

5.2. Systems of linear Inequalities in 2 variables

Goals: (1) Solve system of linear inequalities by graphing
(2) Solve application problems

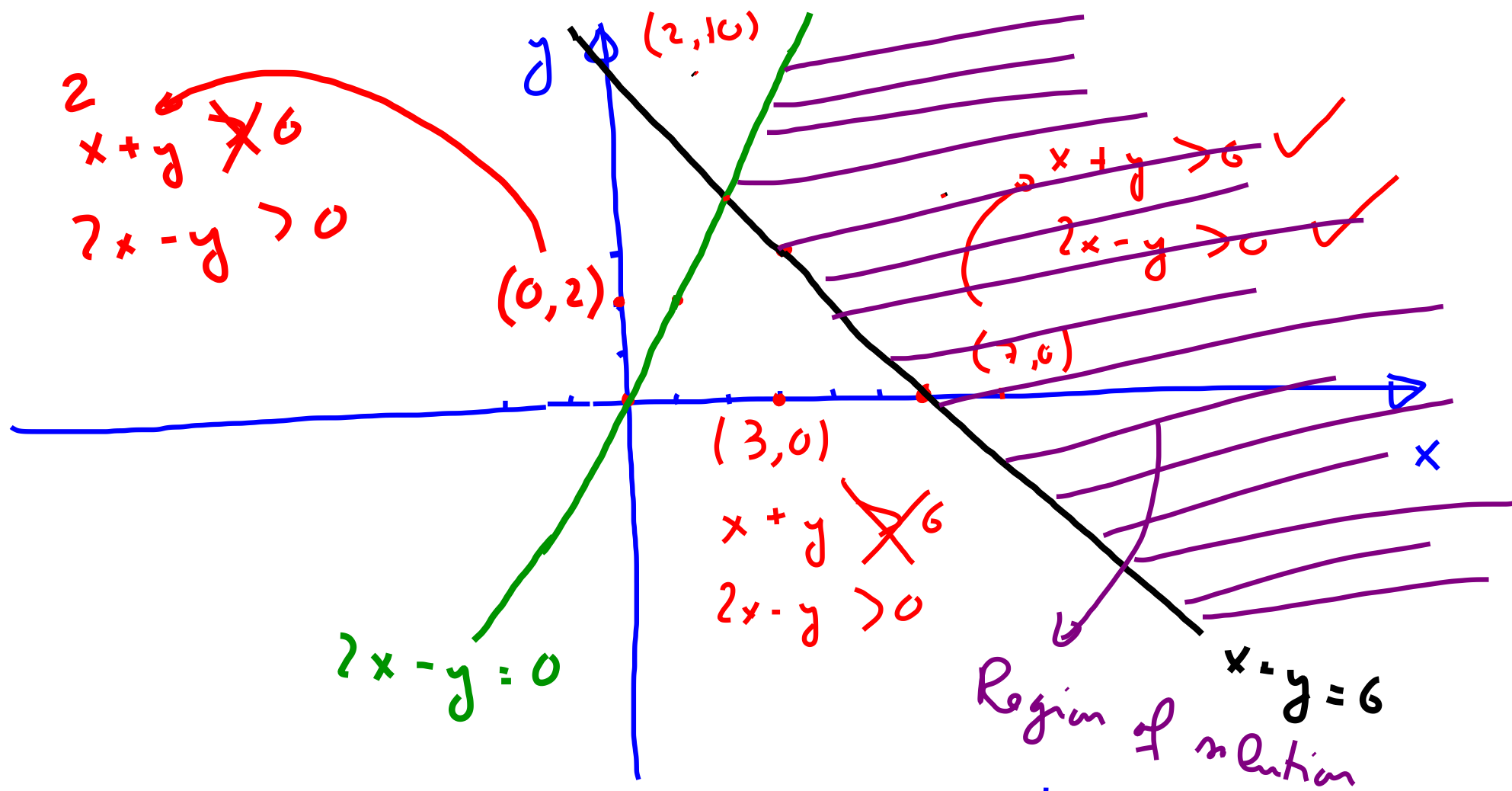
E.g. $x + y > 6$

$$2x - y > 0$$

(1) Graph the equalities: $x + y = 6$
 $2x - y = 0$

x	y
0	6 $\rightarrow (0, 6)$
3	3 $\rightarrow (3, 3)$

x	y
0	0 $\rightarrow (0, 0)$
1	2 $\rightarrow (1, 2)$



② 2 lines divide the plane into 4 regions.
 Choose test points in each region to see which one
 satisfies the 2 inequalities

Using calculator:

