

### *Descriptive Statistics:*

Describes, organizes, and presents data(information) about populations and samples.



### *Inferential Statistics:*

Draws conclusions about populations based upon samples.



*This class focuses on descriptive statistics!*

### **Frequency Distribution:**

A table that lists all the values of a data set along with their respective frequencies.

**Data Set:** {11,12,12,11,15,14,13,12,11,11}

<b>Value</b>	<b>Frequency</b>
<b>11</b>	<b>4</b>
<b>12</b>	
<b>13</b>	
<b>14</b>	
<b>15</b>	
<b>Total</b>	

### **Relative Frequency Distribution:**

A table that lists all the values of a data set along with their respective relative frequencies.

<b>Value</b>	<b>Frequency</b>	<b>Relative Frequency</b>	<b>Percent Frequency</b>
11	4	$\frac{4}{10} = .4$	40%
12	3		
13	1		
14	1		
15	1		
<b>Total</b>	<b>10</b>	<b>1</b>	<b>100%</b>

### **Grouped Frequency Distribution:**

Disjoint classes(ranges) are established for the data values. The grouped frequency distribution lists all the classes along with their respective frequencies.

**Data Set:** {10,21,22,12,50,42,33,20,15,17}

<b>Class</b>	<b>Frequency</b>
<b>10-19</b>	<b>4</b>
<b>20-29</b>	
<b>30-39</b>	
<b>40-49</b>	
<b>50-59</b>	
<b>Total</b>	

**There is a loss of detail in a grouped frequency distribution-the actual data values are lost!**

*Example:*

Class	Frequency
10-19	6
20-29	8
30-39	4
40-49	5
50-59	2
Total	25

**How many values in the data set are less than 20?**

**How many values in the data set are less than 25?**

**How many values in the data set are greater than 39?**

**How many values in the data set are greater than 50?**

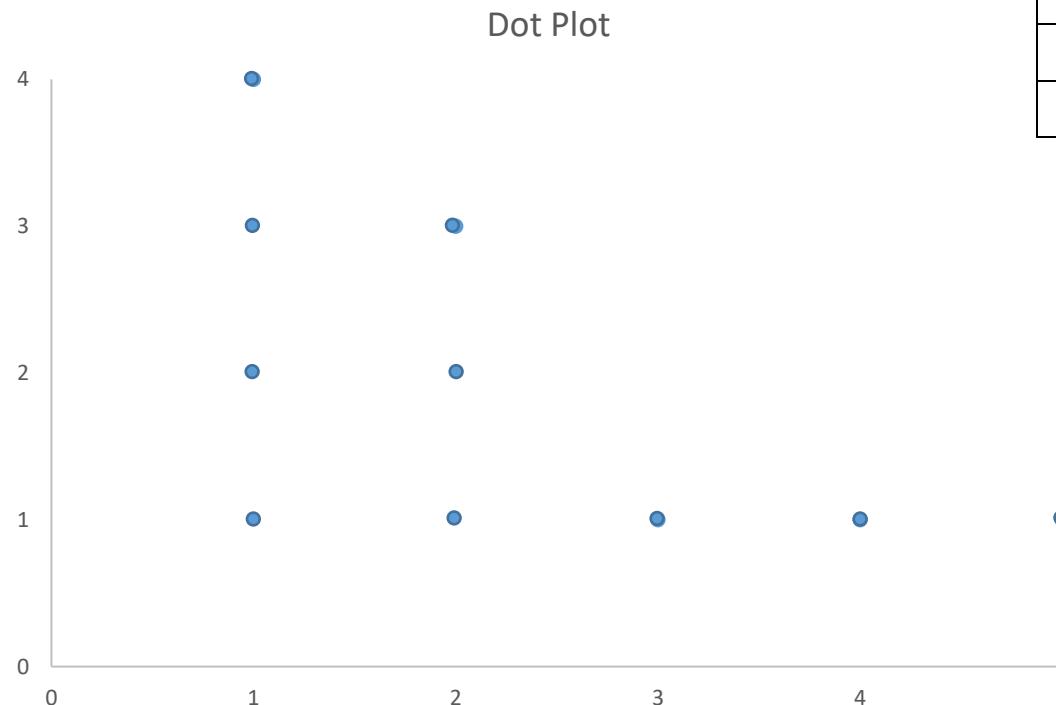
## Graphs of frequency distributions:

### Dot Plot:

The number of vertical dots corresponds to the frequency.

