

FINITE MATHEMATICS

13th Edition

for Business, Economics,
Life Sciences, and
Social Sciences



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Chapter 8

Probability

Section R Review

Review for Chapter 8

Important Terms, Symbols, Concepts



- **8.1 Sample Spaces, Events, and Probability**
 - Probability theory is concerned with **random experiments** for which different outcomes are obtained no matter how carefully the experiment is repeated under the same conditions.
 - The set S of all possible outcomes of a random experiment is called a **sample space**. The subsets of S are called **events**. An event that contains only one outcome is called a **simple event**. Events that contain more than one outcome are **compound events**.

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- **8.1 Sample Spaces, Events, and Probability (continued)**
 - If $S = \{e_1, e_2, \dots, e_n\}$ is a sample space for an experiment, an **acceptable probability assignment** is an assignment of real numbers $P(e_i)$ to simple events such that $0 \leq P(e_i) \leq 1$ and $P(e_1) + P(e_2) + \dots + P(e_n) = 1$.
 - Each number $P(e_i)$ is called the **probability of the simple event e_i** . The **probability of an arbitrary event E** , denoted $P(E)$, is the sum of the probabilities of the simple events in E . If E is the empty set, then $P(E) = 0$.

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■ 8.1 Sample Spaces, Events, and Probability (continued)

- Acceptable probability assignments can be made using a **theoretical** approach or an **empirical** approach. If an experiment is conducted n times and event E occurs with frequency $f(E)$, then the ratio $f(E)/n$ is called the **relative frequency** of the occurrence of E in n trials, or the **approximate empirical probability of E** .
- If the **equally likely assumption** is made, each simple event of the sample space $S = \{e_1, e_2, \dots, e_n\}$ is assigned the same (theoretical) probability $1/n$.

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- **8.2 Union, Intersection, and Complement of Events; Odds**
 - Let A and B be two events in a sample space S . Then $A \cup B = \{x \mid x \in A \text{ or } x \in B\}$ is the **union** of A and B ; $A \cap B = \{x \mid x \in A \text{ and } x \in B\}$ is the **intersection** of A and B .
 - Events whose intersection is the empty set are said to be **mutually exclusive** or **disjoint**.
 - The probability of the union of two events is given by $P(A \cup B) = P(A) + P(B) - P(A \cap B)$.

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■ 8.2 Union, Intersection, and Complement of Events; Odds (continued)

- The **complement** of event E , denoted E' , consists of those elements of S that do not belong to E .

$$P(E') = 1 - P(E)$$

- The language of **odds** is sometimes used, as an alternative to the language of probability, to describe the likelihood of an event. If $P(E)$ is the probability of E , then the **odds for E** are $P(E)/P(E')$, and the **odds against E** are $P(E')/P(E)$.
- If the odds for an event are a/b , then $P(E) = \frac{a}{a+b}$.

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■ 8.3 Conditional Probability, Intersection, and Independence

- If A and B are events in a sample space S , and $P(B) \neq 0$, then the **conditional probability of A given B** is defined by
$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$
- By solving this equation for $P(A \cap B)$ we obtain the **product rule** $P(A \cap B) = P(B) P(A|B) = P(A) P(B|A)$
- Events A and B are **independent** if $P(A \cap B) = P(A) P(B)$.

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■ 8.4 Bayes' Formula

Let $U_1, U_2, \dots, U_n$ be n mutually exclusive events whose union is the sample space S . Let E be an arbitrary event in S such that $P(E) \neq 0$. Then

$$P(U_1|E) = \frac{\text{product of branch probabilities leading to } E \text{ through } U_1}{\text{sum of all branch products leading to } E}$$

Similar results hold for $U_2, U_3, \dots, U_n$

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- **8.5 Random Variable, Probability Distribution, and Expected Value**
 - A **random variable** X is a function that assigns a numerical value to each simple event in a sample space S .
 - The **probability distribution of X** assigns a probability $p(x)$ to each range element x of X : $p(x)$ is the sum of the probabilities of the simple events in S that are assigned the numerical value x .

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■ 8.5 Random Variable, Probability Distribution, and Expected Value (continued)

- If a random variable X has range values $x_1, x_2, \dots, x_n$ which have probabilities $p_1, p_2, \dots, p_n$, respectively, the **expected value of X** is defined by

$$E(X) = x_1p_1 + x_2p_2 + \dots + x_np_n$$

- Suppose the x_i 's are payoffs in a game of chance. If the game is played a large number of times, the expected value approximates the average win per game.