

Test 2 Review

Tuesday, March 3, 2020 9:37 AM

MC

① $y = x^2$: Parent Function.

$$f(x) = \frac{1}{2} (x + 3)^2 - 10$$

Annotations for $f(x) = \frac{1}{2} (x + 3)^2 - 10$:

- $\frac{1}{2}$: Multiply by $\frac{1}{2}$ outside
↓
Shrink vertically by $\frac{1}{2}$
- $x + 3$: add 3 inside
↓
Left, 3 units
- $- 10$: subtract 10 outside
↓
Down, 10 units

Choice A.

② Transformation: $g(x) = f(x - 1) + 3$

Annotations for $g(x) = f(x - 1) + 3$:

- $x - 1$: Right, 1 unit
- $+ 3$: up, 3

Coordinate transformation diagram:

$(6, 15) \xrightarrow{\text{Right, 1}} (7, 15) \xrightarrow{\text{up, 3}} (7, 18)$

Annotations for the diagram:

- $(6, 15) \rightarrow (7, 15)$: + 1 to x-coord
- $(7, 15) \rightarrow (7, 18)$: + 3 to y-coord

Choice : B

③ Graph on left : formula : $f(x) = -x^3 + 3x$.

Graph on right is obtained from graph on left by moving 4 units to left.

→ Transformation : $f(x+4)$

So, formula for graph on right :

$$g(x) = -(x+4)^3 + 3(x+4)$$

(Replace x by $x+4$ in the original formula)

Choice : C

④ $g(x) = \frac{2x}{x^2 - 36}$ → denominator

Domain?

Step 1: Set denominator = 0 and solve :

$$x^2 - 36 = 0$$

$$\rightarrow x^2 = 36 \rightarrow x = \pm\sqrt{36} = \pm 6$$

Step 2: Domain = all real numbers excluding ± 6



Interval notation: $(-\infty, -6) \cup (-6, 6) \cup (6, \infty)$

Choice: B

(5) $h(x) = x + 4$; $g(x) = \sqrt{x+2}$

Find $(h+g)(14)$

$$(h+g)(14) = h(14) + g(14)$$

$$h(14) = 14 + 4 = 18 \quad (\text{Plug } 14 \text{ into } h)$$

$$g(14) = \sqrt{14+2} = \sqrt{16} = 4 \quad (\text{Plug } 14 \text{ into } g)$$

Then:

$$(h+g)(14) = 18 + 4 = \boxed{22}$$

Choice: B

⑥ $f(x) = 6 - 5x$; $g(x) = -3x + 5$

Find $f + g$

$$\begin{aligned}(f+g)(x) &= f(x) + g(x) \\ &= \underbrace{(6 - 5x)}_{f(x)} + \underbrace{(-3x + 5)}_{g(x)}\end{aligned}$$

$$(f+g)(x) = -8x + 11 \quad (\text{combine like terms})$$

Choice: C.

⑦

f/g — division:

$$\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)} = \frac{2x - 5}{\sqrt{x+2}}$$

Square root in denominator

To find domain: Set $x+2 > 0$
 $x > -2$



$$\text{Domain} = \boxed{(-2, \infty)}$$

Choice : D.

⑧ $f(x) = \boxed{-4x+2}$; $g(x) = 5x+8$

$$(g \circ f)(x) = g(\underbrace{f(x)})$$

→ plug $f(x)$ into g

$$= 5(-4x+2) + 8$$

$$= -20x + 10 + 8 \quad (\text{Distribute})$$

$$(g \circ f)(x) = -20x + 18 \quad (\text{Combine like terms})$$

Choice : C

⑨ $f(x) = \frac{x-5}{2}$; $g(x) = 7x+2$

Find $(g \circ f)(15)$

1st way of doing this:

$$(g \circ f)(15) = g(f(15)) : \text{Plug 15 into } f$$

then plug result of that into g

Plug 15 into f : $f(15) = \frac{15 - 5}{2} = 5$.

Then plug 5 into g :

$$g(5) = 7 \cdot (5) + 2 = 37$$

2nd way of doing this.

Find $(g \circ f)(x)$ first:

$$\begin{aligned} (g \circ f)(x) &= g(f(x)) = 7 \cdot \left(\frac{x - 5}{2} \right) + 2 \\ &= \frac{7(x - 5)}{2} + 2 \end{aligned}$$

Then: plug 15 into formula for $g \circ f$:

$$(g \circ f)(15) = \frac{7(15 - 5)}{2} + 2 = 37$$

Choice: D.

10

$$f(x) = \sqrt[3]{x - 27}$$

Step 1: Replace $f(x)$ by y :

$$y = \sqrt[3]{x - 27}$$

Step 2: Swap x and y :

$$x = \sqrt[3]{y - 27}$$

Step 3: Solve for y

$$x^3 = y - 27 \quad (\text{Cube both sides})$$

$$x^3 + 27 = y$$

$$\text{So, } y = x^3 + 27$$

Step 4: Replace y by $f^{-1}(x)$

$$f^{-1}(x) = x^3 + 27$$

Choice C

11

$$f(x) = 8x^3 - 7$$

Step 1: Replace $f(x)$ by y :

$$y = 8x^3 - 7$$

Step 2: Swap x and y :

$$x = 8y^3 - 7$$