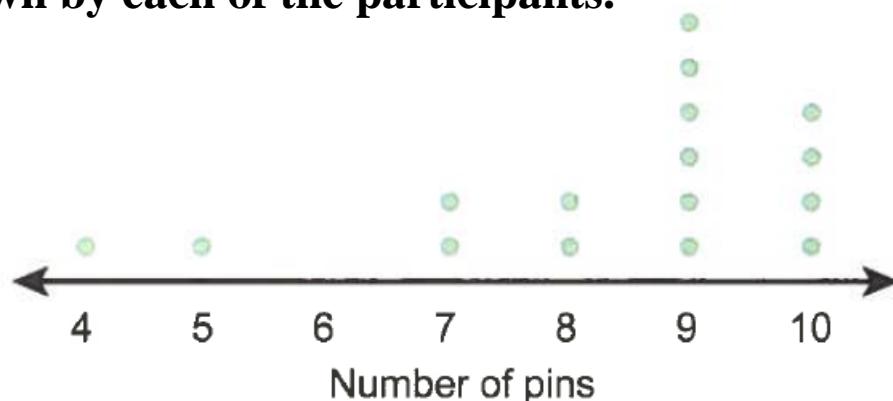


Value	Frequency
1	4
2	3
3	1
4	1
5	1
<b>Total</b>	<b>10</b>



Allows easy visual determination of the most and least frequently occurring values!

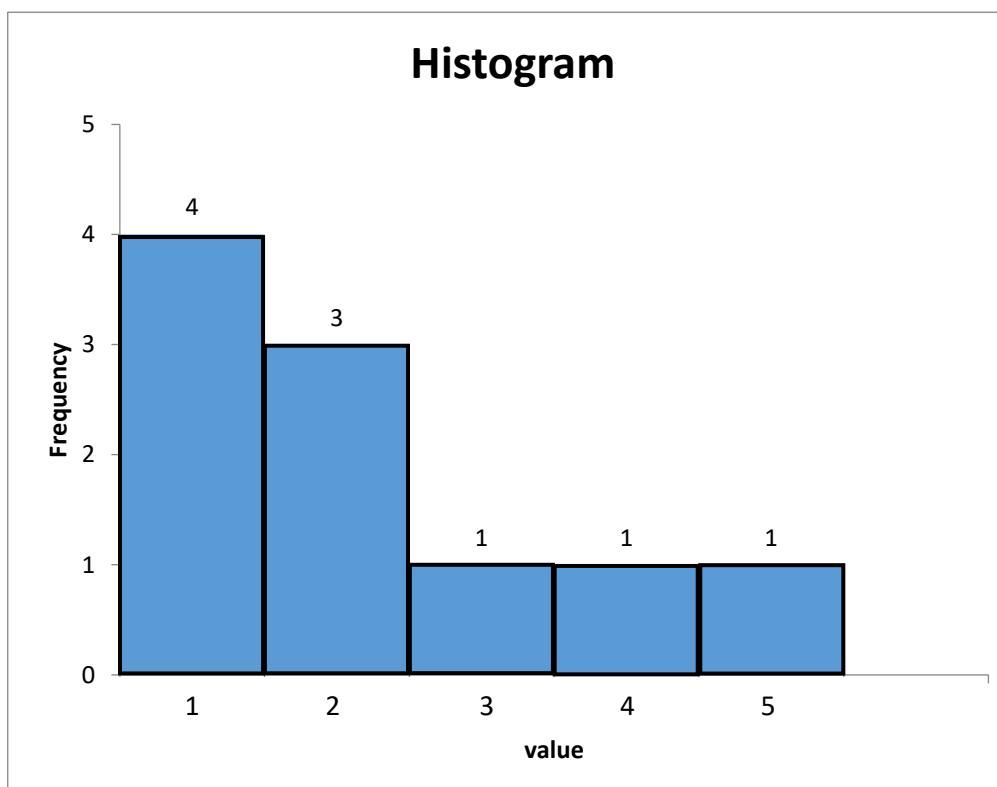
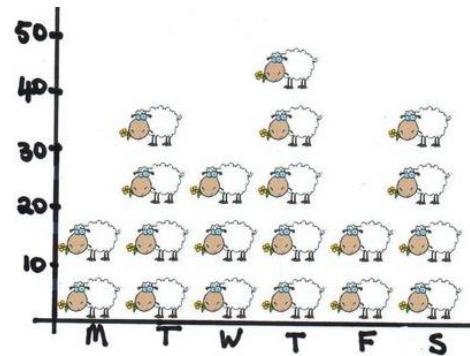
**Example:** At a fund-raising event, participants got to roll one bowling ball down a lane. For every pin that a participant knocked down, the manager donated \$2 to a charity. The following dot plot shows the number of pins knocked down by each of the participants.



