

Ex: A wolf population is growing exponentially.

In 2011, 129 wolves were counted.

In 2013, the population has reached 236 wolves.

- ① What are the 2 data points that can be used to derive the exp. function that models this situation?
- ② Find exp. function.

(1) Data points: $(0, 129)$; $(2, 236)$.

(2) $f(x) = 129 \cdot (1.35)^x$

$$a = 129 \quad 129 \cdot b^2 = 236$$

$$b^2 = \frac{236}{129}; b = 1.35$$

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Compound - Interest Formula

$$A(t) = P \left(1 + \frac{r}{n}\right)^{nt}$$

P: the starting (initial) amount in the account. (P is called the principal)

n: annual interest rate

n: # of compounding periods per year. (monthly: $n=12$, quarterly: $n=4$, semiannually: $n=2$)

A(t): the value of the account after t years

t: measured in years.

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E.g. An initial investment of $\$100,000$ at 12% interest is compounded weekly. What will the investment be worth in 30 years?

$$A(t) = P \left(1 + \frac{r}{n}\right)^{nt}$$

$$P = \$100,000$$

$$r = 0.12$$

$$n = 52$$

$$A(30) = 100000 \cdot \left(1 + \frac{0.12}{52}\right)^{52 \cdot 30} \approx 3.644 \times 10^6$$

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Constant e.

e is a constant, $e \approx 2.718282$

Continuous Compound Interest Formula:

$$A(t) = P \cdot e^{rt}$$

If $P = 100,000$; $r = 0.12$ $\bullet 12 \times 30$

$$A(30) = 100000 \cdot (2.718282) \approx 3.653 \times 10^6$$

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Write an exponential function $y = ab^x$ for a graph that passes through $(2, 1)$ and $(3, 6)$.

$y = \frac{1}{36} \cdot (6)^x$

$ab^2 = 1 \rightarrow a = \frac{1}{b^2}$

$ab^3 = 6 \rightarrow \frac{1}{b^2} \cdot b^3 = 6 \rightarrow b = 6, a = \frac{1}{36}$

$y = 4 \cdot \left(\frac{1}{2}\right)^x; f(x) = 4 \cdot \left(\frac{1}{2}\right)^x; f(-4) = 4 \cdot \left(\frac{1}{2}\right)^{-4} = 64$

The graph of an exponential function of the form $f(x) = ab^x$ passes through $(1, 2)$ and $(2, 1)$.

$f(-4) = 64$

$ab^1 = 2 \rightarrow a = \frac{2}{b}$

$2b = 1; b = \frac{1}{2}, a = 4$

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