## **Traveling Salesman Problem:**

It's the problem of finding a Hamilton circuit in a complete weighted graph that has the smallest weight. Such a Hamilton circuit is called an <u>optimal solution</u> of the

problem.



## **Brute Force Method:**

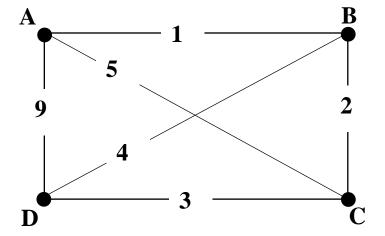
1. List all the Hamilton circuits.





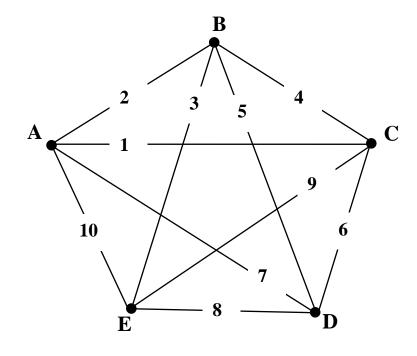
- 2. Determine the weight of each of the listed Hamilton circuits.
- 3. Hamilton circuits with the minimum weight are optimal solutions.

## **Examples:**



Hamilton circuit	Weight
<b>A,B,C,D,A</b>	15
<b>A,B,D,C,A</b>	13
A,C,B,D,A	
A,C,D,B,A	
A,D,B,C,A	
A,D,C,B,A	

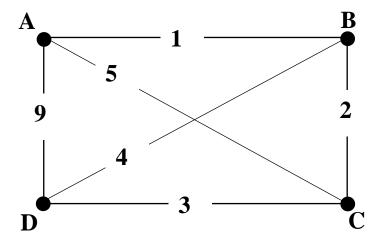
Hamilton Circuit	Weight
A,B,C,D,E,A	30
A,B,C,E,D,A	30
A,B,D,C,E,A	32
A,B,D,E,C,A	25
A,B,E,C,D,A	27
A,B,E,D,C,A	20
A,C,B,D,E,A	28
A,C,B,E,D,A	23
A,C,D,B,E,A	25
A,C,D,E,B,A	20
A,C,E,B,D,A	25
A,C,E,D,B,A	25
A,D,B,C,E,A	35
A,D,B,E,C,A	25
A,D,C,B,E,A	30
A,D,C,E,B,A	27
A,D,E,B,C,A	23
A,D,E,C,B,A	
A,E,B,C,D,A	
A,E,B,D,C,A	
A,E,C,B,D,A	
A,E,C,D,B,A	
A,E,D,B,C,A	
A,E,D,C,B,A	



There is a method for producing approximate optimal solutions called the <u>Nearest</u>

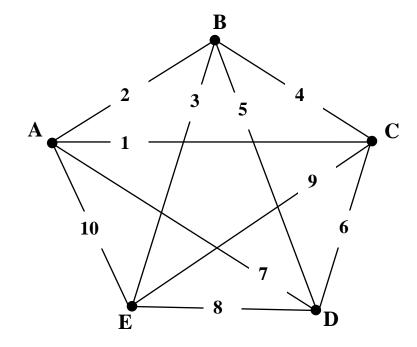
Neighbor Method.

- 1. Choose a starting vertex.
- 2. Choose the edge with the smallest weight.
- 3. From the next vertex, choose the edge with the smallest weight that doesn't lead to a previously visited vertex.
- 4. Continue until all vertices are visited exactly once, and you've returned to the starting vertex.



Find a Nearest Neighbor approximate optimal solution starting at the given vertex.

<b>Starting vertex</b>	Nearest Neighbor solution
A	
В	



Find a Nearest Neighbor approximate optimal solution starting at the given vertex.

<b>Starting vertex</b>	<b>Nearest Neighbor solution</b>
A	
D	