- 1. How many participants were there?**
  
- 2. What was the fewest number of pins any participant knocked down?**
  
- 3. How many participants knocked down at least 9 pins?**
  
- 4. How many participants knocked down at most 7 pins?**

## Histogram:

Special bar graph where the bars are centered at the values, touch adjacent bars, and the height is the frequency.



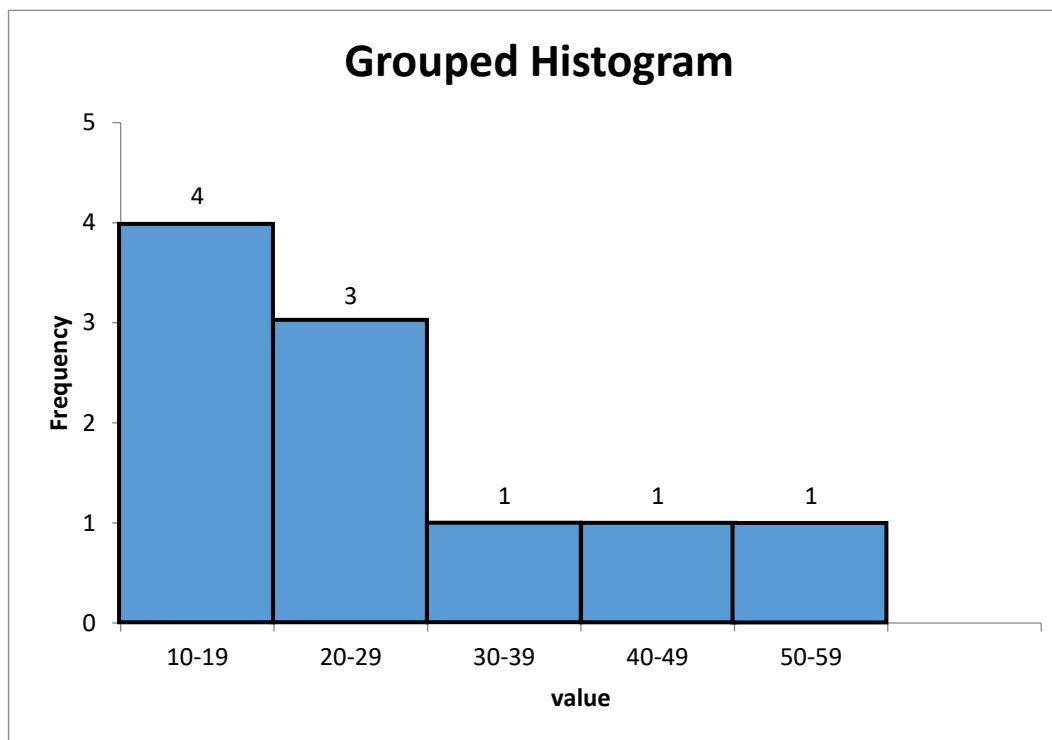
## Baa Graph

Allows easy visual determination of the most and least frequently occurring values!

## Grouped Histogram:

Similar to a histogram

Class	Frequency
10-19	4
20-29	3
30-39	1
40-49	1
50-59	1
Total	10



George found he could track his dried grass yields most effectively by organizing them into haystograms

**Here is a data set consisting of 1,000 values from 0 to 9.**

9	4	6	5	8	3	7	5	3	5
2	3	7	6	1	5	9	5	5	6
3	5	5	8	8	3	8	7	7	7
5	6	6	5	2	4	4	7	4	6
5	6	4	5	4	6	4	5	7	3
2	4	5	4	6	6	3	5	6	2
4	3	4	7	5	2	5	5	5	6
7	3	5	6	4	3	8	3	4	6
6	6	5	6	6	6	6	3	5	6
7	2	5	8	9	5	7	4	4	4
7	5	4	3	7	4	5	6	6	8
5	4	6	6	6	7	6	7	2	6
6	5	4	6	2	7	5	5	3	6
3	7	4	4	6	2	6	6	4	5
3	5	8	4	6	5	2	4	4	5
8	7	7	6	3	6	4	5	5	3
4	5	5	3	5	4	2	6	6	5
6	4	4	6	4	6	4	4	6	7
4	5	4	7	5	5	9	4	5	4
6	6	4	3	8	6	5	4	5	4
2	4	6	6	5	5	5	6	6	6
7	7	5	5	6	2	2	4	4	6
8	9	9	7	3	6	4	6	4	5
5	7	5	2	4	3	4	4	5	6
4	4	8	4	6	8	4	5	8	5
8	7	5	1	3	6	4	6	6	7

