

2.1. Basics of Functions and Their graphs - Part 2

Tuesday, January 28, 2020

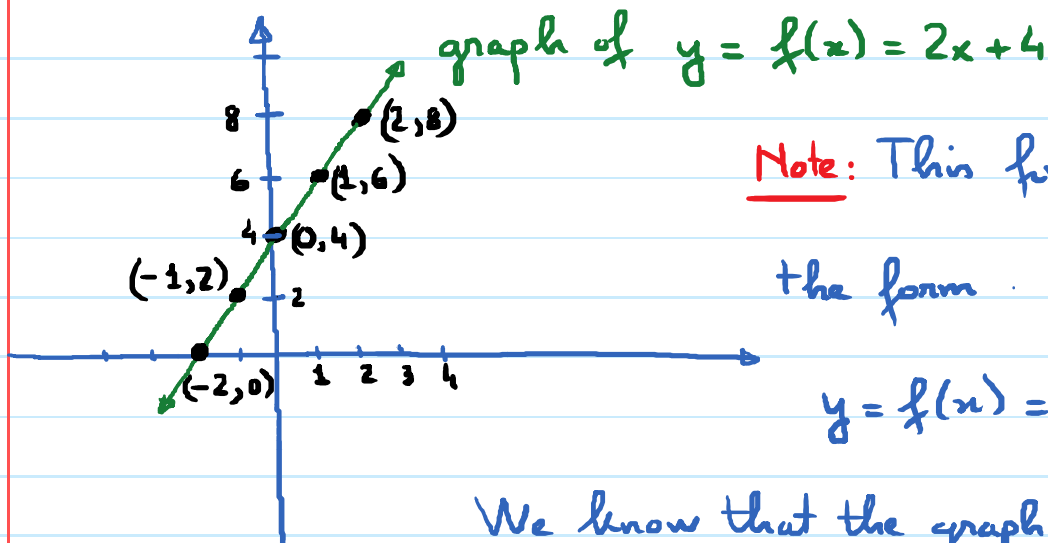
10:03 AM

Objective 1: Graphs of Functions.

Definition: The graph of a function is the graph of its ordered pairs.

E.g. $f(x) = 2x + 4$

| x | $y = f(x) = 2x + 4$ | Ordered pair (x, y) |
|-----|---------------------|-----------------------|
| -2 | 0 | $(-2, 0)$ |
| -1 | 2 | $(-1, 2)$ |
| 0 | 4 | $(0, 4)$ |
| 1 | 6 | $(1, 6)$ |
| 2 | 8 | $(2, 8)$ |



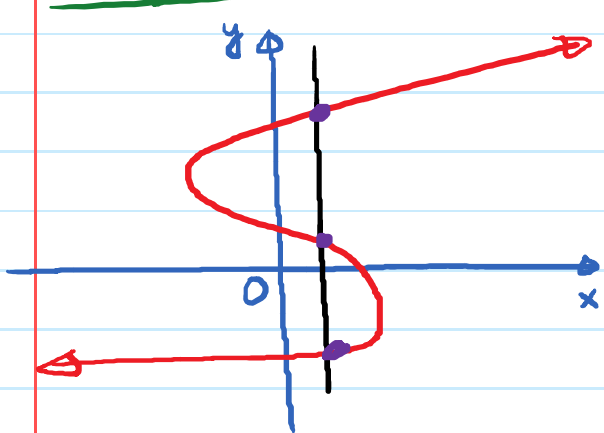
Note: This function has the form

$$y = f(x) = mx + b$$

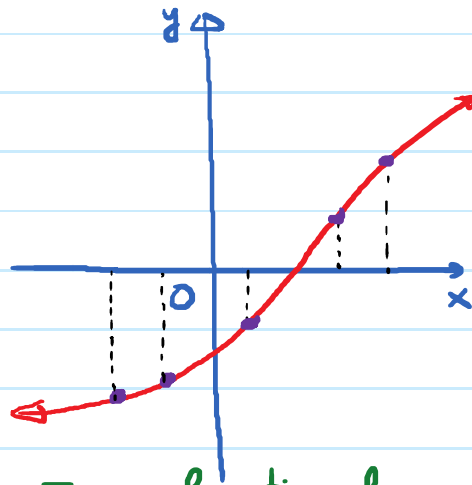
We know that the graph of any function of this form is a straight line.

So, we really just need 2 points to sketch the graph.

Obj 2: Use the vertical line test.



