

There are many correct answers for this one:

$$f(x) = \frac{3}{x}; g(x) = \sqrt{8x+7}$$

$$\text{or } f(x) = \frac{3}{\sqrt{x}}; g(x) = 8x+7$$

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$$\begin{aligned} (f \circ g)(x) &= \frac{1 + \frac{1}{x-1}}{\frac{1}{x-1}} = \frac{\frac{x-1+1}{x-1}}{\frac{1}{x-1}} = \frac{x}{\frac{1}{x-1}} \\ &= \frac{x}{x-1} \cdot \frac{x-1}{1} = x \end{aligned}$$

$$(g \circ f)(x) = \frac{1}{\frac{1+x}{x} - 1} = \frac{1}{\frac{1+x-x}{x}} = \frac{1}{\frac{1}{x}} = x$$

$$\text{So, } (f \circ g)(x) = x \text{ and } (g \circ f)(x) = x$$

So, f and g are inverses of each other.

The vertex is $(2, 2)$. Plug the vertex to the standard form, we have:

$$f(x) = a(x-2)^2 + 2$$

The y -intercept is $(0, 6)$. So,

$$6 = a(-2)^2 + 2, \text{ So, } 6 = 4a + 2. \text{ So, } a = 1.$$

Equation for the quadratic function is:

$$f(x) = (x-2)^2 + 2$$

$$(x^3 - 3) \div (x - 1)$$

$$\begin{array}{r|rrrrr} 1 & 1 & 0 & 0 & -3 \\ & \downarrow & & & & \\ & 1 & 1 & 1 & 1 & \end{array}$$

Remainder

$$\text{Quotient: } x^2 + x + 1$$