

③  $x^2 + y^2 = 8$ . Same question.

$$y^2 = 8 - x^2$$

$$y = \pm \sqrt{8 - x^2}$$

**NO**.

④  $6x - 5y = 7$ . Same question

$$-5y = 7 - 6x$$

$$y = \frac{7 - 6x}{-5}$$

**YES**.

## Obj 4: Evaluate Functions

Function Notation: The notation  $f(x)$  is read as  $f$  of  $x$  (or the value of the function  $f$  at the variable  $x$ ).

$f$  is just the name of the function

$x$  is called the independent variable.

Note:  $f(x)$  DOES NOT mean  $f$  times  $x$ .

E.g.:  $y = 16 - x^2$

↓  
call this  $f(x)$

$$f(x) = 16 - x^2$$

Evaluate this function when  $x = 4$

✓ Notation:  $f(4)$ ;  $f(-2)$

$$f(4) = 16 - (4)^2 = 16 - 16 = 0$$

$f(4) = 0$  (the value of  $f$  at  $x = 4$  is 0)

$$f(-2) = 16 - (-2)^2 = 16 - 4 = 12$$

$$f(h) = 16 - h^2$$

In the formula,  $f(x) = 16 - x^2$ ,  $x$  is a placeholder.

It is a placeholder for any value we evaluate the function at.

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E.g. Given  $g(x) = x^2 + 2x + 3$ .

Evaluate the following and simplify.

(a)  $g(-4)$

(c)  $g(2h)$

(b)  $g(h)$

(d)  $g(h+a)$

(e)  $g(x+1)$

(f)  $g(-x)$

$$g(x) = x^2 + 2x + 3$$

$$\textcircled{a} \quad g(-4) = (-4)^2 + 2 \cdot (-4) + 3 = 16 - 8 + 3 = \boxed{11}$$

$$\textcircled{b} \quad g(h) = h^2 + 2h + 3$$

$$\textcircled{c} \quad g(2h) = (2h)^2 + 2 \cdot (2h) + 3 = \boxed{4h^2 + 4h + 3}$$

$$\begin{aligned} \textcircled{d} \quad g(\boxed{h+a}) &= (h+a)^2 + 2(h+a) + 3 \\ &= (h+a)(h+a) + 2h + 2a + 3 \\ &= h^2 + 2ah + a^2 + 2h + 2a + 3 \end{aligned}$$

$$\begin{aligned} \textcircled{e} \quad g(\boxed{x+1}) &= (x+1)^2 + 2(x+1) + 3 \\ &= (x+1)(x+1) + 2x + 2 + 3 \\ &= x^2 + 2x + 1 + 2x + 5 \end{aligned}$$

$$g(x+1) = x^2 + 4x + 6$$

$$\textcircled{f} \quad g(\boxed{-x}) = (-x)^2 + 2(-x) + 3$$

$$g(-x) = x^2 - 2x + 3$$

Obj 5: Graph functions by plotting points

Definition: The graph of a function is the graph of its ordered pairs.