8	5	4	5	2	2	5	8	5	5
1	6	7	4	9	1	6	6	7	4
5	5	6	5	5	6	6	2	7	2
7	6	3	6	5	6	4	8	3	5
3	5	6	4	8	7	5	6	8	6
3	4	6	2	6	4	8	4	5	5
5	3	6	6	4	5	6	5	4	5
2	7	7	7	4	4	6	5	4	8
6	4	5	4	5	6	8	5	4	7
2	2	2	7	6	3	3	5	4	5
6	4	3	5	8	4	3	4	6	2
3	6	6	3	3	4	7	4	3	2
6	3	6	3	6	4	3	4	3	3
2	6	6	4	5	6	3	5	4	3
6	3	3	3	7	4	4	5	1	5
3	3	5	6	4	3	5	5	4	4
6	6	7	6	6	3	4	8	2	5
6	5	5	5	7	8	4	1	5	
3	4	4	3	4	5	6	4	5	5
4	5	6	5	4	4	7	6	7	3
5	4	4	5	5	5	6	4	4	5
5	3	7	7	2	3	7	6	6	5
2	5	3	3	4	3	4	4	7	6
6	6	3	6	4	5	2	3	6	4
6	6	6	3	6	5	5	2	7	3
4	5	5	3	2	4	6	7	2	2
6	4	5	7	3	4	6	4	5	2
5	7	4	4	3	5	2	7	6	5
5	5	3	4	5	2	6	3	4	4
3	4	6	4	6	5	6	5	5	1

4	3	5	6	5	6	7	6	3	5
6	8	5	3	5	5	6	4	6	3
4	4	5	5	6	5	1	4	6	5
4	4	5	5	5	4	5	5	7	7
6	6	4	5	5	5	2	7	6	4
6	5	6	4	5	6	5	4	3	4
5	5	4	4	6	4	4	5	3	3
7	5	4	6	4	3	3	2	5	5
8	6	7	6	6	4	8	6	5	5
2	6	4	5	4	4	5	5	5	5
5	4	5	4	4	5	4	4	6	2
7	5	5	6	5	4	4	8	6	5
5	4	6	5	6	6	6	2	6	5
1	5	7	6	6	5	8	5	8	7
3	2	5	5	3	6	5	3	6	4
5	7	6	7	3	7	2	4	4	6
7	6	9	6	6	4	4	6	6	5
5	5	5	6	6	5	4	4	4	5
6	4	8	3	8	4	4	5	7	5
3	7	3	5	4	5	5	5	7	3
8	4	4	4	5	6	5	5	3	4
5	6	7	4	5	6	5	4	2	5
3	8	7	5	5	3	9	4	5	4
5	3	3	5	5	8	4	6	7	5
8	5	6	5	3	7	6	7	6	5
6	2	3	1	5	4	7	5	5	4
5	6	6	5	8	4	6	5	6	4
6	6	7	7	6	3	7	5	6	3
2	5	7	7	3	6	6	4	7	5
3	7	8	5	5	5	3	5	5	5