① Get y by itself

$$x + y > 6 \longrightarrow$$

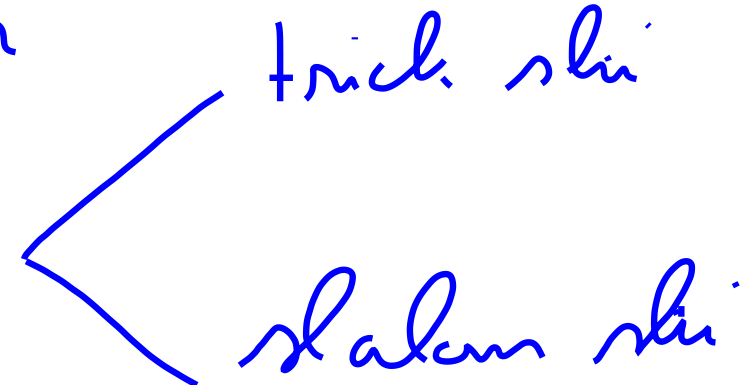
$$y > 6 - x$$

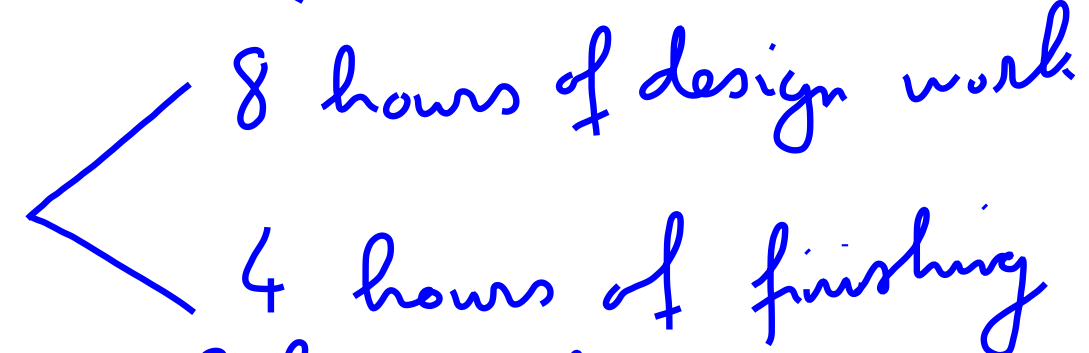
$$2x - y > 0 \longrightarrow -y > -2x \longrightarrow$$

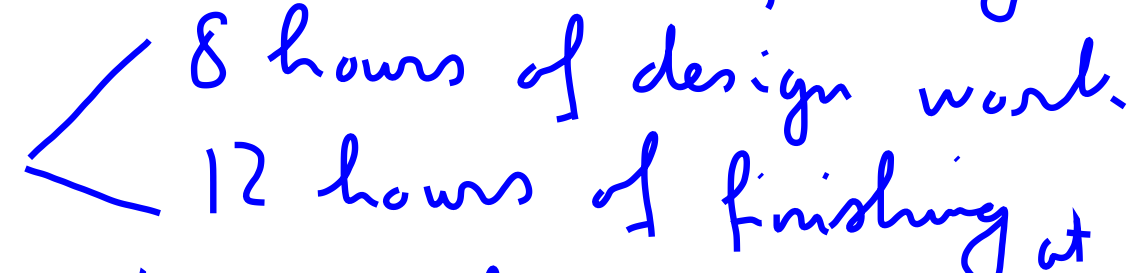
$$y < 2x$$

② Input into calculators. Using above / below function

Note: the feasible region in this example is
(region of solutions) unbounded.

E.g. Ski manufacturer
2 types of skis 

Each trick ski 
8 hours of design work
4 hours of finishing

Each slalom ski 
8 hours of design work
12 hours of finishing

Total # of hours allocated for design work is ^{at most} 160

Total # of hours for finishing at most 180.

trick skis produced is at most 15

x : # of trick skis produced

y : # of slalom skis produced.

Construct a system of inequalities for this problem and graph the feasible region.

$$x \geq 0$$

$$y \geq 0$$

$$x \leq 15$$

$$\underline{8x + 8y \leq 160}$$

$$\underline{4x + 12y \leq 180}$$

$$\textcircled{1} \quad \begin{aligned} 8x + 8y &= 160 \\ x + y &= 20 \end{aligned}$$

	x	y
(0,20)	0	20
(10,10)	10	10

$$\begin{aligned} 4x + 12y &= 180 \\ x + 3y &= 45 \end{aligned}$$

x	y	
0	15	(0,15)
15	10	(15,10)

