

Review of Radical Equations:

1. Isolate a radical on one side of the equation.

2. Raise both sides to a power that eliminates the isolated radical.

3. Repeat steps 1 and 2, if needed.

4. Solve the new radical-free equation.

5. Check your solution(s) in the original equation.



Examples:

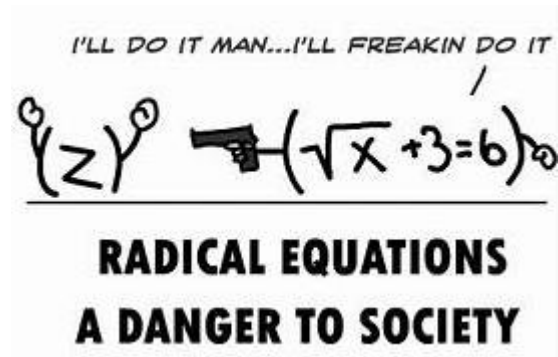
1. $\sqrt{5x+2} = 7$

2. $\sqrt{3x} - 4 = 6$

3. $\sqrt[3]{x} = -2$

4. $\sqrt{x-3} = -4$

5. $x - 5 = \sqrt{x+7}$

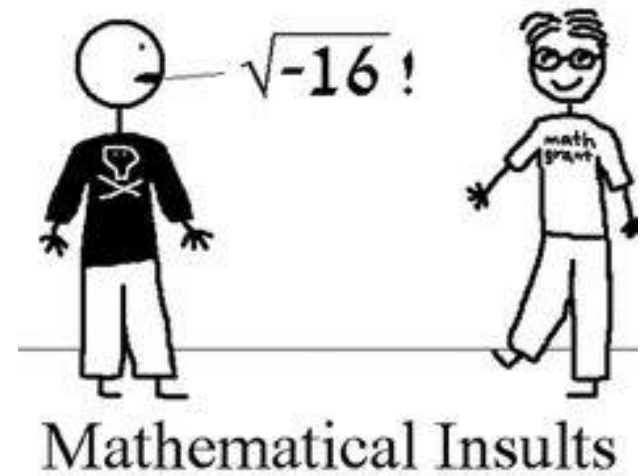


6. $\sqrt{2x+7} - 2 = x$

7. $\sqrt{5x-3} = \sqrt{2x+3}$

8. $\sqrt{x-9} + \sqrt{x} = 1$

9. $\sqrt{4x-3} = 2 + \sqrt{2x-5}$



Quadratic-like radical equations:

1. $x^{\frac{2}{3}} + x^{\frac{1}{3}} - 6 = 0$

$$\left(x^{\frac{1}{3}}\right)^2 + x^{\frac{1}{3}} - 6 = 0 \text{ or } \left(\sqrt[3]{x}\right)^2 + \sqrt[3]{x} - 6 = 0$$

2. $x^{\frac{1}{2}} - 4x^{\frac{1}{4}} + 3 = 0$

$$\left(x^{\frac{1}{4}}\right)^2 - 4x^{\frac{1}{4}} + 3 = 0 \text{ or } \left(\sqrt[4]{x}\right)^2 - 4\sqrt[4]{x} + 3 = 0$$

Write a single radical expression.

$$\frac{\sqrt[4]{x-3}}{\sqrt{x-3}}$$

"That's totally gnarly, dude!"

Absolute Value Equations:

The absolute value of a number is its distance from zero on the number line.

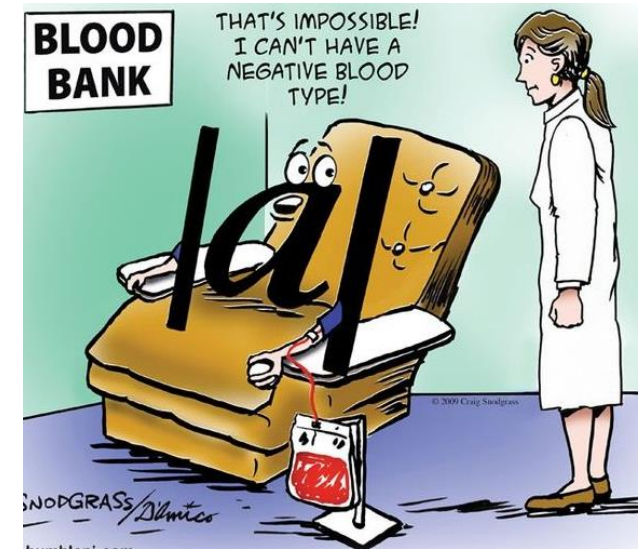
1. For $a > 0$,

$|something| = a$ means that $something = \pm a$.

2. For $a < 0$,

$|something| = a$ means that the equation has no solution.

3. $|something| = 0$ means that $something = 0$.



Solve the absolute value equation.

$$|7x + 2| = -3$$

No SOLUTION!

Examples:

1. $|x| = 5$

2. $|x| = -9$

3. $|3x - 2| = 7$

4. $|x| - 2 = 6$

5. $|6x| + 8 = 32$

Absolute Value Equations

$$6. \left| \frac{4-5x}{6} \right| = 7$$

$$|X + 3| = |X - 11|$$

Plenty of Example Problems!

$$7. 2|2x-7|+11=25$$

$$8. |x-6| = -8$$

$$9. |2x-8| = |x+3|$$

{If $|a| = |b|$, then either $a = b$ or $a = -b$.}

$$10. |x-15| = |x+8|$$