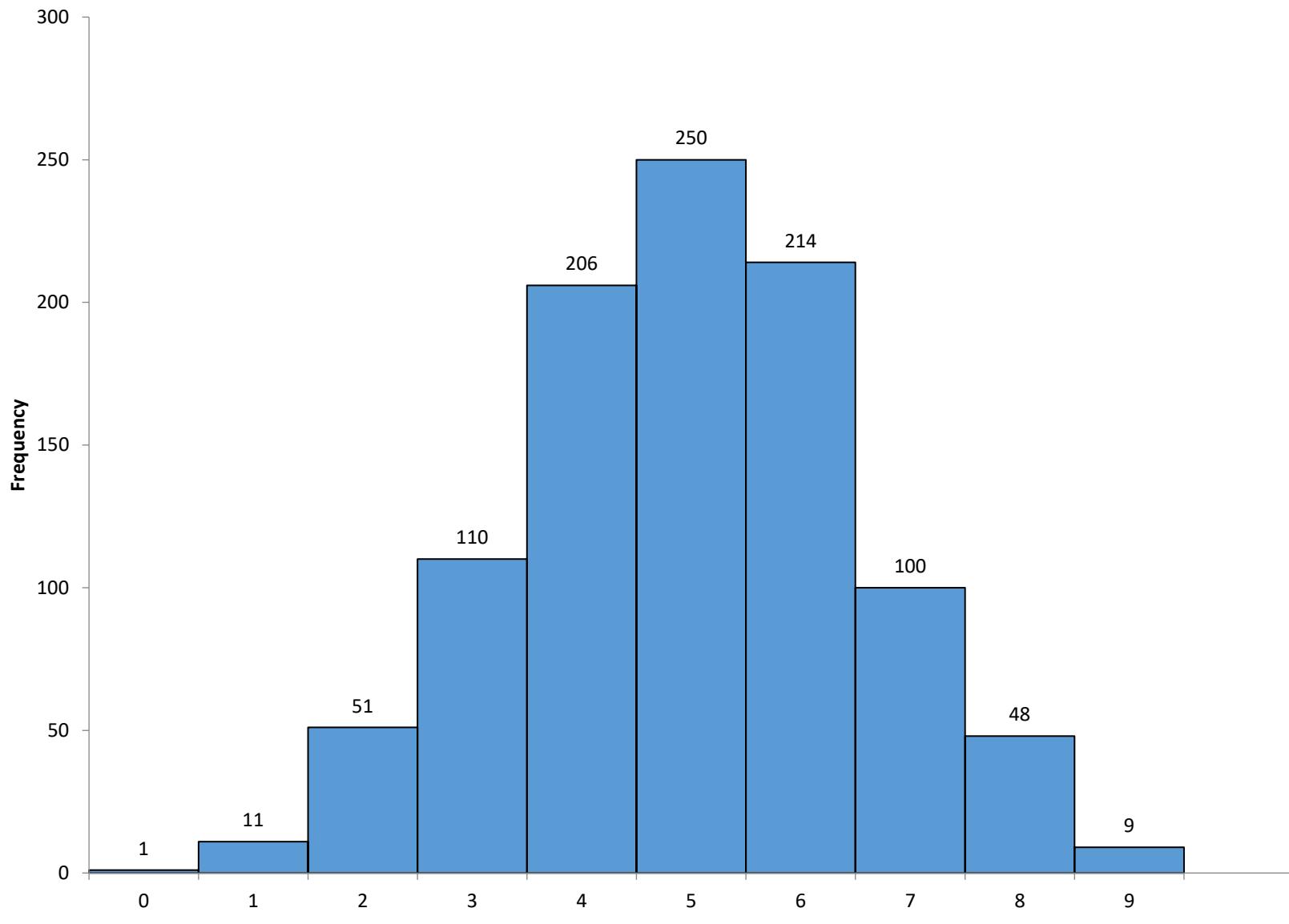
6	4	7	4	3	4	5	5	4	6
4	6	7	7	6	4	5	6	6	8
7	3	8	6	3	7	5	8	5	7
4	4	4	5	6	4	8	7	6	6
4	5	5	2	6	4	6	4	5	6
3	0	4	5	7	5	4	6	8	6
5	6	6	7	7	5	6	4	7	5
3	4	6	6	5	4	6	8	3	4
6	7	5	7	7	5	6	5	5	4
6	6	4	4	5	3	6	6	5	4
4	5	5	5	4	5	5	4	2	5
3	3	7	3	4	7	4	1	4	6
4	6	8	3	5	3	6	4	7	4
5	6	7	4	3	2	4	7	8	6

**Excel can automatically construct a frequency distribution and histogram for this large data set.**

$x$	<i>Frequency</i>
0	1
1	11
2	51
3	110
4	206
5	250
6	214
7	100
8	48
9	9
<b>Total</b>	<b>1,000</b>

A nice compact summary of this large data set!