Not a function of y in terms of x

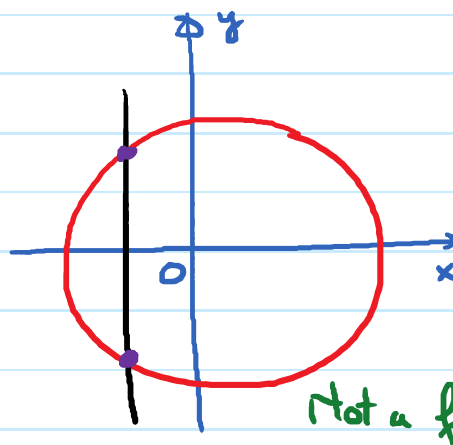
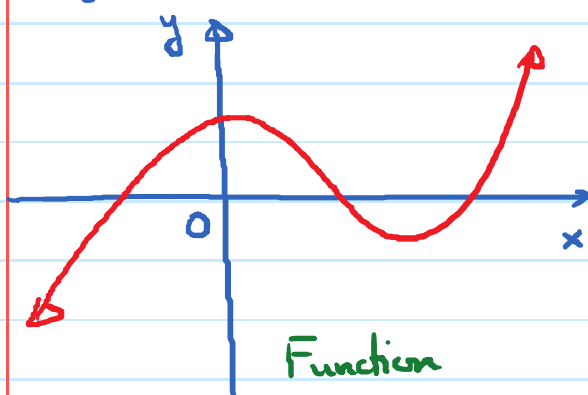


Is a function of y in terms of x

The vertical line test:

If any vertical line intersects a graph in more than one point, then the graph does not define y as a function of x .

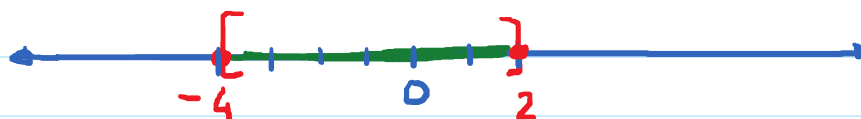
E.g.



Obj 3: Identify Domain and Range of a function from the graph.

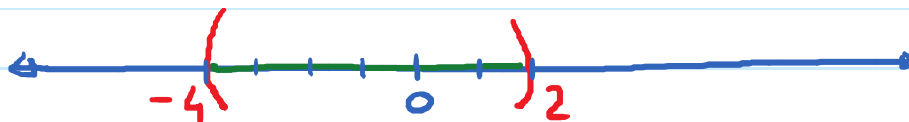
Recall: Interval Notation:

What is the difference between $[-4, 2]$ and $(-4, 2)$?



$[-4, 2]$: all the numbers in between -4 and 2 and

including the number -4 and the number 2



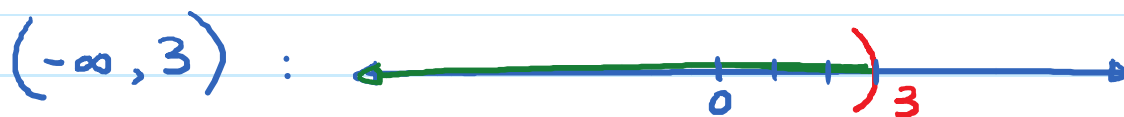
$(-4, 2)$: all the numbers in between -4 and 2

and excluding -4 and 2

$[-4, 2)$: all the numbers in between -4 and 2
and including -4 and excluding 2.



all numbers ≥ -2



all numbers < 3

* Set builder notation:

Set builder

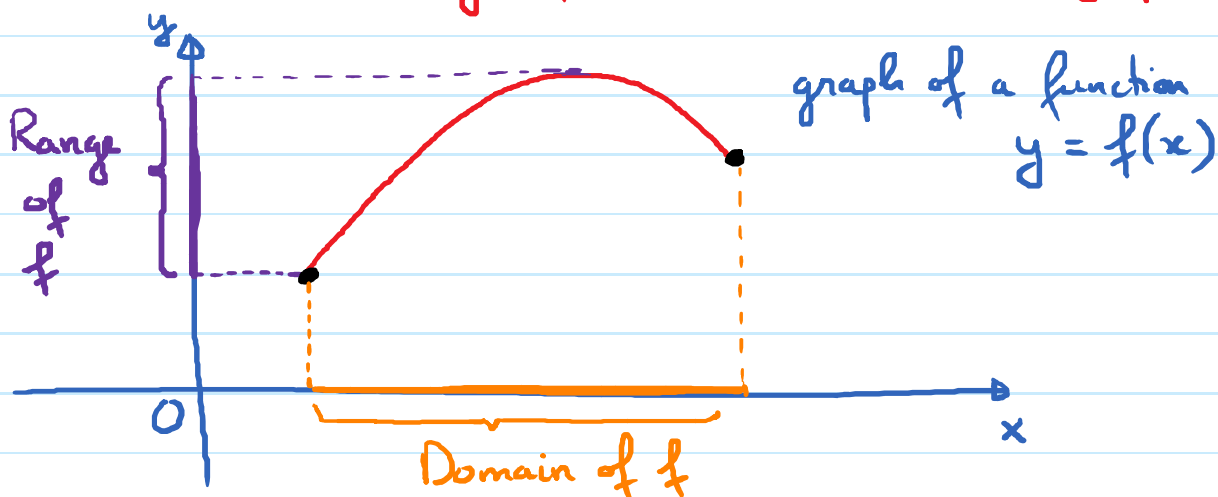
$[-4, 2)$

Interval notation

$= \{x \mid -4 \leq x < 2\}$

notation

* Domain and Range of a function from its graph.



Domain: Set of inputs (found on x-axis from the x-coordinate of the leftmost point of the graph to the x-coordinate of the rightmost point of the graph)