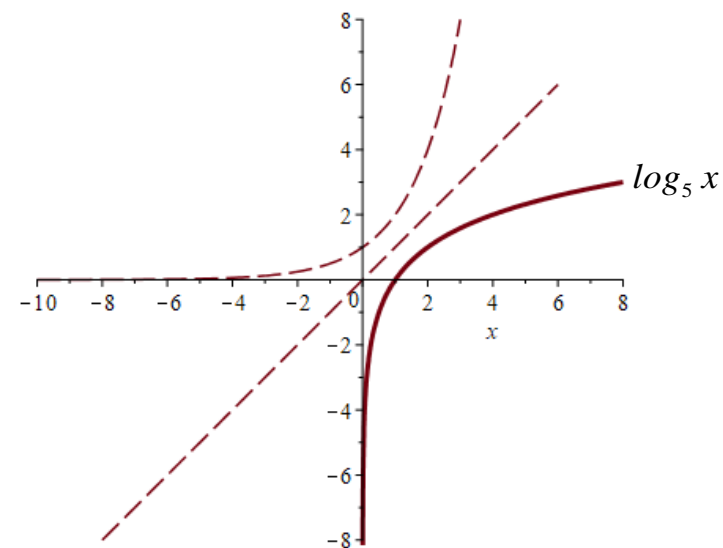
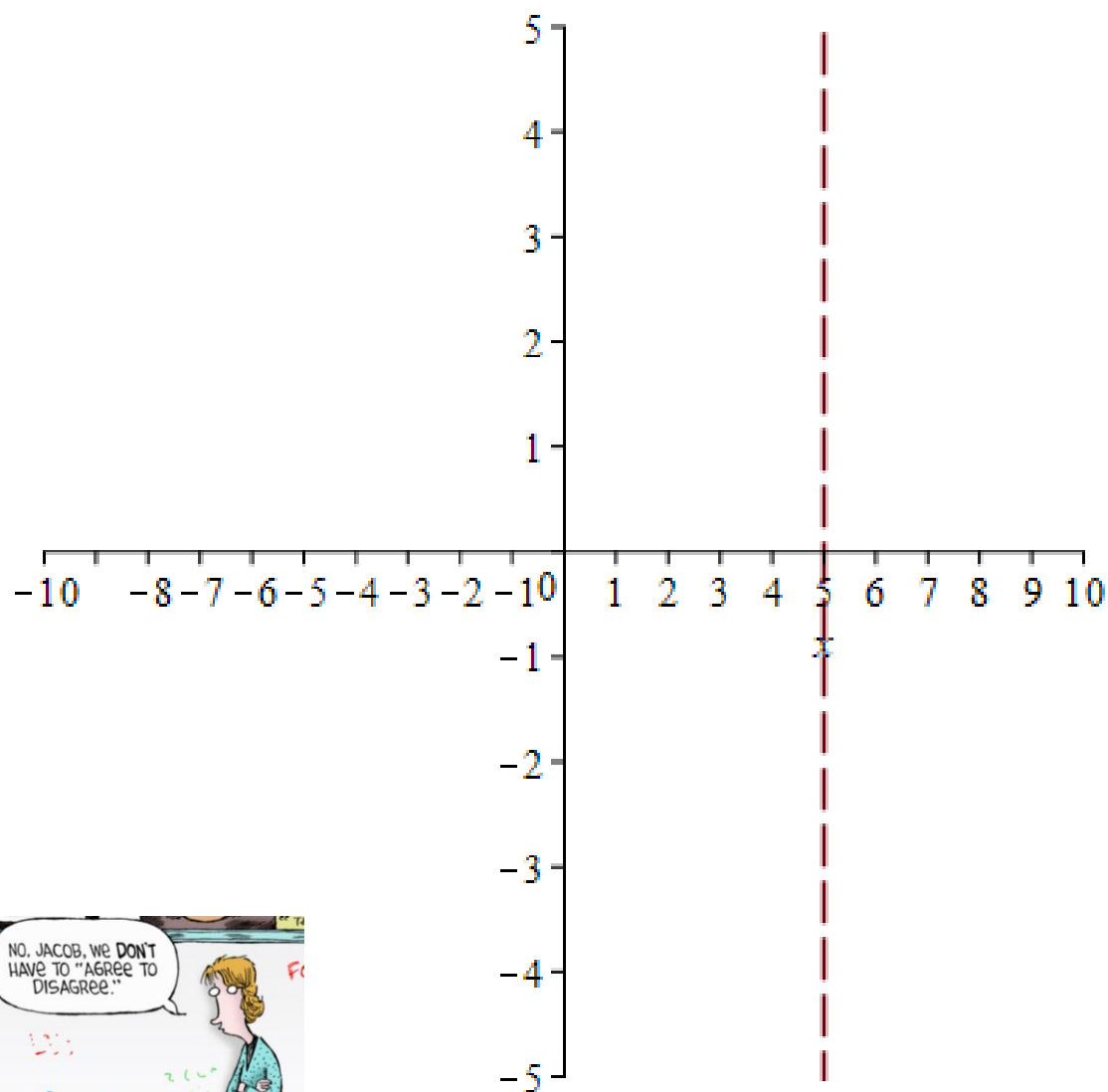