# Histogram



**Here is a data set consisting of 1,000 values from 36 to 92.**

62	56	54	58	66	58	64	53	63	69
74	58	59	55	61	63	71	54	64	54
63	39	61	44	61	50	52	62	45	63
63	56	58	67	76	57	55	58	65	49
76	63	61	60	60	70	60	55	79	48
63	50	55	57	76	57	73	47	58	62
49	71	56	59	70	45	57	60	68	73
52	60	60	80	66	51	62	68	54	58
61	58	64	67	66	61	51	63	52	57
71	60	62	53	60	68	57	57	62	55
64	46	54	63	64	66	65	49	56	72
69	63	63	67	72	64	51	68	63	40
62	57	69	68	49	65	66	71	53	68
59	56	52	61	54	58	61	63	76	75
65	64	51	61	63	57	58	66	63	46
73	69	54	57	51	51	54	60	59	52
59	53	49	56	54	57	64	68	64	64
61	64	57	62	57	56	65	51	58	50
59	56	68	65	71	56	63	71	58	59
65	63	64	63	58	66	74	53	71	76
55	73	65	67	59	52	52	62	55	70
60	64	77	58	57	58	63	68	54	64
69	57	61	62	58	57	51	62	66	52
61	67	69	73	54	70	51	71	45	54
69	54	57	65	67	67	69	70	55	46
67	52	62	60	47	62	51	68	67	55

71	76	56	53	63	60	57	41	64	66
59	62	64	53	54	64	52	73	73	62
68	58	58	70	68	74	65	43	65	52
81	57	57	58	54	64	72	71	58	66
56	64	62	68	48	53	41	56	68	73
60	49	56	55	70	53	59	61	71	60
44	79	64	60	56	67	45	57	50	58
54	54	46	69	59	51	66	53	58	64
65	59	55	60	53	58	85	59	60	70
67	58	79	64	61	68	57	53	45	56
67	57	69	40	71	61	74	61	63	56
57	59	63	49	66	53	57	51	47	50
57	56	65	63	65	71	60	70	64	60
51	69	53	53	71	54	65	48	47	62
81	58	55	73	65	59	65	70	65	58
65	69	49	53	60	59	56	60	55	53
56	58	61	67	59	68	64	59	66	58
63	61	58	66	62	67	66	59	75	54
55	55	71	47	58	70	48	57	49	55
52	55	60	53	68	63	51	64	64	77
54	70	67	49	59	52	57	69	92	65
78	74	54	67	55	57	69	59	55	58
52	73	60	69	47	55	64	61	53	60
48	54	59	54	62	63	68	57	72	71
43	58	58	70	57	50	53	63	61	69
68	61	53	60	60	59	81	63	51	53
42	47	49	64	68	60	68	71	55	41
59	56	52	54	50	54	60	69	61	50
70	55	56	48	64	70	53	51	54	56
62	70	67	57	68	56	60	54	60	71

59	61	60	54	62	71	56	79	59	55
49	50	63	59	47	64	53	62	56	50
68	58	72	60	55	50	57	59	54	68
65	44	57	61	79	58	54	66	72	65
69	57	62	57	72	61	58	56	61	36
59	52	58	68	50	57	63	48	83	57
46	53	69	65	59	45	61	72	61	71
50	58	64	63	64	62	66	72	62	53
62	50	73	72	58	51	59	66	52	47
62	49	72	57	65	66	55	67	52	53
54	63	59	61	60	49	52	59	60	61
65	59	66	68	59	53	70	66	56	49
62	56	58	66	51	58	83	69	49	54
72	52	59	55	56	70	62	60	70	57
58	56	53	54	60	74	62	64	60	63
64	53	62	56	56	72	53	66	60	57
63	60	59	67	52	69	53	53	49	66
76	64	58	63	51	63	44	69	74	61
54	51	67	44	56	66	56	53	54	66
58	46	54	61	53	62	50	58	55	59
55	51	55	52	65	61	58	60	69	55
65	66	72	56	58	63	49	47	69	54
64	69	54	68	60	71	58	66	53	59
72	69	51	62	55	45	47	59	69	61
65	61	56	59	64	65	64	56	60	61
69	79	54	74	65	62	64	51	58	55
46	54	54	67	66	45	53	70	51	69
47	53	70	63	66	42	47	47	62	51
64	53	57	60	69	56	61	54	57	51
54	48	65	57	57	61	62	59	70	73