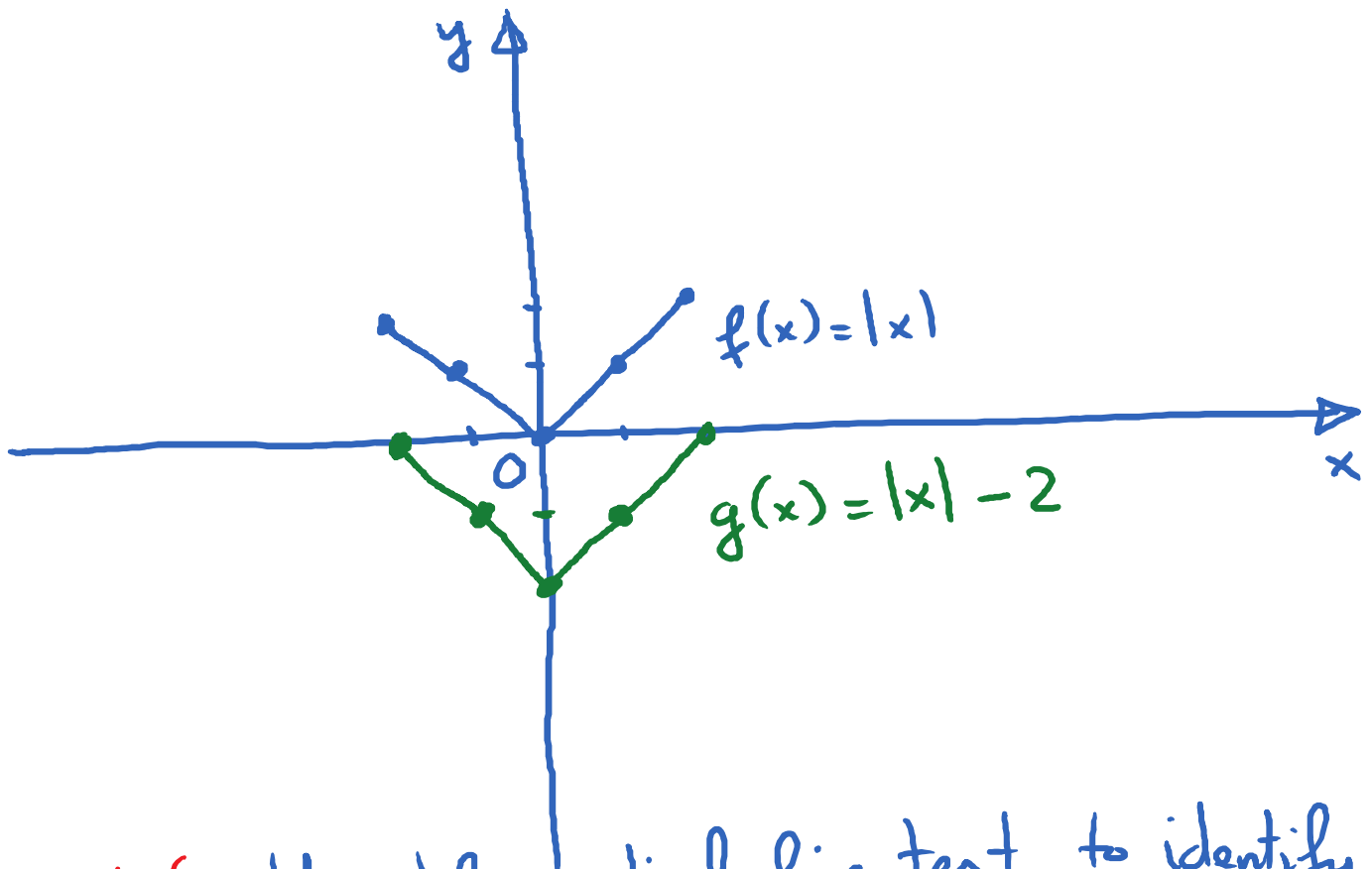
E.g. Graph the functions  $f(x) = |x|$  and  $g(x) = |x| - 2$  in the same coordinate plane. Choose integer values of  $x$  starting with  $-2$  and ending with  $2$ .

$$f(x) = |x|$$

$x$	$f(x)$
-2	2 $\rightarrow (-2, 2)$
-1	1 $\rightarrow (-1, 1)$
0	0 $\rightarrow (0, 0)$
1	1 $\rightarrow (1, 1)$
2	2 $\rightarrow (2, 2)$

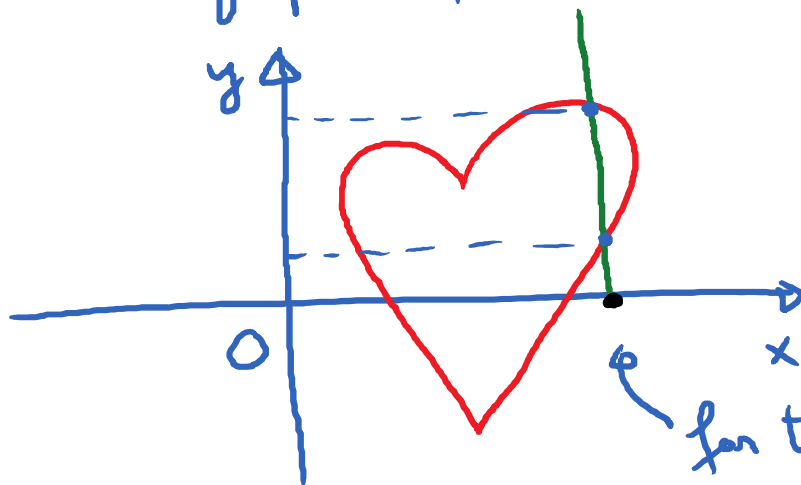
$$g(x) = |x| - 2$$

$x$	$g(x)$
-2	0 $\rightarrow (-2, 0)$
-1	-1 $\rightarrow (-1, -1)$
0	-2 $\rightarrow (0, -2)$
1	-1 $\rightarrow (1, -1)$
2	0 $\rightarrow (2, 0)$



Obj # 6: Use the vertical line test to identify graphs of functions

NOT a function.



for this value of  $x$ , we get 2 values of  $y$ .