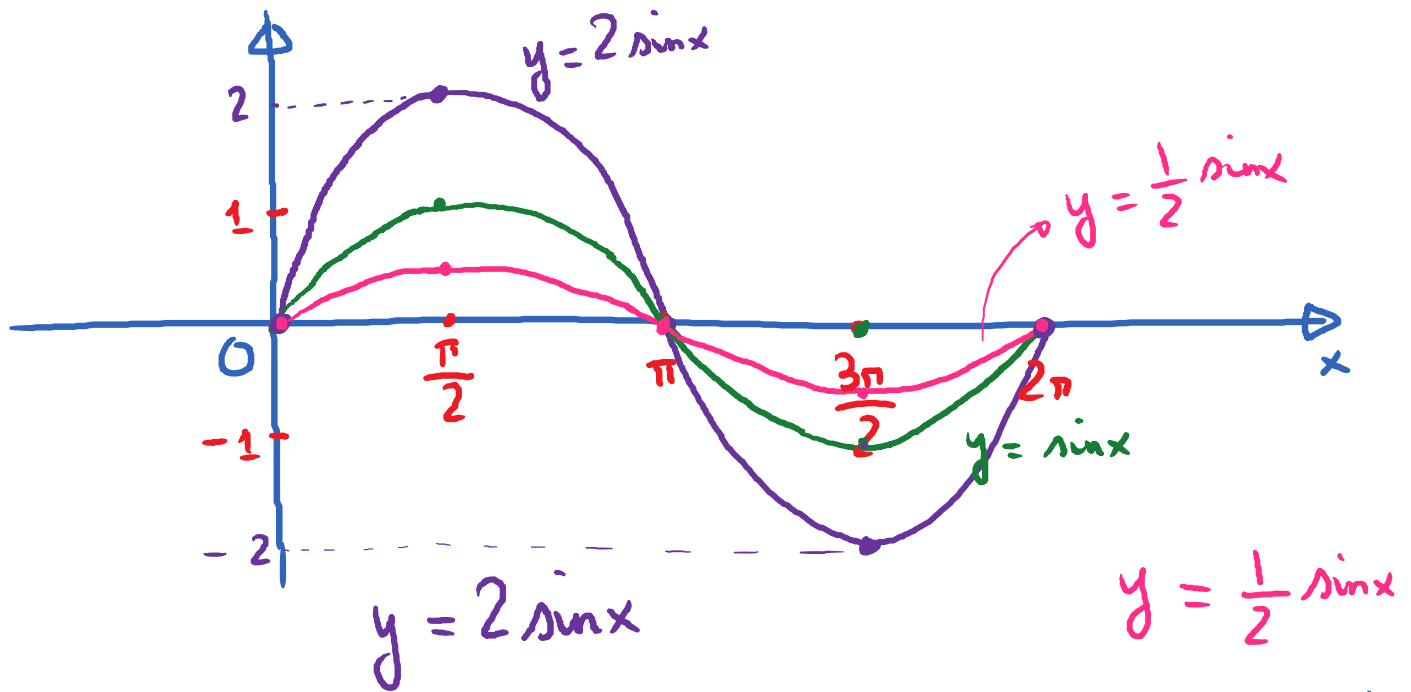


# Graphs of functions of the form $y = a \sin x$



$x$	$y = \sin x$
0	0
$\frac{\pi}{2}$	1
$\pi$	0
$\frac{3\pi}{2}$	-1
$2\pi$	0

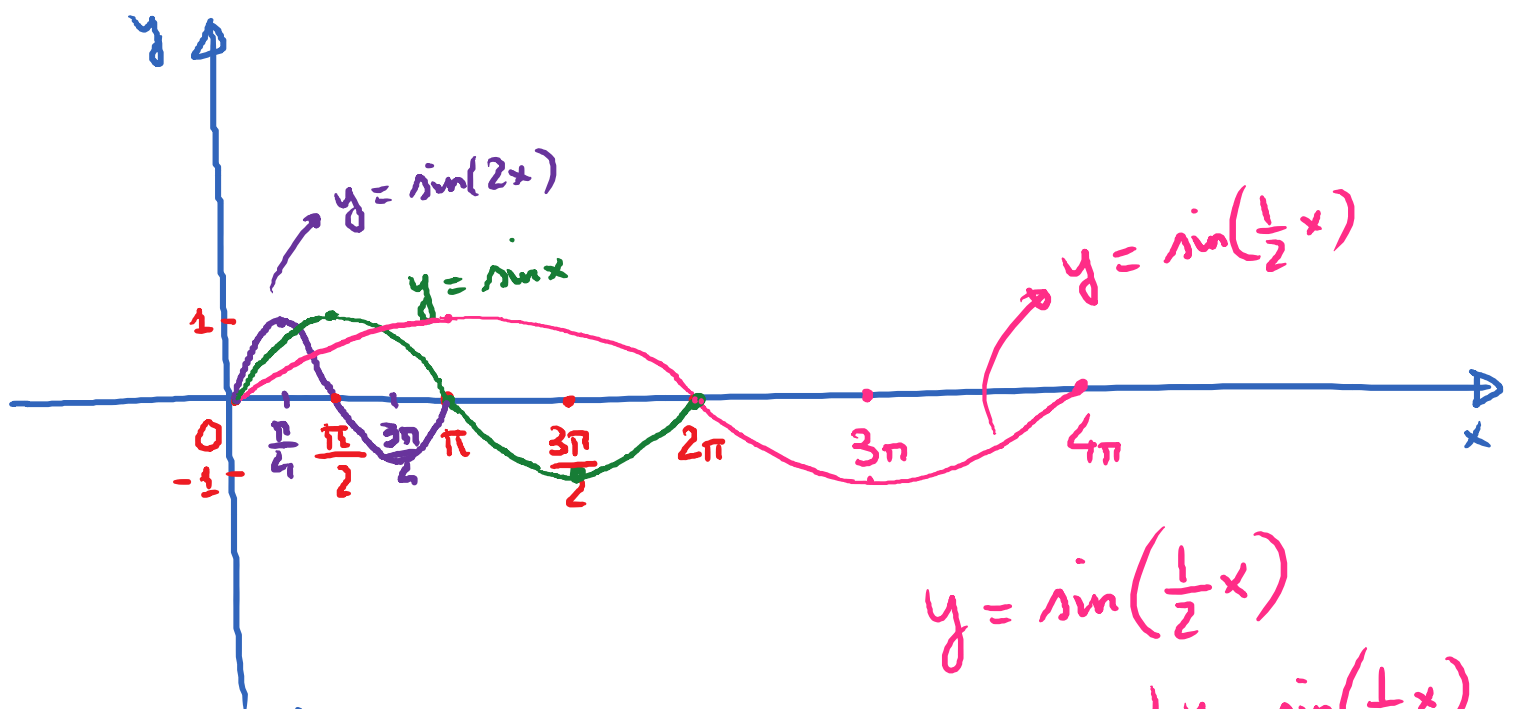
$x$	$y = 2 \sin x$
0	0
$\frac{\pi}{2}$	2
$\pi$	0
$\frac{3\pi}{2}$	-2
$2\pi$	0

$x$	$y = \frac{1}{2} \sin x$
0	0
$\frac{\pi}{2}$	$\frac{1}{2}$
$\pi$	0
$\frac{3\pi}{2}$	$-\frac{1}{2}$
$2\pi$	0

The amplitude of a periodic function is half the difference between the maximum and the minimum values of the function

In general, the amplitude of  $y = a \sin x$  or  $y = a \cos x$  is  $|a|$ .

Graphs of functions of the form  $y = \sin(bx)$



$x$	$y = \sin x$
$0$	$0$
$\frac{\pi}{2}$	$1$
$\pi$	$0$
$\frac{3\pi}{2}$	$-1$
$2\pi$	$0$

