

Goals: ① Understand Set Notations

- ② Perform Operations on sets
- ③ Solve some applications

Definition of a set:

A set is a collection of objects

E.g.

$$A = \{1, 2, 3\} \leftarrow \text{listing method.}$$

$$B = \{a, b, c, d, e, f\}$$

$$C = \{ \text{Jan, Feb, Mar, May, Jun, Nov} \}$$

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$\mathbb{R}$  = set of all real numbers.

$\mathbb{Z}$  = set of all integers.

Notation:  $e \in A$

This notation means that  $e$  is an element of the set  $A$ .

E.g.  $A = \{1, 2, 3\}$

$1 \in A$ .  $2 \in A$ .  $3 \in A$ .

$B = \{\text{all states in the U.S}\}$

$\text{TX} \in B$ ,  $\text{CA} \in B$ ,  $\text{AZ} \in B$ .

$\mathbb{Z}$ .  $-100 \in \mathbb{Z}$ ,  $10402 \in \mathbb{Z}$ .

Notation:  $e \notin A$ .

This means that  $e$  is NOT an element of the set  $A$ .

$A = \{1, 2, 3\}$ .  $6 \notin A$ .

$B = \{\text{all States in the U.S}\}$ .

$10 \notin B$ ;  $\text{China} \notin B$

$\mathbb{Z}$ .  $\frac{3}{5} \notin \mathbb{Z}$ .

# Empty Set or Null Set

E.g. Describe the set of real numbers that are the solution to the equation.

$$x^2 + 1 = 0$$

$$x^2 = -1$$

$$x = \pm\sqrt{-1}$$

No real solutions.

The solution set of this equation has no elements in it. It is the empty set or the null set.

Notation for the empty set:  $\emptyset$

## Set Builder Notation .

$A = \{a, b, c, d, \dots, z\} \rightarrow$  listing method

Instead of using the listing method, we can use set builder notation to describe the set.

$A = \{x \mid x \text{ is a letter of the English alphabet}\}$

read as "such that"

$B = \{x \mid x \text{ is a month in the year}\}$

$C = \{x \mid x \text{ is a rational number}\}$

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## Subsets

Definition: A and B are sets.

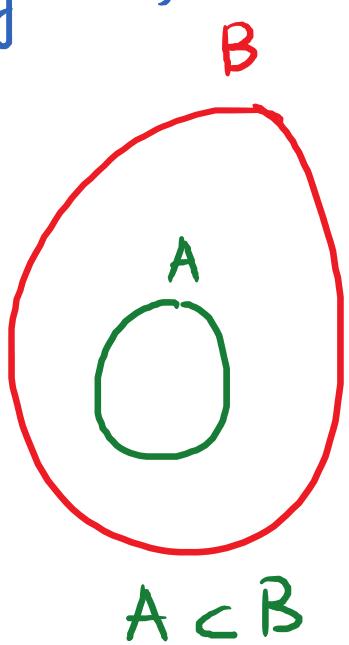
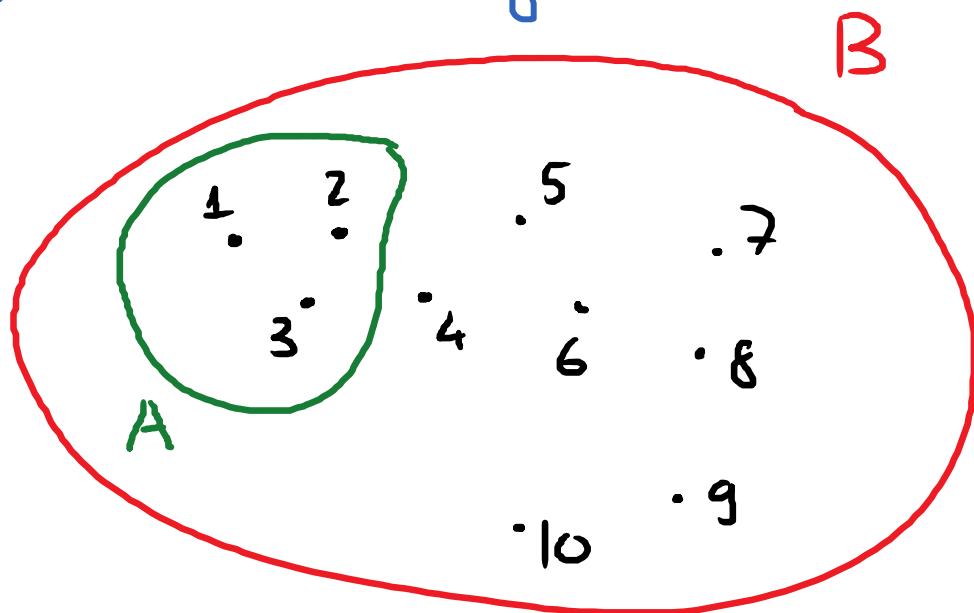
We say that A is a subset of B if every element of A is also an element of B

E.g.  $A = \{1, 2, 3\}$ .  $B = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$

A is a subset of B.

Notation for subset:  $A \subset B$

To visualize sets and the relations among sets, we can use Venn Diagram.



Note:  $\emptyset$  is a subset of every set.

E.x.  $A = \{1, 2, 3\}$ .

Find all the subsets of this set.

$\boxed{\emptyset}, \{1\}, \{2\}, \{3\}, \{1, 2\}, \{1, 3\};$   
 $\{2, 3\}, \boxed{\{1, 2, 3\}}$  → 8 subsets

E.x.  $B = \{1, 2, 3, 4\}$  → 16 subsets.

$\emptyset, \{1\}, \{2\}, \{3\}, \{4\}, \{1, 2\}, \{1, 3\}, \{1, 4\},$   
 $\{2, 3\}, \{2, 4\}, \{3, 4\}, \{1, 2, 3, 4\}$   
 $\{1, 2, 3\}; \{2, 3, 4\}, \{1, 2, 4\}, \{1, 3, 4\}$

E.x.  $C = \{1, 2, 3, 4, 5\}$  → How many subsets?  
32 subsets