

Test 1 Review

Tuesday, September 18, 2018

1:58 PM

#1 Plug the ordered pair into the equation

$$4x - 3y = 28$$

\downarrow \downarrow
4 4

$$4 \cdot (4) - 3 \cdot (4) \stackrel{?}{=} 28$$

$$4 \neq 28$$

Answer: NO

#2 $f(2) = 4 \cdot (2)^2 + 5(2) - 5$
 $= 21$

#3 Domain = Projection of Graph onto the x-axis
 $= [-4, 4]$

#4 $f(x) = \frac{7}{2-x}$. Find Domain?

Step 1: Set Denominator = 0 and Solve for x.

$$2-x=0 \rightarrow x=2$$

Step 2: Domain = All real #s except for $x=2$

$$= (-\infty, 2) \cup (2, \infty)$$

$$= \boxed{\{x \mid x \neq 2\}} \rightarrow \text{choice B.}$$

#5 $(f/g)(3) = \frac{f(3)}{g(3)}$

From the graphs, $f(3) = 1$ and $g(3) = -1$.

$$\text{So, } \frac{f(3)}{g(3)} = \frac{1}{-1} = \boxed{-1}$$

#6 $(f \cdot g)(x) = f(x) \cdot g(x) = (5x-6) \cdot (6x-9)$

$$= \boxed{30x^2 - 81x + 54}$$

#7

$$\text{Slope} = \frac{-17 - (-13)}{2 - 7} = \frac{-17 + 13}{-5} = \frac{-4}{-5} = \boxed{\frac{4}{5}}$$

#8

$$\text{Slope} = \frac{\text{change in } y}{\text{change in } x} = \frac{\text{Rise}}{\text{Run}} = \frac{-10000}{5} = \boxed{-2000}$$

#9

 $(-6, 0)$ and $(-9, 8)$

$$\text{Slope} = \frac{8 - 0}{-9 - (-6)} = \frac{8}{-9 + 6} = \frac{8}{-3} = -\frac{8}{3}$$

$$y - 0 = -\frac{8}{3}(x + 6)$$

$$y = -\frac{8}{3}x - \frac{48}{3} = -\frac{8}{3}x - 16$$

#10 $-9x - 2y = 39 \rightarrow -2y = 9x + 39$

$\rightarrow y = -\frac{9}{2}x - \frac{39}{2} \rightarrow \text{Slope} = -\frac{9}{2}$

Since the line passing through $(-3, -2)$ is parallel to this, its slope is $-\frac{9}{2}$.

Point-Slope Form:

$$y - (-2) = -\frac{9}{2}(x - (-3))$$

Slope-intercept form:

$$y = -\frac{9}{2}(x+3) - 2$$

$$y = -\frac{9}{2}x - \frac{27}{2} - 2$$

$$y = -\frac{9}{2}x - \frac{31}{2}$$

#11 $3x - 2y = 1 \rightarrow -2y = -3x + 1$

$$\rightarrow y = \frac{3}{2}x - \frac{1}{2} \rightarrow \text{Slope} = \frac{3}{2}$$

$$2x + 3y = 1 \rightarrow 3y = -2x + 1$$

$$\rightarrow y = -\frac{2}{3}x + \frac{1}{3} \rightarrow \text{Slope} = -\frac{2}{3}$$

They are
perpendicular

#12 2 data points

| x | y |
|------|------|
| 1.35 | 4820 |
| 1.40 | 3961 |

$\rightarrow (1.35, 4820)$

$\rightarrow (1.40, 3961)$

Find a linear function $y = mx + b$ that fits the data.