$x$	$y = \sin(\frac{1}{2}x)$
$0$	$0$
$\pi$	$1$
$2\pi$	$0$
$3\pi$	$-1$
$4\pi$	$0$

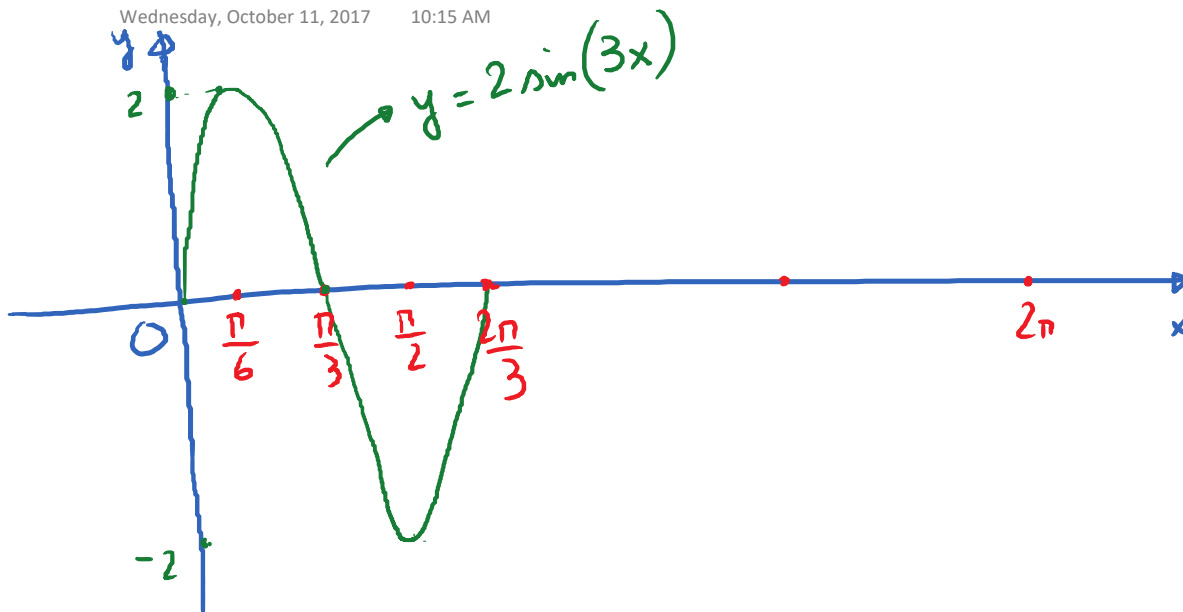
The period of the function  $y = \sin(bx)$  or  $y = \cos(bx)$  is  $\frac{2\pi}{b}$ .

Graphs of Functions of the form  $y = a \sin(bx)$

E.g. Graph the function  $y = 2 \sin(3x)$  in one period.

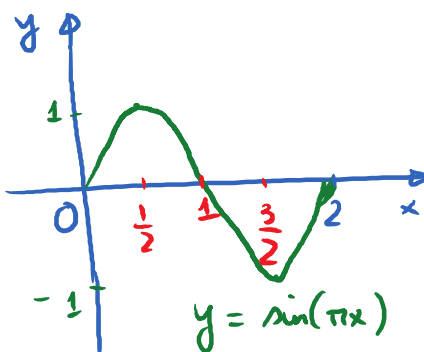
Period =  $\frac{2\pi}{3}$ ; Amplitude = 2.

$x$	$y = \sin x$		$x$	$y = 2 \sin(3x)$
0	0		0	0
$\frac{\pi}{2}$	1	→	$\frac{\pi}{6}$	2
$\pi$	0	→	$\frac{\pi}{3}$	0
$\frac{3\pi}{2}$	-1	→	$\frac{\pi}{2}$	-2
$2\pi$	0	→	$\frac{2\pi}{3}$	0



E.g. Graph  $y = \sin(\pi x)$

$x$	$y = \sin x$		$x$	$y = \sin(\pi x)$
$0$	$0$	$\rightarrow$	$0$	$0$
$\frac{\pi}{2}$	$1$	$\rightarrow$	$\frac{1}{2}$	$1$
$\pi$	$0$	$\rightarrow$	$1$	$0$
$\frac{3\pi}{2}$	$-1$	$\rightarrow$	$\frac{3}{2}$	$-1$
$2\pi$	$0$	$\rightarrow$	$2$	$0$



Ex. Graph  $y = 3 \cos(\pi x)$  in one period.

$x$	$y = \cos x$

$x$	$y = 3 \cos(\pi x)$

Solved!