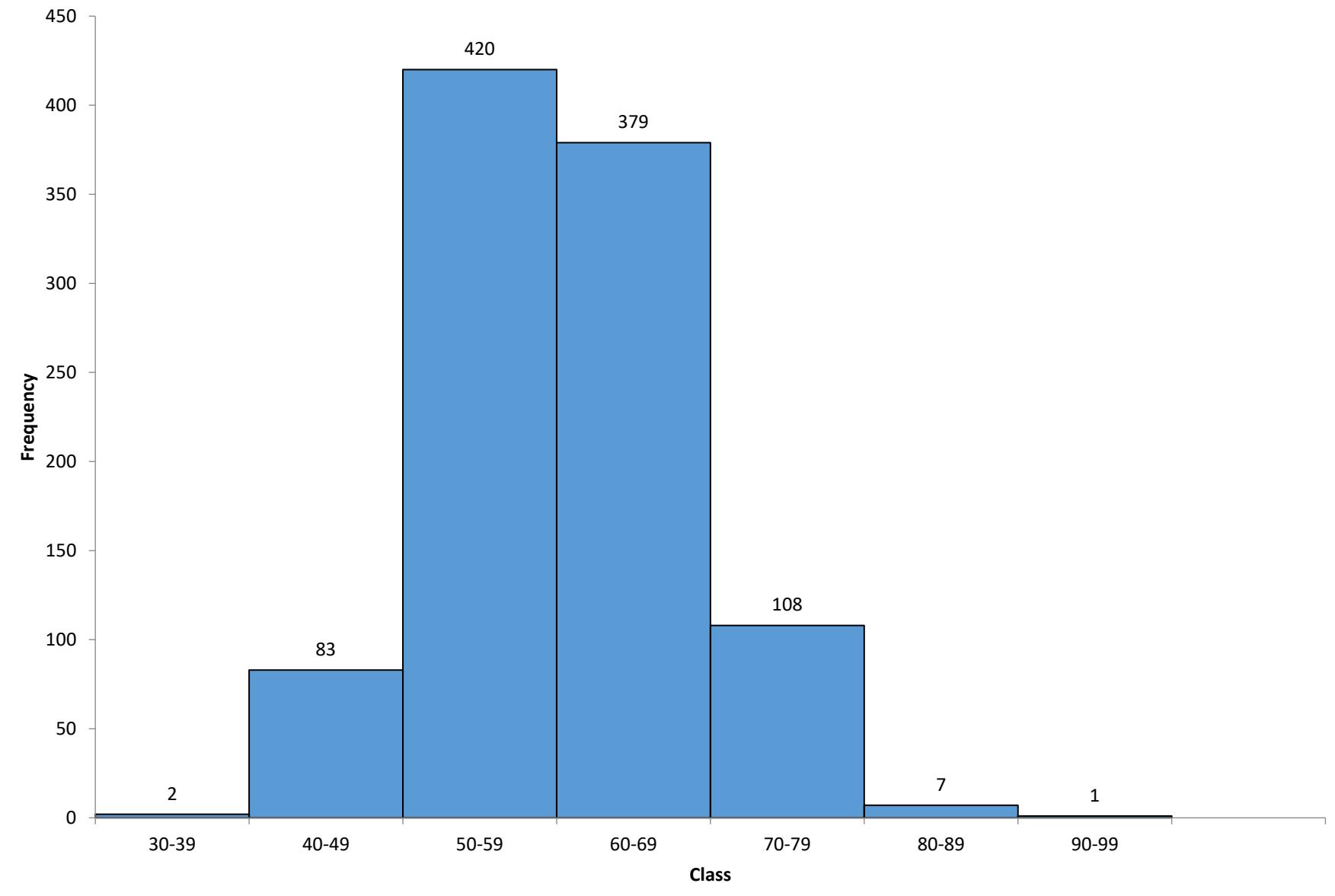
69	46	56	52	64	65	52	63	63	57
60	65	59	58	52	51	50	64	53	44
59	68	59	54	63	49	62	64	52	53
65	53	47	57	52	48	59	61	61	40
60	73	54	60	70	49	47	60	55	53
51	52	60	63	59	51	52	69	58	52
54	63	69	51	74	54	57	54	59	62
76	61	70	70	51	70	65	73	53	60
61	55	70	57	52	59	53	51	58	68
40	53	64	50	69	48	59	56	58	68
56	61	54	60	56	55	58	41	63	63
58	66	54	62	53	55	49	53	48	59
61	59	72	54	50	49	65	50	57	78
68	60	51	69	53	62	63	56	53	74

**Excel can automatically construct a grouped frequency distribution and histogram for this large data set.**

<i>Class</i>	<i>Frequency</i>
<b>30-39</b>	<b>2</b>
<b>40-49</b>	<b>83</b>
<b>50-59</b>	<b>420</b>
<b>60-69</b>	<b>379</b>
<b>70-79</b>	<b>108</b>
<b>80-89</b>	<b>7</b>
<b>90-99</b>	<b>1</b>
<b>Total</b>	<b>1,000</b>

A nice compact summary of this large data set!