**Domain:**

**Range:**

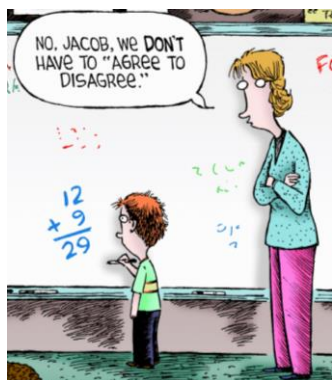


4.  $f(x) = \log_5(5-x)$



**Domain:**

**Range:**



**Logarithms are actually exponents.  $\log_b x$  is the power or exponent that you raise  $b$  to in order to get  $x$ .**

**1.  $\log_8 8$**

**2.  $\log_3 9$**

**3.  $\log_2 \frac{1}{4}$**

**4.  $\log_{\frac{1}{2}} 8$**

**5.  $\log_6 \sqrt{6}$**

**6.  $\log_5 \sqrt[3]{25}$**

**7.  $\log_{\sqrt{3}} 9$**





## Logarithmic and Exponential Form of Equations:

### Logarithmic Form:

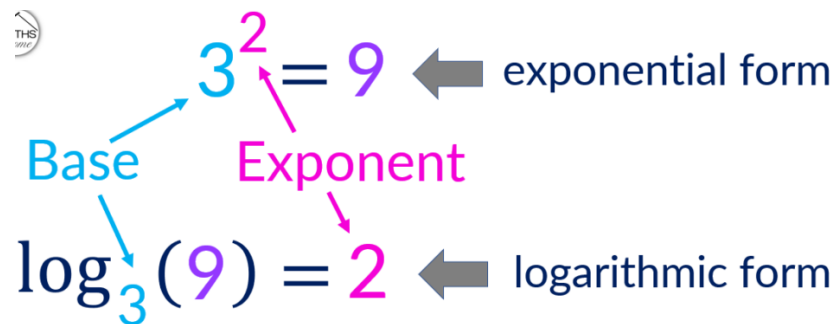
$$3 = \log_{10} 1,000$$

Exponentiate to get the exponential form.

### Exponential Form:

$$3^4 = 81$$

Apply a logarithmic function to get the logarithmic form.



**An Important Logarithmic Property:**

$$\log_b(b^x) = x; \text{ for all } x$$

$$b^{\log_b x} = x; \text{ for } x > 0$$

**Solve the following logarithmic equations:**

**1.**  $\log_5 x = 2$

**2.**  $\log_3(3x - 2) = 3$

**Inverse  
property  
of  
logarithms**

$$\log_b b^x = x$$
$$b^{\log_b x} = x$$

3.  $\log_x 4 = 2$

4.  $\log_4 64 = x$



"First you forget logarithms. Then you forget how to do long division. Then the multiplication table begins to go . . ."

5.  $\log_3(x^2 + 1) = 2$

6.  $\log_5(x^2 + 4x + 4) = 2$