

(11)

$$f(x) = \frac{1}{5}x + 7$$

$$y = \frac{1}{5}x + 7 \quad (\text{Replace } f(x) \text{ with } y)$$

$$x = \frac{1}{5}y + 7 \quad (\text{Interchange } x \text{ and } y)$$

$$x - 7 = \frac{1}{5}y$$

$$5(x - 7) = y$$

$$5x - 35 = y$$

$$y = 5x - 35 \rightarrow f^{-1}(x) = 5x - 35$$

Answer: D.

(12)

Do $f(g(x))$; $f(h(x))$; $g(h(x))$, we see that:

$$g(h(x)) = 2\left(\frac{x+8}{2}\right) - 8 = x + 8 - 8 = x.$$

The other two do not simplify to x .

So, $g(x)$ and $h(x)$ are inverses of one another.

Answer: A.

Short Answer:

(13)

$$y = |x| \xrightarrow[\text{by } 3.9]{\text{vertically stretch}} 3.9|x|$$

(original)

Reflected across x-axis

$$-3.9|x| - 0.59 \xleftarrow{0.59 \text{ down}} -3.9|x|$$

So, final formula: $y = -3.9|x| - 0.59$ ← answer.

14

$$y = f(x)$$

original

$$y = f(x+1)$$

transformed

Left 1

x	$y = f(x)$
7	18

$(7, 18)$

original

Left 1

$(6, 18)$

Subtract x-coord. by 1

Answer:

$(6, 18)$

15

$$f(x) = \frac{x}{\sqrt{x-3}}$$

This has square root in denominator.

To find domain: Set $x-3 > 0$

$$x > 3$$

In interval notation:

$$D = (3, \infty)$$

16

$$f(x) = \frac{x-5}{2}; \quad g(x) = 7x+2$$

$$(g \circ f)(15)$$

Plug 15 into f , simplify, then plug result into g .

$$f(15) = \frac{(15) - 5}{2} = 5$$

$$g(5) = 7(5) + 2 = 37$$

Answer: 37

Essay

(17) $f(x) = 4x^2 + 3x + 5$; $g(x) = 3x - 3$

$$\begin{aligned} (g \circ f)(x) &= g(f(x)) = g(4x^2 + 3x + 5) \\ &= 3(4x^2 + 3x + 5) - 3 \\ &= 12x^2 + 9x + 15 - 3 \end{aligned}$$

$$(g \circ f)(x) = 12x^2 + 9x + 12$$

(18) $f(x) = \frac{5}{7x-1}$. Find inverse

$$y = \frac{5}{7x-1} \quad (\text{Replace } f(x) \text{ with } y)$$

$$x = \frac{5}{7y-1} \quad (\text{interchange } x \text{ and } y)$$

$$x(7y-1) = \left(\frac{5}{7y-1}\right) \cancel{(7y-1)} \quad (\text{Multiply both sides by } 7y-1)$$

$$x(7y-1) = 5$$

$$7y-1 = \frac{5}{x} \quad (\text{Divide both sides by } x)$$

$$7y = \frac{5}{x} + 1 \quad (\text{Add } 1)$$

$$y = \frac{\frac{5}{x} + 1}{7} \quad (\text{Divide by } 7)$$

$$f^{-1}(x) = \frac{\frac{5}{x} + 1}{7} \quad (\text{Replace } y \text{ by } f^{-1}(x))$$

(You can leave the answer like this or simplify as follows:

$$\begin{aligned} f^{-1}(x) &= \frac{\frac{5}{x} + \frac{1 \cdot x}{1 \cdot x}}{7} = \frac{\frac{5+x}{x}}{\frac{7}{1}} \\ &= \frac{5+x}{x} \cdot \frac{1}{7} = \frac{5+x}{7x} \end{aligned}$$