## Grouped Histogram

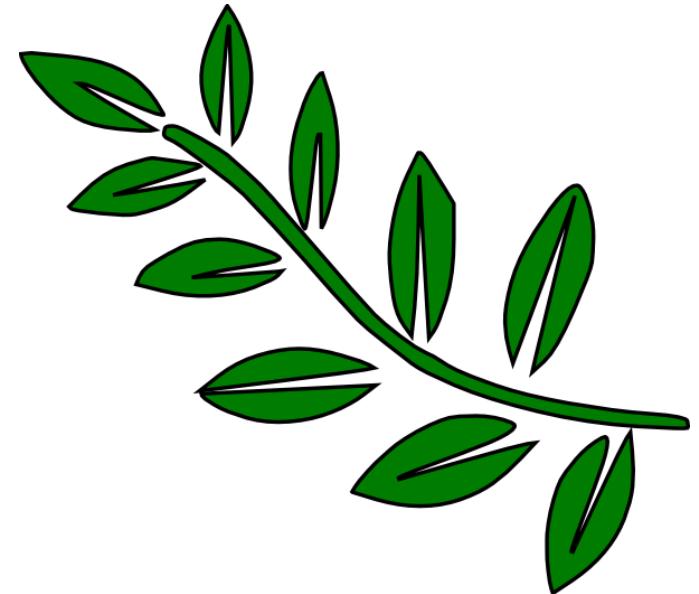


## Stem and Leaf Plot:

The actual data values themselves are used to create a frequency distribution of the data set.

**Data Set:** {10,22,31,11,22,36,46,45,50,42}

1	0	1
2	2	
3	1	
4		
5		



Allows easy visual determination of the most and least frequently occurring decades!



You did WHAT  
with my leaves???

## Ordered Stem and Leaf Plot:

<b>1</b>	0	1
<b>2</b>	2	2
<b>3</b>	1	6
<b>4</b>	6	5    2
<b>5</b>	0	

The leaves are listed in ascending order.

<b>1</b>
<b>2</b>
<b>3</b>
<b>4</b>
<b>5</b>

Allows easy visual determination of the smallest and largest values!

**Example:**

<b>3</b>	2	3	5	8
<b>4</b>	0	3	9	
<b>5</b>	1	1		
<b>6</b>	2	2	7	
<b>7</b>	0	0	0	5

**How many values are in the data set?**

**What's the smallest value?**

**What's the largest value?**

**What's the most frequently occurring value?**

**How many values are in the 60's?**

**Which decade has the fewest values?**

Split Stem and Leaf Plot	
0	1, 1, 3
0	6, 7, 7, 8
1	0, 2, 2, 3
1	8
2	1, 3, 3, 3, 4, 5, 6, 7, 8, 9
2	1, 3, 3, 3, 4
2	5, 6, 7, 8, 9
3	1, 1, 1, 4, 6
3	1, 1, 1, 4
3	6

Key: 1 | 2 = 12 inches  
NOTE: LEAVES <= 25  
Key: 1 | 2 = 12 inches

### Split Stem-and-Leaf Plots:

Sometimes the stems are split into two with the first stem getting the digits 0-4 and the second stem getting the digits 5-9. Instead of a histogram with class widths of 10, the class widths are 5.



3	2	3
3	5	8
4	0	3
4	9	
5	1	1
5		
6	2	2
6	7	
7	0	0
7	5	

Which range of 5 contains the most values? Which range of 5 contains the fewest values?

## Back-to-Back Stem-and-Leaf Plots:

Used to compare two data sets.

Data Set A	Data Set B
	1    6    8
	2    1    4    5    6    7    7
	7    3    0    5    9    9    9
	2    4    1    3    4    6    7    8
6    5    5    5    4    3    2    1	5    5
7    7    6    6    5    4    3    1	6    2
9    9    8    8    7    7    3    2    2    0	7
6    5    4    2    1    0    0	8
	9



The values of which data set are generally larger?

Which data set has more values?

What value is common to both data sets?

## Line Graph:

Plots data over time to indicate trends(up or down).



Year	Profit in Dollars
2004	75,465
2005	82,160
2006	86,187
2007	97,355
2008	110,423
2009	94,191
2010	103,505

**Trends are more easily detected visually.**