

M.C. $24 = 8 \cdot 3$

① $12x^2 + 14x + 2 = 0$
 $12x^2 + 8x + 3x + 2 = 0$
 $4x(3x+2) + 3x+2 = 0$
 $(3x+2)(4x+1) = 0$
 $3x+2=0$ $4x+1=0$
 $x = -\frac{2}{3}$ $x = -\frac{1}{4}$
 $-\frac{2}{3} - \frac{1}{4} = -\frac{8-3}{12} = -\frac{5}{12}$

② $x^2 + x + 1 = 0$
 Discriminant $= b^2 - 4ac = 1 - 4 \cdot 1 \cdot 1 = -3 < 0$

Sum of solutions $= -\frac{b}{a}$
 $-\frac{b \pm \sqrt{b^2 - 4ac}}{2a}$
 $-\frac{1 \pm \sqrt{1-4}}{2}$
 $-\frac{1 \pm \sqrt{-3}}{2}$
 $-\frac{1 \pm i\sqrt{3}}{2}$
 $-\frac{2b}{2a} = -\frac{b}{a}$

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③ $(x+5)^{\frac{3}{2}} = 8$
 $x+5 = 8^{\frac{2}{3}} = (\sqrt[3]{8})^2 = 2^2 = 4$
 $x+5 = 4$; $x = -1$

④ $|4x+1| - 3 = 6$; $|4x+1| = 9$
 $4x+1 = 9$ on $4x+1 = -9$ $2 - \frac{5}{2}$
 $4x = 8$ $4x = -10$
 $x = 2$ $x = -\frac{5}{2}$ $= \frac{4-5}{2} = -\frac{1}{2}$

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⑤ $\frac{3}{4} = \frac{\frac{1}{2}}{\frac{1}{2}}$
 $3x = x$
 $3x = x$
 $3x - x = 0$
 $2x = 0$
 $x = 0$

⑥ $g(x) = \sqrt{x-4}$. Solve the equation: $g(x) = 2$
 $(\sqrt{x-4})^2 = 2^2$
 $x-4 = 4$; $x = 8$

$x = \frac{1}{3}$ $3x^{\frac{1}{4}} - 1 = 0$
 $3x^{\frac{1}{4}} = 1$; $\frac{1}{x} = \frac{1}{3}$; $x = (\frac{1}{3})^4 = \frac{1}{81}$

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⑦ $f(x) = x^2 + 3x - 4$. Find $f(a+1)$
 $f(a+1) = (a+1)^2 + 3(a+1) - 4$
 $= a^2 + 2a + 1 + 3a + 3 - 4$
 $= a^2 + 5a$

⑧

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⑨ $f(2) = -1$

⑩
 Range: $[0, \infty)$

⑪ Domain: $f(x) = -2x(x-1)(x-2)$
 Domain: $(-\infty, \infty)$

⑫ $g(x) = \frac{x+3}{x^2+5x+6}$ Domain: $x = -3$
 Domain: $(-\infty, -3) \cup (-3, -2) \cup (-2, \infty)$ $x^2+5x+6 = 0$ $x = -2$
 $(x+3)(x+2) = 0$

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⑬ Domain of $f(x) = \sqrt{4-3x}$
 $4-3x \geq 0$
 $4 \geq 3x$
 $\frac{4}{3} \geq x$
 $x \leq \frac{4}{3}$
 Domain: $(-\infty, \frac{4}{3}]$

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14)
$$f(x) = \begin{cases} x^2 - 2 & \text{if } x < 2 \\ 4 + |x - 5| & \text{if } x \geq 2 \end{cases}$$

$f(2) = 4 + |2 - 5| = 4 + |-3| = 4 + 3 = 7$.

15) A.R.O.C. of $f(x) = x - 2\sqrt{x}$ on $[1, 9]$.

$$\frac{f(9) - f(1)}{9 - 1} = \frac{f(9) - f(1)}{8} = \frac{(9 - 2\sqrt{9}) - (1 - 2\sqrt{1})}{8} = \frac{8 - 4}{8} = \frac{4}{8} = \frac{1}{2}$$

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16) $f(x) = x^2 + 2x - 8$.

A.R.O.C. on $[5, a]$.

$$\frac{f(a) - f(5)}{a - 5} = \frac{a^2 + 2a - 8 - (5^2 + 2 \cdot 5 - 8)}{a - 5} = \frac{a^2 + 2a - 8 - (27)}{a - 5} = \frac{a^2 + 2a - 35}{a - 5} = \frac{(a - 5)(a + 7)}{a - 5} = a + 7$$

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A.R.O.C.

$$\frac{f(7) - f(1)}{7 - 1} = \frac{3 - 5}{6} = \frac{-2}{6} = -\frac{1}{3}$$

18) $(1, 3) \cup (5, 7)$ • decreasing. $\left[-\frac{1}{3}\right]$.

19) $f(a) < f(b)$ for $a < b$.

20) $\frac{3.68 - 3.30}{2012 - 2008} = \frac{0.38}{4} = 0.095$

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21) (a) $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$.

(b) If $a \cdot b = 0$, then either $a = 0$ or $b = 0$.

(c) A relation is set of ordered pairs.

(d) a relation in which every input leads to exactly one output.

(e) $x = \pm \sqrt{k}$

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22) (a) $x^3 + 2x^2 - x - 2 = 0$

$$x^2(x+2) - (x+2) = 0$$

$$(x^2 - 1)(x+2) = 0$$

$$(x-1)(x+1)(x+2) = 0 \quad -18 = -9 \cdot 2$$

$x = 1$ or $x = -1$ or $x = -2$.

(b) $(\sqrt{x+3})^2 = (3x-1)^2$

$$x+3 = (3x-1)(3x-1)$$

$$x+3 = 9x^2 - 3x - 3x + 1$$

$$x+3 = 9x^2 - 6x + 1$$

$$9x^2 - 7x - 2 = 0$$

$$9x^2 - 9x + 2x - 2 = 0$$

$$9x(x-1) + 2(x-1) = 0$$

$$(x-1)(9x+2) = 0$$

$x = 1$ or $x = -2/9$

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$x = 1$

$$\sqrt{1+3} = 3 \cdot 1 - 1$$

$$\sqrt{4} = 2$$

$$2 = 2$$

$x = -2/9$

$$\sqrt{-2/9 + 3} = 3 \cdot (-2/9) - 1$$

$$\sqrt{25/9} = -5/3$$

$$5/3 \neq -5/3$$

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