Step 1: Find Slope. $m = \frac{3961 - 4820}{1.40 - 1.35}$

$$m = -17180$$

Step 2: Point-Slope Form

$$y - 4820 = -17180(x - 1.35)$$

Step 3: Slope-Intercept Form

$$y = -17180x + 23193 + 4820$$

$$y = -17180x + 28013$$

At price of \$1.23,

$$y = (-17180) \cdot (1.23) + 28013$$

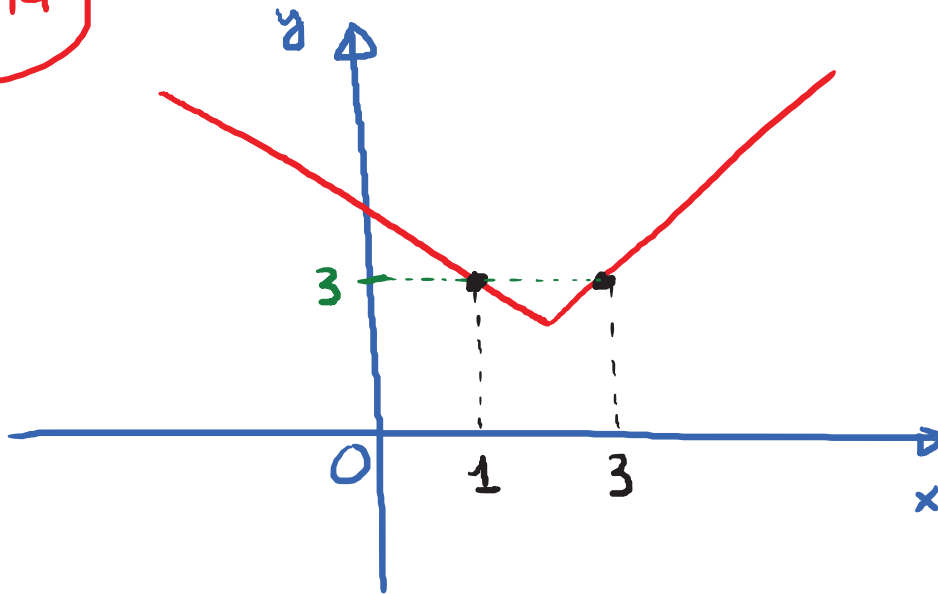
$$y = 6881.6$$

Short Answer Part:

$$\textcircled{\#13} \quad \underbrace{P(33)}_{\text{pressure at the depth of 33 ft}} = 1 + \frac{33}{33} = \boxed{2} \text{ (atm)}$$

pressure at
the depth of 33 ft

#14

Answer: $x=1$ and $x=3$.

#15

$$f(x) = \frac{2}{x-12} ; g(x) = 7x - 5$$

Step 1: Find D_f .

$$D_f = (-\infty, 12) \cup (12, \infty)$$

Step 2: Find D_g .

$$D_g = (-\infty, \infty)$$

Step 3: Find $D_f \cap D_g$.

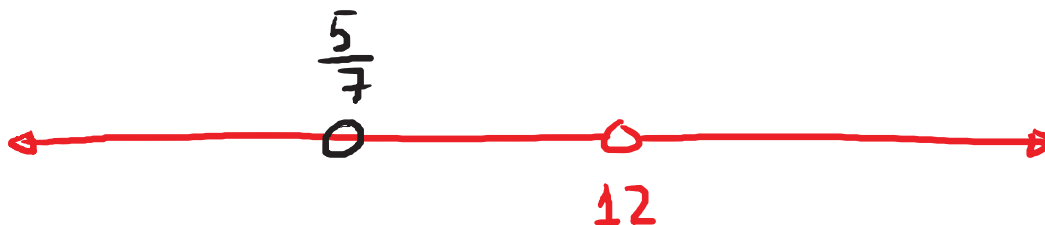
$$D_f \cap D_g = (-\infty, 12) \cup (12, \infty)$$

Step 4: Find x such that $g(x) = 0$

$$7x - 5 = 0 \longleftrightarrow x = \frac{5}{7}$$

exclude

Step 5: Conclusion:



Interval Notation: $(-\infty, \frac{5}{7}) \cup (\frac{5}{7}, 12) \cup (12, \infty)$

Set Builder Notation: $\{x \mid x \neq \frac{5}{7} \text{ and } x \neq 12\}$

#16

$$6x - 8y = 8 \longleftrightarrow -8y = -6x + 8$$

$$\longleftrightarrow y = \frac{3}{4}x - 1$$

Slope = $\frac{3}{4}$; y-intercept: $(0, -1)$

#17

$$y = -\frac{8}{5}x + \frac{39}{5}$$

#18

$$7x - 8y = -30 \rightarrow -8y = -7x - 30$$

$$\rightarrow y = \frac{7}{8}x + \frac{15}{4} \rightarrow \text{Slope} = \frac{7}{8}$$

Slope of line passing through $(6, -9)$ and perpendicular to this is $-\frac{8}{7}$.

$$\text{Point-Slope Form: } y - (-9) = -\frac{8}{7}(x - 6)$$

$$y + 9 = -\frac{8}{7}(x - 6)$$

$$\text{Slope-intercept form: } y = -\frac{8}{7}x + \frac{48}{7} - 9$$

$$y = -\frac{8}{7}x - \frac{15}{7}$$

#19

$$f(x) = 6x^2 + 3x$$

$$\begin{aligned} f(2a) &= 6(2a)^2 + 3(2a) \\ &= 6(4a^2) + 6a \end{aligned}$$

$$f(2a) = 24a^2 + 6a$$

#20

Point-Slope Form:

$$y - (-4) = -\frac{4}{5}(x - 7)$$

$$y + 4 = -\frac{4}{5}(x - 7)$$

Slope-Intercept Form:

$$y = -\frac{4}{5}x + \frac{28}{5} - 4$$

$$y = -\frac{4}{5}x + \frac{8}{5}$$