

$$\begin{cases} u = x^2 \end{cases}$$

$$du = 2x dx$$

$$\begin{cases} dv = e^{-(n+2)x} dx \end{cases} \rightarrow$$

$$v = -\frac{1}{n+2} e^{-(n+2)x}$$

$$-\frac{x^2}{n+2} e^{-(n+2)x} + \int \frac{2x}{n+2} e^{-(n+2)x} dx$$

$$-\frac{x^2}{n+2} e^{-(n+2)x} + \frac{2}{n+2} \int x \cdot e^{-(n+2)x} dx$$

$$\begin{cases} u = x \\ dv = e^{-(n+2)x} dx \end{cases} \rightarrow \begin{cases} du = dx \\ v = -\frac{1}{n+2} e^{-(n+2)x} \end{cases}$$

$$-\frac{x}{n+2} e^{-(n+2)x} + \frac{1}{n+2} \int e^{-(n+2)x} dx$$

$$-\frac{x^2}{n+2} e^{-(n+2)x} - \frac{2x}{(n+2)^2} e^{-(n+2)x} + \frac{2}{(n+2)^2} \left(-\frac{1}{n+2} e^{-(n+2)x} \right)$$

$$\left(-\frac{x^2}{n+2} e^{-(n+2)x} - \frac{2x}{(n+2)^2} e^{-(n+2)x} - \frac{2}{(n+2)^3} e^{-(n+2)x} \right) \Big|_0^\infty$$

$$\rightarrow \boxed{\frac{2}{(n+2)^3}}$$